

## What do we learn?

- Central results by Shannon and their consequences
  - $\checkmark$  the source coding theorem

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- ✓ the noisy channel coding theorem
- "The legend of Minimum Description Length (MDL) Principle"

# What is Information theory?

Claude Shannon, "A mathematical Theory of Communication" Bell Syst. Tech. Journal, 27: 379-423,623-656, 1948.



## Simply put

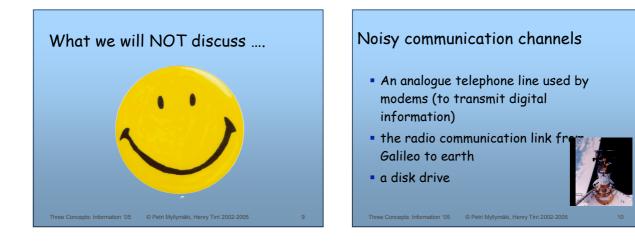
- The problem of representing the source alphabet symbols s in terms of another system of symbols (0,1)
  - Channel encoding: how to represent the source symbols so that their representations are far apart in some suitable sense ("error-correction")
  - Source encoding: How to represent the source symbols in a minimal form for purposes of efficiency ("compression")

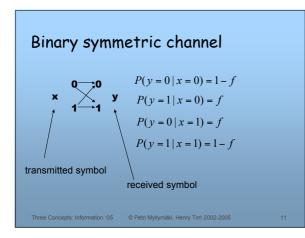
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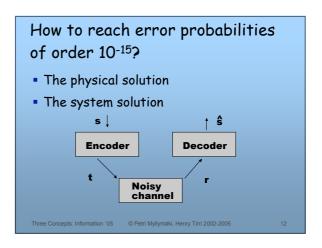
#### The course focus

- we will address source encoding as it has deep relationship to modeling
- (by the end of the course) abstract from actual codes to code lengths
- discuss information-theoretic principles that can be used as a foundation of statistical modeling

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#### "To be more precise"

- Information theory answers questions about the theoretical limitations of such systems
- Coding theory discusses how to build practical encoding and decoding systems

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Encoding		Decoding							
s	t	r (	000 0	001 0	10 10	00 10	1 11	0 011	111
0	000	ŝ	0	0	0	0 1	1	1	1
1	111			-	-				
_									
	S	0	0	1	0	1	1	0	
	t	000	000	111	000	111	111	000	
	n	000	001	000	000	101	000	000	
	r	000	001	111	000	010	111	000	

### Think!

• What is the error probability for the previous repetition code for a binary symmetric channel with noise level f?



#### Some analysis

- For f = 0.1 the error probability  $p_b = 0.03$
- What did we loose?
  ✓ information transmission rate reduced by factor of three!
- Good?
  - ✓ assume we want a probability of error close to 10<sup>-15</sup>. What would be the rate of the repetition code? (~1/60)

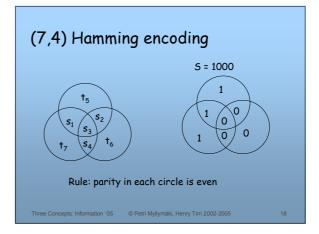
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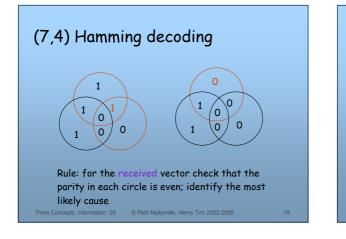
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- Goal: (very) small probability of error and a good transmission rate
- Idea: add redundancy to blocks instead of encoding one bit at a time (the origin of "parity")
- Solution: (N,K) block code adds (N-K) redundant bits to the end of the sequence of K source bits

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## Performance of the best codes

We want

 $\checkmark$ small error probability p<sub>b</sub>

✓large (transmission) rate R

- What points in the (p<sub>b</sub>,R)-plane are achievable?
- A good guess: boundary passes through the origin (0,0)

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