Introduction to bioinformatics, Autumn 2007, Exercise 2

15.9.2007

- 1. (Chapter 2, Exercise 4) Suppose N has a binomial distribution with n=10 and p=0.3.
 - (a) Using the formula (2.17), calculate P(N=0), P(N=2), E(N) and VarN.
 - (b) Using R and Computational Example 2.2., simulate observations from N. Use the simulated values to estimate the probabilities you calculated in (a), and compare with the results in (a).
 - (c) Now use R to simulate observations from N when n=1000 and p=0.25. What is your estimate of $P(N \ge 280)$? (See (2.20).)
- 2. (Chapter 2, Exercise 5) Verify the terms in the first row of the transition matrix *P* presented in Section 2.6.3. Describe how you would use the sequence of *M. genitalium* to produce this matrix.

- 3. (Chapter 2, Exercise 6) Find the stationary distribution of the chain with transition matrix P in Section 2.6.3; that is, solve the equations $\pi = \pi P$ subject to the elements of π begin positive and summing to 1. Compare π to the base composition of M.genitalium, and comment.
- 4. (Chapter 2, Exercise 12 (a) (c)) In this exercise we have two random variables X and Y which are not independent. Their joint probability distribution is given in the following table:

		Y			
		1	3	6	9
	2	0.11	0.05	0.20	0.08
X	3	0.20	0.02	0.00	0.10
	7	0.11 0.20 0.00	0.05	0.10	0.09

The values of X are written in the first column and the values of Y in the first row. The table is read as P(X = 7&Y = 6) = 0.10, and so on.

- (a) Find the marginal distribution of X and Y. (That is, $P(X=2), P(X=3), \ldots$)
- (b) Write Z = XY. Find the probability distribution of Z.
- (c) The covariance between any two random variables is defined by

$$Cov(X,Y) = \mathbb{E}(X - \mathbb{E}X)(Y - \mathbb{E}Y).$$

Show that $Cov(X, Y) = \mathbb{E}(XY) - \mathbb{E}X \times \mathbb{E}Y$.

- 5. (Chapter 2, Exercise 12 (d) (f))
 - (a) Find $\mathbb{E}X, \mathbb{E}Y, \sigma_X^2 = VarX, \sigma_Y^2 = VarY$, and Cov(X,Y) for the example in the table.
 - (b) The **correlation coefficient** ρ is defined by $\rho_{X,Y} = Cov(X,Y)/\sigma_X\sigma_Y$. It can be shown that $-1 \leq \rho \leq 1$, the values ± 1 arising when Y is a linear function of X. Verify this last statement.
 - (c) Calculate ρ for the example in the table.