



Teachers

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- Prof. Elja Arjas, Department of Mathematics and Statistics, University of Helsinki
- Prof. Samuel Kaski, Helsinki University of Technology

 How to encod for the course?

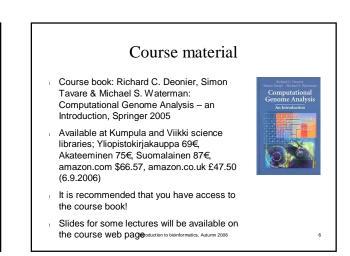
 • Use the registration system of the Computer Science department: https://ilmo.cs.helsinki.fi

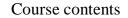
#### How to successfully pass the course?

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- You can get a maximum of 60 points
  - Course exam: maximum of 50 points
  - Exercises: maximum of 10 points
    - 0% completed assignments gives you 0 points, 80% gives 10 points
- Course will be graded on the scale 0-5
- To get the lowest passing grade 1/5, you need to have at least 30 points
- Course exam: Monday 16.10. at 16.00-19.00

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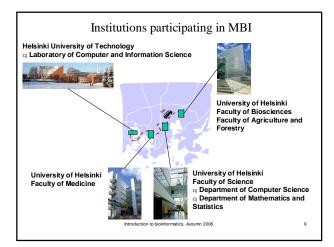
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- Biological background (book chapter 1)
- Probability calculus (chapters 2 and 3)
- Sequence alignment (chapter 6)
- Phylogenetics (chapter 12)
- Expression data analysis (chapter 11)

#### Master's Degree Programme in Bioinformatics (MBI)

- Two-year MSc programme
- Offered jointly by the University of Helsinki and Helsinki University of Technology
- Admission for 2007-2008 in January 2007





### Bioinformatics courses at the University of Helsinki

- Practical course in biodatabases (II period): techniques for accessing and integrating data in biology databases.
- Computational neuroscience (II period): mathematical modeling of information processing taking place in the brain.
- Biological sequence analysis (III period): basic probabilistic methods for modelling and analysis of biological sequences.
- Modeling of vision (III period): mechanisms and modeling of human perception.
- Metabolic modeling (IV period): metabolic networks, fluxes and regulation of metabolism.

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## Bioinformatics courses at the University of Helsinki

#### Department of Mathematics and Statistics

- Modelling fluctuating populations (I and II periods): systems driven by fluctuating parameters
- Evolution and the theory of games (III period): introduction to game theory with emphasis on applications in evolutionary and behavioural biology

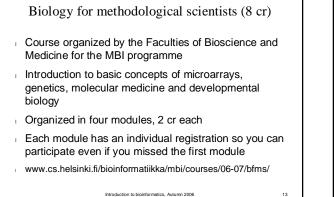
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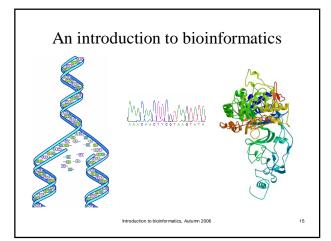
#### Bioinformatics courses at Helsinki University of Technology

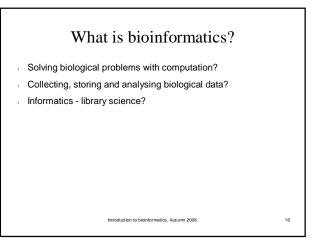
#### Laboratory of Computer and Information Science

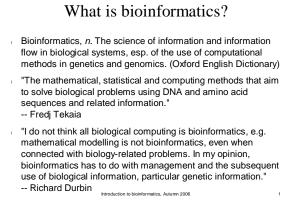
- Special course in bioinformatics II (I and II periods): data integration and fusion in bioinformatics.
- Signal processing in neuroinformatics (I and II periods): overview of some of the main biomedical signal processing techniques
- High-throughput bioinformatics (III and IV periods): computational and statistical methods for analyzing modern high-throughput biological data
- Image analysis in neuroinformatics (III and IV periods): biomedical image processing techniques
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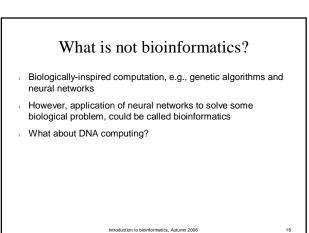


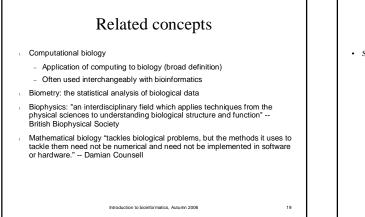


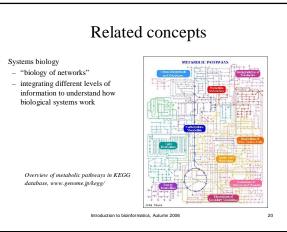


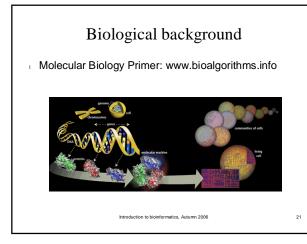


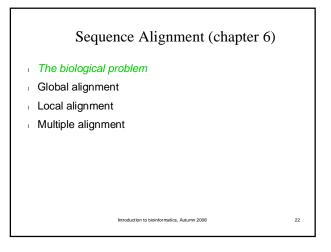












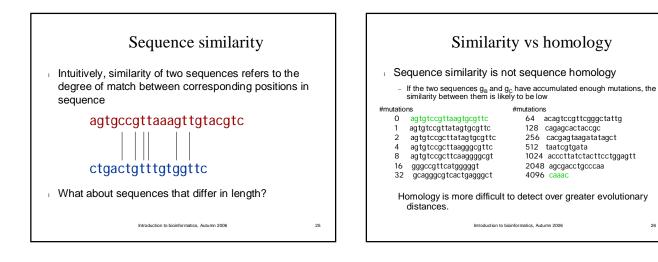
## Background: comparative genomics

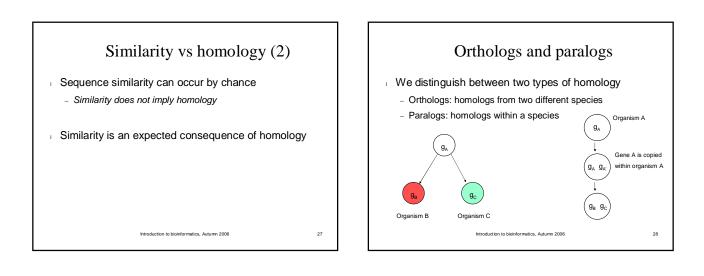
- Basic question in biology: what properties are shared among organisms?
- Genome sequencing allows comparison of organisms at DNA and protein levels
- Comparisons can be used to
  - Find evolutionary relationships between organisms
  - Identify functionally conserved sequences
  - Identify corresponding genes in human and model organisms: develop models for human diseases

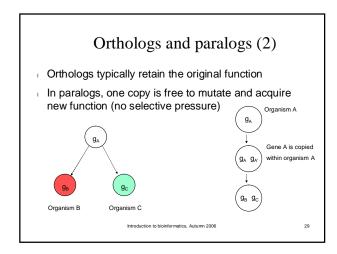
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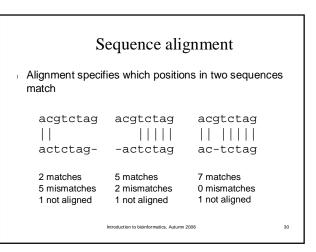
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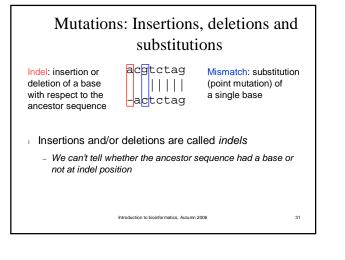
Homologs• Two genes or characters<br/>g<sub>B</sub> and g<sub>C</sub> evolved from<br/>the same ancestor g<sub>A</sub> are<br/>called *homologs*g<sub>A</sub> = agtgccgttaagtgcgtct<br/>age agtgccgttaagtgtgcagtc• Homologs usually exhibit<br/>conserved functionsg<sub>B</sub> = agtgccgttaagttgtacgtc<br/>gc = tgactgttgtggtcc• Close evolutionary<br/>relationship => expect a<br/>igh number of homologsg<sub>B</sub> = agtgccgttagtgtgtgtcgtc

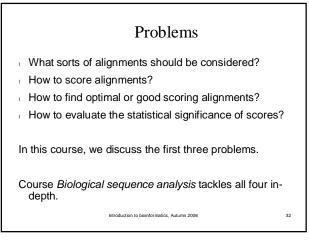


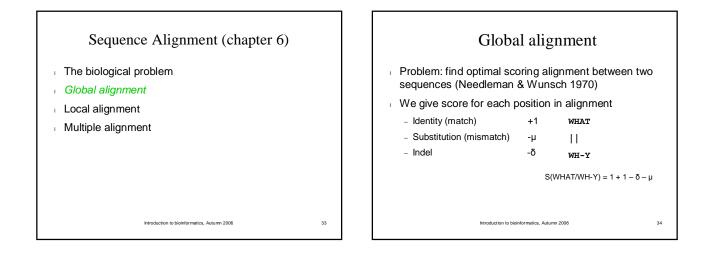


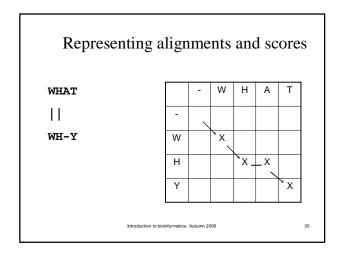


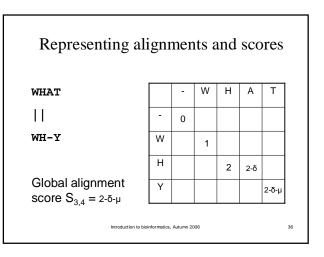


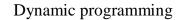










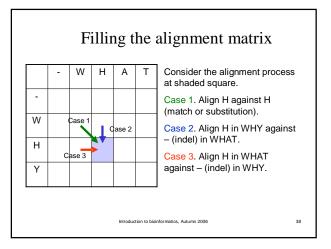


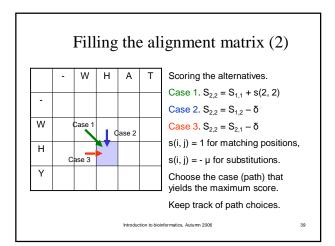
- How to find the optimal alignment?
- We use previous solutions for optimal alignments of smaller subsequences

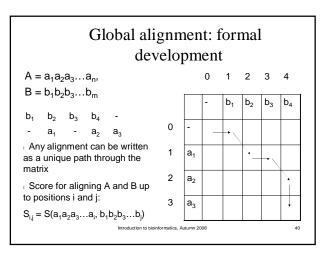
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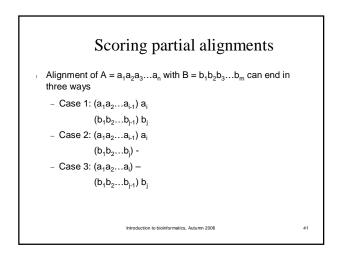
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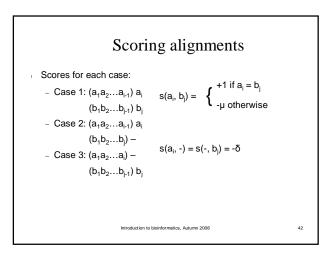
This general approach is known as dynamic programming

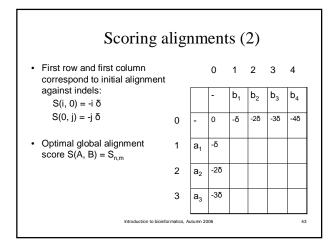


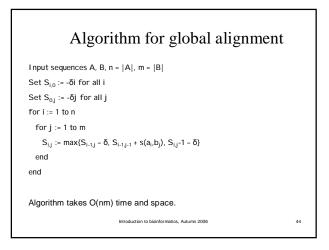


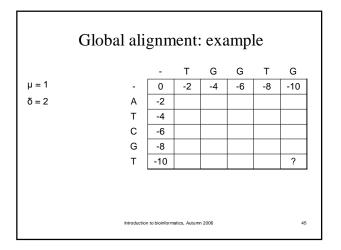


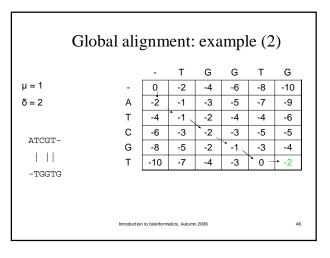


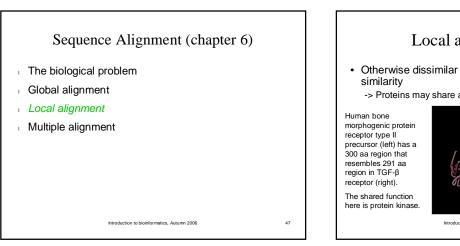


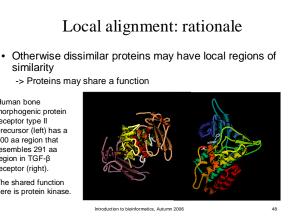


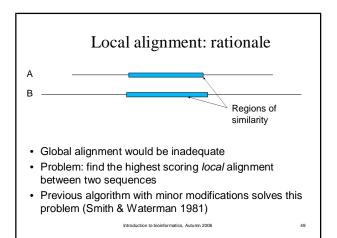


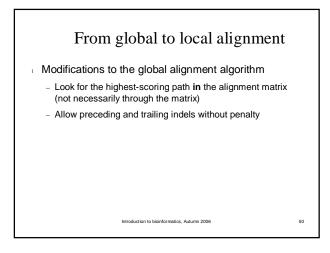


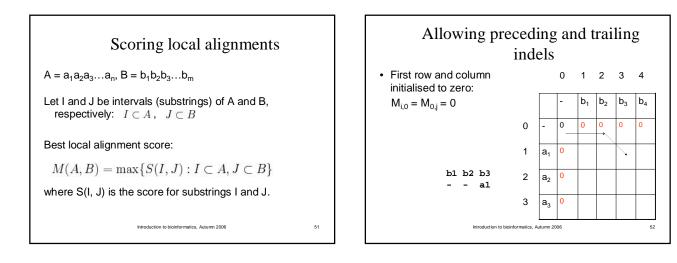


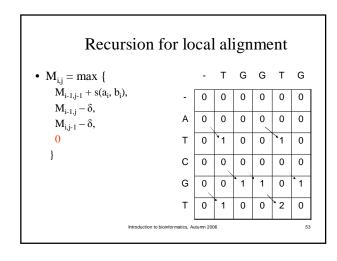


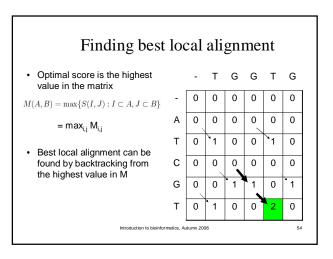


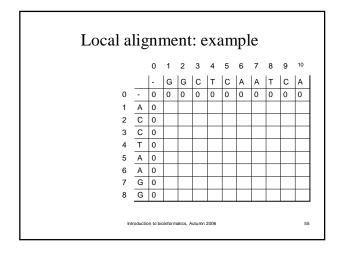


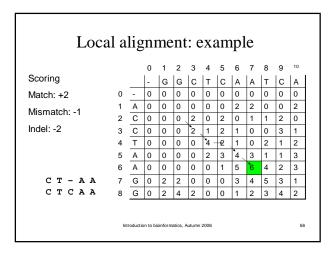


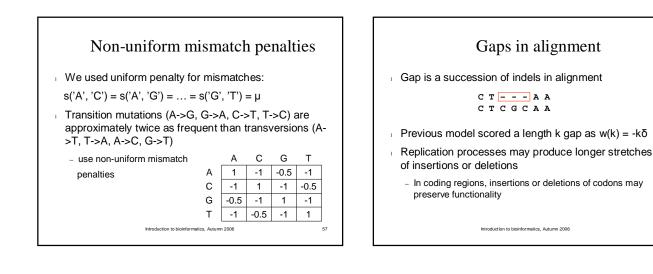


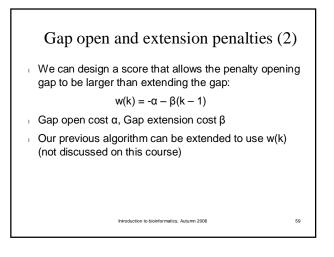


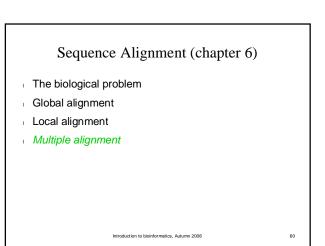












#### Multiple alignment

- Consider a set of n sequences on the right
  - Orthologous sequences from
  - different organisms
  - Paralogs from multiple duplications
- How can we study relationships between these sequences?

aggcgagctgcgagtgcta cgttagattgacgctgac ttccggctgcgac gacacggcgaacgga agtgtgcccgacgagcgaggag gcgggctgtgagcgcta aagcggcctgtgtgcccta atgctgctgccagtgta agtcgagccccgagtgc agtccgagtcc actcggtgc

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## Optimal alignment of three sequences

- Alignment of A =  $a_1a_2...a_i$  and B =  $b_1b_2...b_j$  can end either in (-,  $b_j$ ), ( $a_i$ ,  $b_j$ ) or ( $a_i$ , -)
- $2^2 1 = 3$  alternatives
- Alignment of A, B and C =  $c_1c_2...c_k$  can end in  $2^3 1$ ways:  $(a_i, -, -), (-, b_j, -), (-, -, c_k), (-, b_j, c_k), (a_i, -, c_k), (a_i, b_j, -)$  or  $(a_i, b_j, c_k)$
- Solve the recursion using three-dimensional dynamic programming matrix: O(n<sup>3</sup>) time and space
- Generalizes to n sequences but impractical with moderate number of sequences

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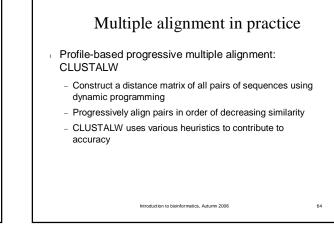
#### Multiple alignment in practice

 In practice, real-world multiple alignment problems are usually solved with heuristics

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- Progressive multiple alignment
  - Choose two sequences and align them
  - Choose third sequence w.r.t. two previous sequences and align the third against them
  - Repeat until all sequences have been aligned
  - Different options how to choose sequences and score alignments

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#### Additional material

- R. Durbin, S. Eddy, A. Krogh, G. Mitchison: Biological sequence analysis
- Course Biological sequence analysis in Spring 2007

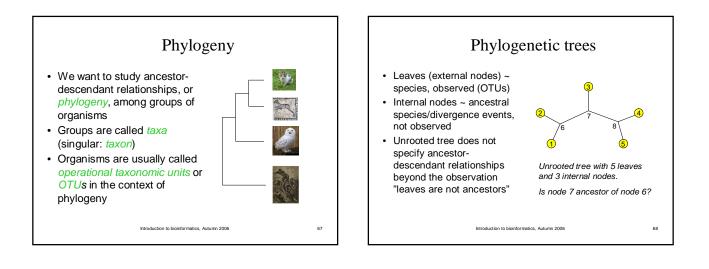
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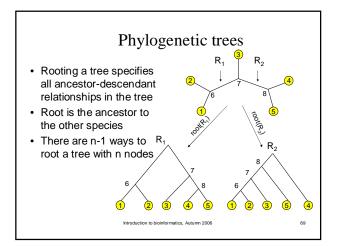
#### Inferring the Past: Phylogenetic Trees (chapter 12)

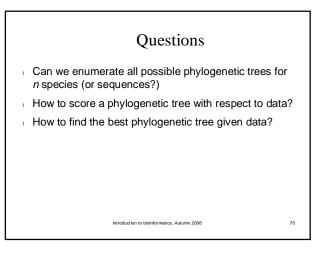
- The biological problem
- Parsimony and distance methods
- Models for mutations and estimation of distances

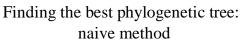
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Maximum likelihood methods







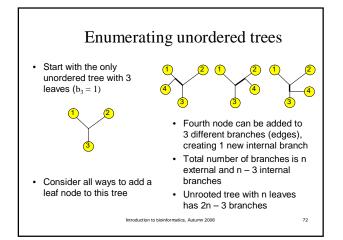


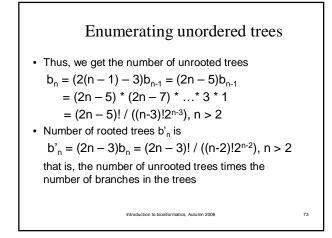
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- How can we find the phylogenetic tree that best represents the data?
- Naive method: enumerate all possible trees
- How many different trees are there of *n* species?

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Denote this number by b<sub>n</sub>





#### Number of possible rooted and unrooted trees

n	Bn	b'n
3	1	3
4	3	15
5	15	105
6	105	945
7	954	10395
8	10395	135135
9	135135	2027025
10	2027025	34459425
20	2.22E+020	8.20E+021
30	8.69E+036	4.95E+038

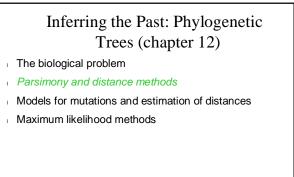
Too many trees? We can't construct and evaluate every phylogenetic tree even for a smallish number of species

- Better alternative is to
  - Devise a way to evaluate an individual tree against the data
  - Guide the search using the evaluation criteria to reduce the search space

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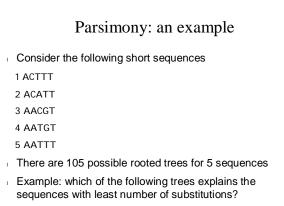


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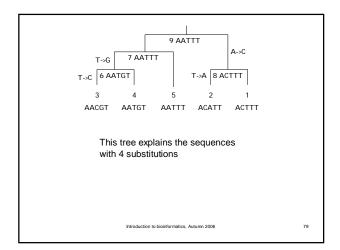
#### Parsimony method

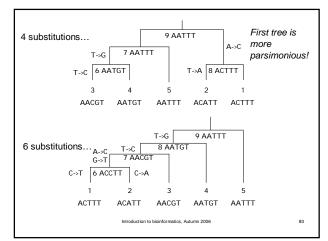
- The parsimony method finds the tree that explains the observed sequences with a minimal number of substitutions
- Method has two steps
  - Compute smallest number of substitutions for a given tree with a *parsimony algorithm*
  - Search for the tree with the minimal number of substitutions

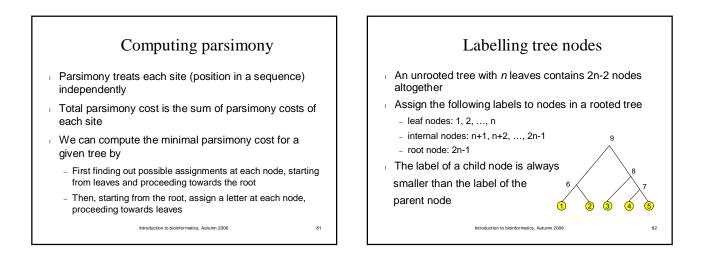
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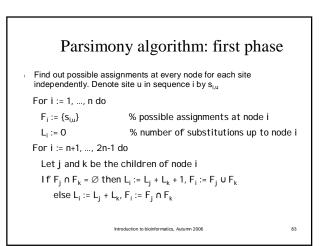


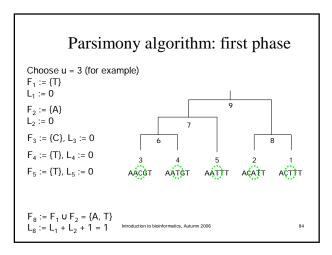
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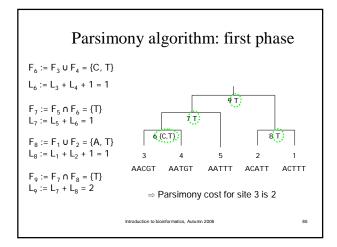


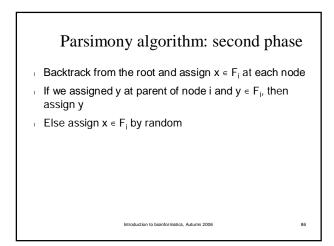


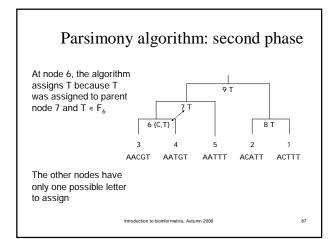


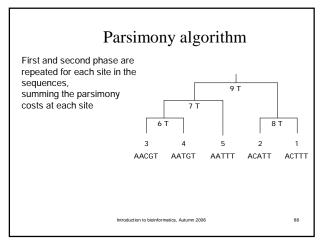


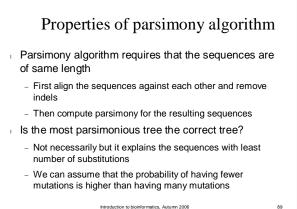




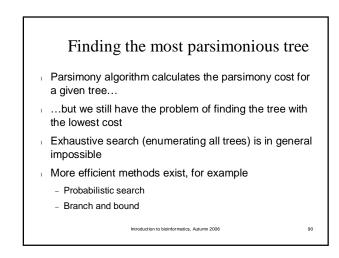


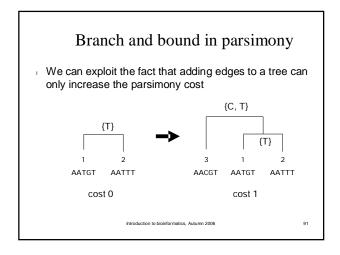


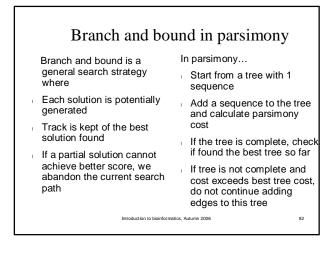


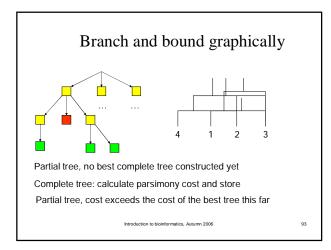


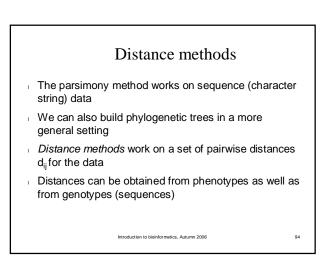
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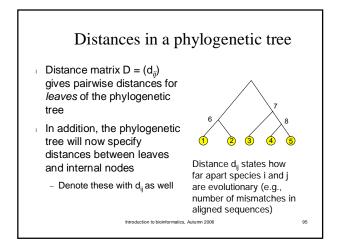


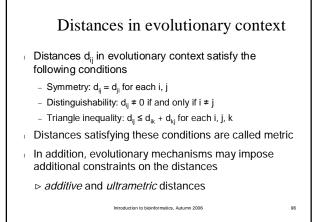


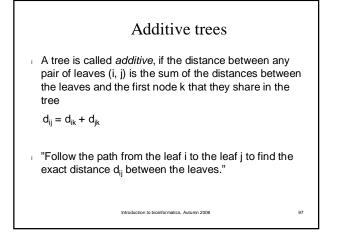


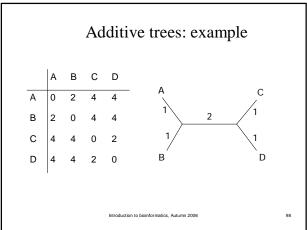


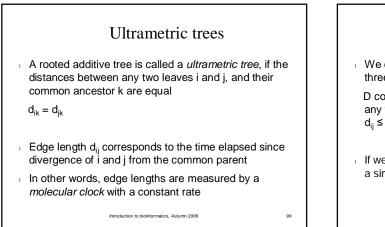


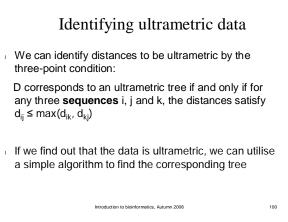


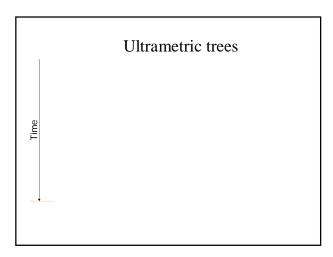


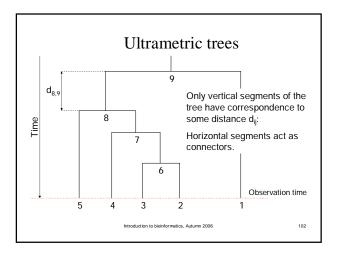


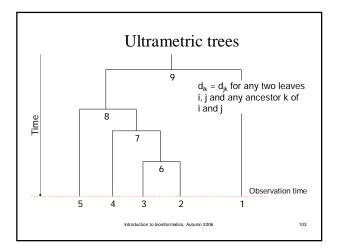


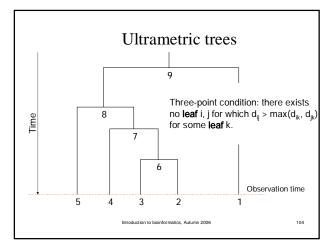


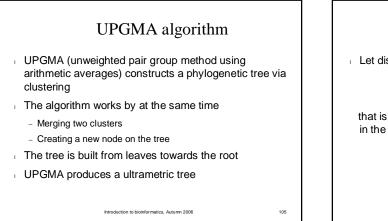


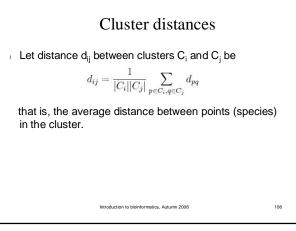










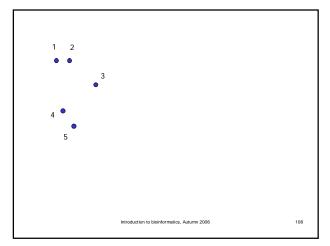


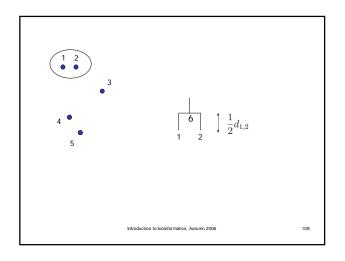
## UPGMA algorithm

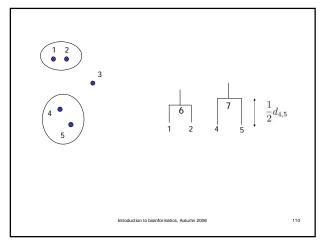
I nitialisation

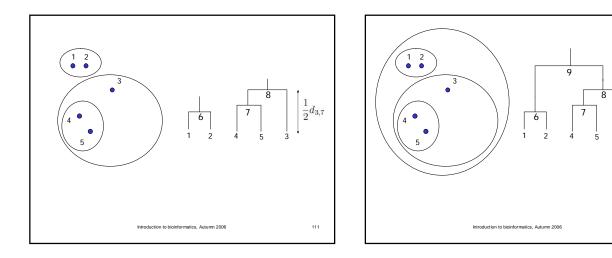
- Assign each point i to its own cluster  ${\rm C}_{\rm i}$
- Define one leaf for each sequence, and place it at height zero
  - Find clusters i and j for which d<sub>ij</sub> is minimal
  - Define new cluster k by  $C_k = C_i \cup C_j$ , and define  $d_{kl}$  for all l
  - Define a node k with children i and j. Place k at height  $d_{ij}/2$
  - Remove clusters i and j
- Termination:
  - When only two clusters i and j remain, place root at height  $d_{ij}/2$

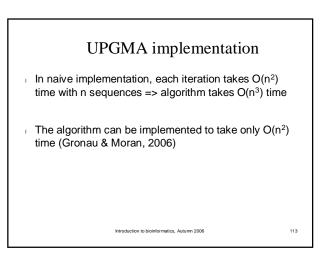
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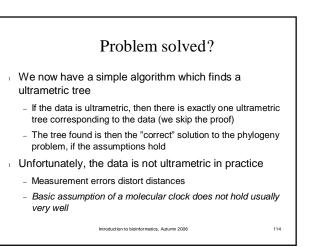




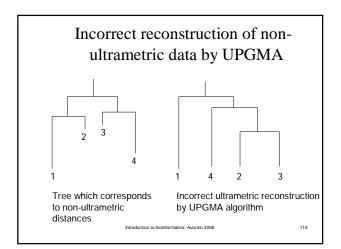


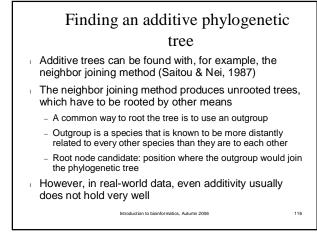


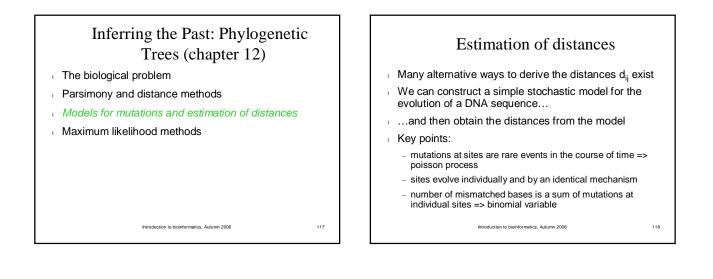




 $\frac{1}{2}d_{6,8}$ 



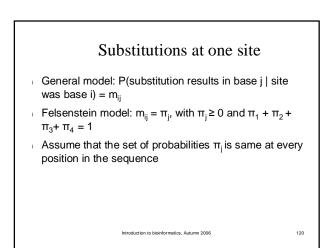


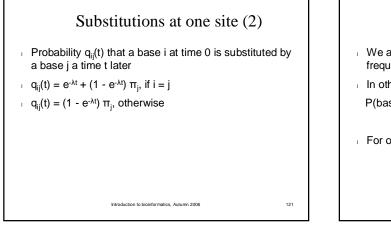


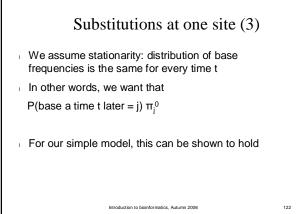
# A stochastic model for base substitutions

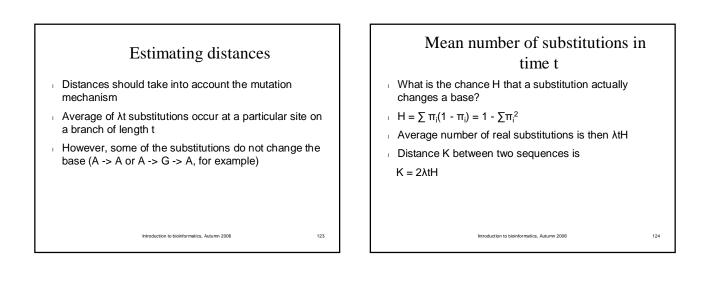
- Consider a single homologous site in two sequences
- Assume the sites diverged for time length t: the sites are separated by time 2t
- Suppose that the number of substitutions in any branch of length t has a Poisson distribution with mean  $\lambda t$
- Probability that k substitutions occur is given by the Poisson probability  $e^{-\lambda t}(\lambda t)^{k/(k!)}$ , k = 0, 1, 2, ...

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# Estimating distances from sequence data

- We want to estimate  $K = 2\lambda tH$  from sequence data
- The chance  $\mathsf{F}_{ij}(t)$  that we observe a base i in one sequence and a base j in another is

 $F_{ij}(t) = \sum_{l} \pi_{l} q_{li}(t) q_{lj}(t)$ 

by averaging over the possible ancestral nucleotides

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Estimating distances from sequence data

Expression  $F_{ij}(t) = \sum_i \pi_i q_{ii}(t) q_{ij}(t)$  can be simplified by assuming that the mutation process is reversible:

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 $\pi_i m_{ij} = \pi_j m_{ji}$  for all  $i \neq j$ 

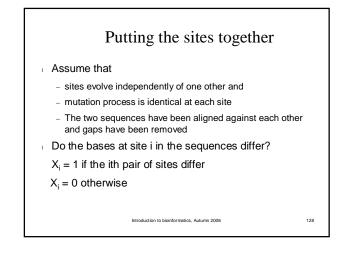
- From this it can be shown that  $\pi_i q_{ij}(t) = \pi_i q_{ji}(t)$  for all i, j and t > 0
- Now the model simplifies into  $F_{ii}(t) = \pi_i q_{ii}(2t)$

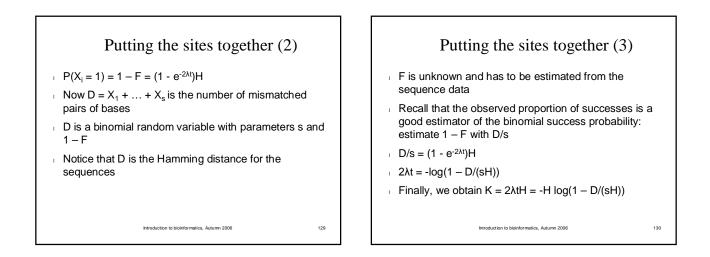
## Estimating distances from sequence dataWhat is the probabilitity F = F(t) that the letters at a

particular position in two immediate descendants from the same node are identical?

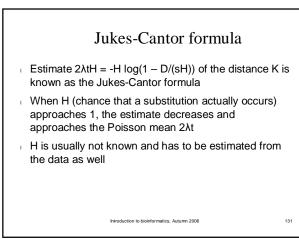
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 $\mathsf{F} = \sum_{i} \pi_{i} q_{ii}(2t) = e^{-2\lambda t} + (1 - e^{-2\lambda t})(1 - H)$ 





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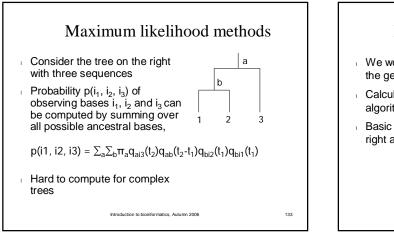


#### Inferring the Past: Phylogenetic Trees (chapter 12)

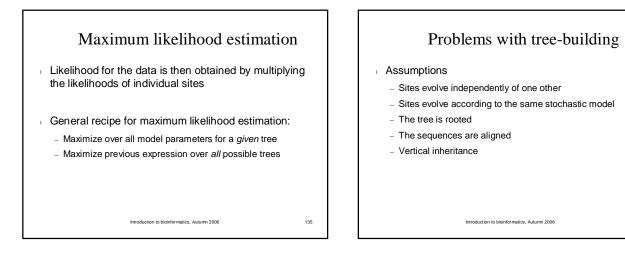
- The biological problem
- Parsimony and distance methods
- Models for mutations and estimation of distances

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Maximum likelihood methods



# Maximum likelihood estimation We would like to calculate likelihood p(i<sub>1</sub>, i<sub>2</sub>, ..., i<sub>n</sub>) in the general case Calculations can be arranged using the peeling algorithm Basic idea is to move all summation signs as far to the right as possible



# Additional material on phylogenetic trees

- Durbin, Eddy, Krogh, Mitchison: Biological sequence analysis
- Jones, Pevzner: An introduction to bioinformatics algorithms
- Gusfield: Algorithms on strings, trees, and sequences

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