# MATLAB ${ }^{\circledR}$ / R Reference <br> November 24, 2009 

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I wrote the first version of this reference during the Spring 2007 semester, as I learned R while teaching my course "MAT400, Modeling \& Simulation" at the University of Maine. The course covers population and epidemiological modeling, including deterministic and stochastic models in discrete and continuous time, along with spatial models. Half of the class meetings are in a regular classroom, and half are in a computer lab where students work through modeling \& simulation exercises. When I taught earlier versions of the course, it was based on Matlab only. In Spring 2007, some biology graduate students in the class who had learned $R$ in statistics courses asked if they could use $R$ in my class as well, and I said yes. My colleague Bill Halteman was a great help as I frantically learned R to stay ahead of the class. As I went, every time I learned how to do something in R for the course, I added it to this reference, so that I wouldn't forget it later. Some items took a huge amount of time searching for a simple way to do what I wanted, but at the end of the semester, I was pleasantly surprised that almost everything I do in Matlab had an equivalent in R. I was also inspired to do this after seeing the "R for Octave Users" reference written by Robin Hankin. I've continued to add to the document, with many additions based on topics that came up while teaching courses on Advanced Linear Algebra and Numerical Analysis.

This reference is organized into general categories. There is also a Matlab index and an R index at the end, which should make it easy to look up a command you know in one of the languages and learn how to do it in the other (or if you're trying to read code in whichever language is unfamiliar to you, allow you to translate back to the one you are more familiar with). The index entries refer to the item numbers in the first column of the reference document, rather than page numbers.

Any corrections, suggested improvements, or even just notification that the reference has been useful will be appreciated. I hope all the time I spent on this will prove useful for others in addition to myself and my students. Note that sometimes I don't necessarily do things in what you may consider the "best" way in a particular language; I often tried to do things in a similar way in both languages. But if you believe you have a "better" way (either simpler, or more computationally efficient) to do something, feel free to let me know.

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## 1 Help

| No. | Description | MATLAB | R |
| :---: | :--- | :--- | :--- |
| 1 | Show help for a function (e.g. <br> sqrt $)$ | help sqrt, or helpwin sqrt to see <br> it in a separate window | help(sqrt) or ?sqrt |
| 2 | Show help for a built-in key- <br> word (e.g. for) | help for | help('for') or ?'for'' |
| 3 | General list of many help top- <br> ics | help | library() to see available libraries, <br> or library (help='base') for very <br> long list of stuff in base package which <br> you can see help for |
| 4 | Explore main documentation <br> in browser | doc or helpbrowser (previously it <br> was helpdesk, which is now being <br> phased out) | help.start() |
| 5 | Search documentation for <br> keyword or partial keyword <br> (e.g. functions which refer to <br> "binomial") | lookfor binomial | help.search('binomial') |

## 2 Entering/building/indexing matrices

| No. | Description | Matlab | R |
| :---: | :---: | :---: | :---: |
| 6 | $\begin{aligned} & \text { Enter a row vector } \vec{v}= \\ & {\left[\begin{array}{llll} 1 & 2 & 3 & 4 \end{array}\right]} \end{aligned}$ | $\mathrm{v}=\left[\begin{array}{llll}1 & 2 & 3 & 4\end{array}\right]$ | $\mathrm{v}=\mathrm{c}(1,2,3,4) \quad$ or alternatively $\mathrm{v}=\mathrm{scan}()$ then enter "1 234 " and press Enter twice (the blank line terminates input) |
| 7 | Enter a column vector $\left[\begin{array}{l}1 \\ 2 \\ 3 \\ 4\end{array}\right]$ | [1; 2; 3; 4] | $c(1,2,3,4)$ <br> ( R does not distinguish between row and column vectors.) |
| 8 | Enter a matrix $\left[\begin{array}{lll}1 & 2 & 3 \\ 4 & 5 & 6\end{array}\right]$ | [123; 456 | To enter values by row: matrix(c(1, 2, 3,4,5,6), nrow=2, byrow=TRUE) To enter values by column: matrix(c(1,4,2,5,3,6), nrow=2) |
| 9 | Access an element of vector $\mathbf{v}$ | v(3) | v [3] |
| 10 | Access an element of matrix A | A $(2,3)$ | A $[2,3]$ |
| 11 | Access an element of matrix A using a single index: indices count down the first column, then down the second column, etc. | A(5) | A [5] |
| 12 | Build the vector [2 34567 ] | 2:7 | 2:7 |
| 13 | Build the vector [76543 2] | 7:-1:2 | 7:2 |
| 14 | Build the vector [2 $\left.5 \begin{array}{l}5 \\ 8\end{array} 1114\right]$ | 2:3:14 | seq( $2,14,3$ ) |


| No. | Description | Matlab | R |
| :---: | :---: | :---: | :---: |
| 15 | Build a vector containing $n$ equally-spaced values between $a$ and $b$ inclusive | linspace (a,b,n) | seq(a,b,length.out=n) or just seq(a,b,len=n) |
| 16 | Build a vector containing $n$ logarithmically equallyspaced values between $10^{a}$ and $10^{b}$ inclusive | logspace (a,b,n) | 10^seq(a,b,len=n) |
| 17 | Build a vector of length $k$ containing all zeros | zeros ( $k, 1$ ) (for a column vector) or zeros ( $1, \mathrm{k}$ ) (for a row vector) | rep(0,k) |
| 18 | Build a vector of length $k$ containing the value $j$ in all positions | $j *$ ones $(k, 1)$ (for a column vector) or $\mathrm{j} *$ ones $(1, \mathrm{k})$ (for a row vector) | $\mathrm{rep}(\mathrm{j}, \mathrm{k})$ |
| 19 | Build an $m \times n$ matrix of zeros | zeros(m, n) | $\begin{aligned} & \text { matrix }(0, \text { nrow=m,ncol=n }) \text { or just } \\ & \text { matrix }(0, m, n) \end{aligned}$ |
| 20 | Build an $m \times n$ matrix containing $j$ in all positions | j*ones (m, n ) | $\operatorname{matrix}(\mathrm{j}, \mathrm{nrow}=\mathrm{m}, \mathrm{ncol}=\mathrm{n}) \quad$ or just $\operatorname{matrix}(\mathrm{j}, \mathrm{m}, \mathrm{n})$ |
| 21 | $n \times n$ identity matrix $I_{n}$ | eye(n) | diag(n) |
| 22 | Build diagonal matrix $A$ using elements of vector $\mathbf{v}$ as diagonal entries | diag(v) | diag(v,nrow=length(v)) (Note: if you are sure the length of vector $\mathbf{v}$ is 2 or more, you can simply say diag(v).) |
| 23 | Extract diagonal elements of matrix $A$ | $\mathrm{v}=\mathrm{diag}(\mathrm{A})$ | $\mathrm{v}=\mathrm{diag}(\mathrm{A})$ |
| 24 | "Glue" two matrices a1 and a2 (with the same number of rows) side-by-side | [a1 a2] | cbind(a1, a2) |
| 25 | "Stack" two matrices a1 and a2 (with the same number of columns) on top of each other | [a1; a2] | rbind(a1, a2) |
| 26 | Reverse the order of elements in vector $\mathbf{v}$ | v(end:-1:1) | rev(v) |
| 27 | Column 2 of matrix A | A(: , 2) | $\mathrm{A}[, 2]$ Note: that gives the result as a vector. To make the result a $m \times 1$ matrix instead, do A[,2, drop=FALSE] |
| 28 | Row 7 of matrix $\mathbf{A}$ | A $(7,:)$ | $\mathrm{A}[7$,$] Note: that gives the result as a$ vector. To make the result a $1 \times n$ matrix instead, do A [7, , drop=FALSE] |
| 29 | All elements of A as a vector, column-by-column | A (:) (gives a column vector) | c (A) |
| 30 | Rows 2-4, columns 6-10 of A (this is a $3 \times 5$ matrix) | A ( $2: 4,6: 10$ ) | A [2:4,6:10] |
| 31 | A $3 \times 2$ matrix consisting of rows 7,7 , and 6 and columns 2 and 1 of $A$ (in that order) | A([77 7], [2 1]) | $\mathrm{A}[\mathrm{c}(7,7,6), \mathrm{c}(2,1)]$ |


| No. | Description | Matlab | R |
| :---: | :---: | :---: | :---: |
| 32 | Given a single index ind into an $m \times n$ matrix $\mathbf{A}$, compute the row $\mathbf{r}$ and column $\mathbf{c}$ of that position (also works if ind is a vector) | $[\mathrm{r}, \mathrm{c}]=\mathrm{ind} 2 \mathrm{sub}(\operatorname{size}(\mathrm{A}), \mathrm{ind})$ | $\begin{aligned} & r=((\text { ind }-1) \% \% m)+1 \\ & c=\text { floor }((\text { ind }-1) / m)+1 \end{aligned}$ |
| 33 | Given the row $\mathbf{r}$ and column c of an element of an $m \times n$ matrix $\mathbf{A}$, compute the single index ind which can be used to access that element of $\mathbf{A}$ (also works if $\mathbf{r}$ and $\mathbf{c}$ are vectors) | ind $=$ sub2ind (size(A), r, c) | ind $=(\mathrm{c}-1) * \mathrm{~m}+\mathrm{r}$ |
| 34 | Given equal-sized vectors $\mathbf{r}$ and $\mathbf{c}$ (each of length $k$ ), set elements in rows (given by r) and columns (given by c) of matrix $\mathbf{A}$ equal to 12 . That is, $k$ elements of $A$ will be modified. | ```inds = sub2ind(size(A),r,c); A(inds) = 12;``` | $\begin{aligned} & \text { inds }=\operatorname{cbind}(r, c) \\ & \text { A [inds] }=12 \end{aligned}$ |
| 35 | Truncate vector $\mathbf{v}$, keeping only the first 10 elements | $\mathrm{v}=\mathrm{v}(1: 10)$ | $\mathrm{v}=\mathrm{v}[1: 10], \text { or length }(\mathrm{v})=10$ also works |
| 36 | Extract elements of vector $\mathbf{v}$ from position a to the end | v (a: end) | v[a:length(v)] |
| 37 | All but the $k^{\text {th }}$ element of vector $\mathbf{v}$ | $\mathrm{v}([1:(\mathrm{k}-1)(\mathrm{k}+1) \mathrm{end}])$ | v [-k] |
| 38 | All but the $j^{\text {th }}$ and $k^{\text {th }}$ elements of vector $\mathbf{v}$ | No simple way? Generalize the previous item | $\mathrm{v}[\mathrm{c}(-\mathrm{j},-\mathrm{k})]$ |
| 39 | Reshape matrix $A$, making it an $m \times n$ matrix with elements taken columnwise from the original $A$ (which must have $m n$ elements) | $\mathrm{A}=\mathrm{reshape}(\mathrm{A}, \mathrm{m}, \mathrm{n})$ | $\operatorname{dim}(\mathrm{A})=\mathrm{c}(\mathrm{m}, \mathrm{n})$ |
| 40 | Extract the lower-triangular portion of matrix $A$ | $\mathrm{L}=\operatorname{tril}(\mathrm{A})$ | $\mathrm{L}=\mathrm{A}$; L $\mathrm{upper} . \operatorname{tri}(\mathrm{L})]=0$ |
| 41 | Extract the upper-triangular portion of matrix $A$ | $\mathrm{U}=\operatorname{triu}(\mathrm{A})$ | $\mathrm{U}=\mathrm{A}$; U[lower.tri(U)]=0 |
| 42 | Enter $n \times n$ Hilbert matrix $H$ where $H_{i j}=1 /(i+j-1)$ | hilb (n) | Hilbert(n), but this is part of the Matrix package which you'll need to install (see item 316 for how to install/load packages). |
| 43 | Enter an $n$-dimensional array, e.g. a $3 \times 4 \times 2$ array with the values 1 through 24 | reshape $(1: 24,3,4,2)$ reshape $(1: 24,[342])$ | array (1:24, c $(3,4,2)$ ) (Note that a matrix is 2 -D, i.e. rows and columns, while an array is more generally $N-\mathrm{D}$ ) |

### 2.1 Cell arrays and lists

| No. | Description | Matlab | R |
| :---: | :---: | :---: | :---: |
| 44 | Build a vector $\mathbf{v}$ of length $\mathbf{n}$, capable of containing different data types in different elements (called a cell array in Matlab, and a list in R) | $\mathrm{v}=\operatorname{cell}(1, \mathrm{n}) \quad$ In general, cell(m,n) makes an $m \times n$ cell array. Then you can do e.g.: $\begin{aligned} & \mathrm{v}\{1\}=12 \\ & \mathrm{v}\{2\}=\text { 'hi there } \\ & \mathrm{v}\{3\}=\operatorname{rand}(3) \end{aligned}$ | $\begin{aligned} & \mathrm{v}=\text { vector('list', } \mathrm{n}) \text { Then you } \\ & \text { can do e.g.: } \\ & \mathrm{v}[[1]]=12 \\ & \mathrm{v}[[2]]=\text { 'hi there' } \\ & \mathrm{v}[[3]]=\text { matrix(runif }(9), 3) \end{aligned}$ |
| 45 | Extract the $i^{\text {th }}$ element of a cell/list vector $\mathbf{v}$ | $\mathrm{w}=\mathrm{v}\{\mathrm{i}\}$ <br> If you use regular indexing, i.e. w $=\mathrm{v}(\mathrm{i})$, then $\mathbf{w}$ will be a $1 \times 1$ cell matrix containing the contents of the $i^{\text {th }}$ element of $\mathbf{v}$. | $\mathrm{w}=\mathrm{v}[[\mathrm{i}]]$ <br> If you use regular indexing, i.e. $\mathrm{w}=$ v [i], then $\mathbf{w}$ will be a list of length 1 containing the contents of the $i^{\text {th }}$ element of $\mathbf{v}$. |
| 46 | Set the name of the $i^{\text {th }}$ element in a list. | (Matlab does not have names associated with elements of cell arrays.) | names(v) [3] = 'myrandmatrix' <br> Use names (v) to see all names, and names (v) v NULL to clear all names. |

### 2.2 Structs and data frames

| No. | Description | Matlab | R |
| :---: | :---: | :---: | :---: |
| 47 | Create a matrix-like object with different named columns (a struct in Matlab, or a data frame in R) | ```avals=2*ones(1,6); yvals=6:-1:1; v=[1 5 3 2 3 7]; d=struct('a',avals, 'yy', yyvals, 'fac', v);``` | $\begin{aligned} & \mathrm{v}=\mathrm{c}(1,5,3,2,3,7) ; \mathrm{d}=\text { data.frame } \\ & \text { cbind }(\mathrm{a}=2, \mathrm{yy}=6: 1), \mathrm{v}) \end{aligned}$ |

Note that I (surprisingly) don't use R for statistics, and therefore have very little experience with data frames (and also very little with Matlab structs). I will try to add more to this section later on.

## 3 Computations

### 3.1 Basic computations

| No. | Description | Matlab | R |
| :---: | :---: | :---: | :---: |
| 48 | $a+b, a-b, a b, a / b$ | a+b, a-b, a*b, a/b | a+b, a-b, a*b, a/b |
| 49 | $\sqrt{a}$ | sqrt (a) | sqrt (a) |
| 50 | $a^{b}$ | a^b | a^b |
| 51 | $\|a\|$ (note: for complex arguments, this computes the modulus) | abs (a) | abs (a) |
| 52 | $e^{a}$ | $\exp (\mathrm{a})$ | $\exp (\mathrm{a})$ |
| 53 | $\ln (a)$ | $\log (\mathrm{a})$ | $\log (\mathrm{a})$ |
| 54 | $\log _{2}(a), \log _{10}(a)$ | $\log 2(a), \log 10(a)$ | $\log 2(a), \log 10(a)$ |
| 55 | $\sin (a), \cos (a), \tan (a)$ | $\sin (\mathrm{a}), \cos (\mathrm{a}), \tan (\mathrm{a})$ | $\sin (\mathrm{a}), \cos (\mathrm{a}), \tan (\mathrm{a})$ |
| 56 | $\sin ^{-1}(a), \cos ^{-1}(a), \tan ^{-1}(a)$ | $\operatorname{asin}(\mathrm{a}), \operatorname{acos}(\mathrm{a}), \operatorname{atan}(\mathrm{a})$ | $\operatorname{asin}(\mathrm{a}), \operatorname{acos}(\mathrm{a}), \operatorname{atan}(\mathrm{a})$ |
| 57 | $\sinh (a), \cosh (a), \tanh (a)$ | $\sinh (\mathrm{a}), \cosh (\mathrm{a}), \tanh (\mathrm{a})$ | $\sinh (\mathrm{a}), \cosh (\mathrm{a}), \tanh (\mathrm{a})$ |
| 58 | $\begin{array}{ll} \sinh ^{-1}(a), & \cosh ^{-1}(a), \\ \tanh ^{-1}(a) \end{array}$ | $\operatorname{asinh}(\mathrm{a}), \operatorname{acosh}(\mathrm{a}), \operatorname{atanh}(\mathrm{a})$ | $\operatorname{asinh}(\mathrm{a}), \operatorname{acosh}(\mathrm{a}), \operatorname{atanh}(\mathrm{a})$ |


| No. | Description | Matlab | R |
| :---: | :---: | :---: | :---: |
| 59 | $n$ MOD $k$ (modulo arithmetic) | $\bmod (\mathrm{n}, \mathrm{k})$ | n \%\% k |
| 60 | Round to nearest integer | round (x) | round (x) (Note: R uses IEC 60559 standard, rounding 5 to the even digit so e.g. round (0.5) gives 0 , not 1.) |
| 61 | Round down to next lowest integer | floor (x) | floor (x) |
| 62 | Round up to next largest integer | ceil (x) | ceiling (x) |
| 63 | Sign of $x(+1,0$, or -1$)$ | $\operatorname{sign}(x)$ (Note: for complex values, this computes $\mathrm{x} / \mathrm{abs}(\mathrm{x})$.) | $\operatorname{sign}(x)$ (Does not work with complex values) |
| 64 | $\begin{aligned} & \text { Error function } \operatorname{erf}(x)= \\ & (2 / \sqrt{\pi}) \int_{0}^{x} e^{-t^{2}} d t \end{aligned}$ | erf (x) | $2 * \operatorname{pnorm}(\mathrm{x} *$ sqrt (2) ) -1 |
| 65 | Complementary ror function $\quad$ er- $(2 / \sqrt{\pi}) \int_{x}^{\infty} e^{-t^{2}} d t=1-\operatorname{erf}(x)$ | erfc (x) | 2*pnorm(x*sqrt (2), lower=FALSE) |
| 66 | Inverse error function | $\operatorname{erfinv}(\mathrm{x})$ | qnorm( $(1+\mathrm{x}) / 2) / \mathrm{sqrt}(2)$ |
| 67 | Inverse complementary error function | $\operatorname{erfcinv}(\mathrm{x})$ | qnorm (x/2, lower=FALSE)/sqrt (2) |
| 68 | $\begin{aligned} & \text { Binomial } \left.\quad \begin{array}{c} \text { coefficien } \\ n \\ k \end{array}\right)=n!/(n!(n-k)!) \end{aligned}$ | nchoosek (n, k) | choose ( $\mathrm{n}, \mathrm{k}$ ) |

Note: the various functions above (logarithm, exponential, trig, abs, and rounding functions) all work with vectors and matrices, applying the function to each element, as well as with scalars.

### 3.2 Complex numbers

| No. | Description | MatLAB | R |
| :---: | :--- | :--- | :--- |
| 69 | Enter a complex number | $1+2 \mathrm{i}$ | $1+2 \mathrm{i}$ |
| 70 | Modulus (magnitude) | $\operatorname{abs}(\mathbf{z})$ | $\operatorname{abs}(\mathbf{z})$ or Mod $(\mathbf{z})$ |
| 71 | Argument (angle) | $\operatorname{angle}(\mathbf{z})$ | $\operatorname{Arg}(z)$ |
| 72 | Complex conjugate | $\operatorname{conj}(\mathbf{z})$ | $\operatorname{Conj}(z)$ |
| 73 | Real part of $z$ | $\operatorname{real}(\mathbf{z})$ | $\operatorname{Re}(z)$ |
| 74 | Imaginary part of $z$ | $\operatorname{imag}(z)$ | $\operatorname{Im}(z)$ |

### 3.3 Matrix/vector computations

| No. | Description | Matlab | R |  |
| :---: | :---: | :---: | :---: | :---: |
| 75 | Matrix multiplication $A B$ | A * B | A \% *\% B |  |
| 76 | Element-by-element multiplication of $A$ and $B$ | A .* B | A * B |  |
| 77 | Transpose of a matrix, $A^{T}$ | A' (This is actually the complex conjugate (i.e. Hermitian) transpose; use A.' for the non-conjugate transpose if you like; they are equivalent for real matrices.) | $t(A)$ for transpose, or $\operatorname{Conj}(t(A))$ for conjugate (Hermitian) transpose |  |
| 78 | Solve $A \vec{x}=\vec{b}$ | $\mathrm{A} \backslash \mathrm{b}$ Warning: if there is no solution, Matlab gives you a least-squares "best fit." If there are many solutions, Matlab just gives you one of them. | solve(A, b) Warning: this only works with square invertible matrices. |  |
| 79 | Reduced echelon form of $A$ | rref (A) | R does not have a function to do this |  |
| 80 | Compute inverse of $\mathbf{A}$ | $\operatorname{inv}(\mathrm{A})$ | solve(A) |  |
| 81 | Compute $A B^{-1}$ | A/B | A \%*\% solve(B) |  |
| 82 | Element-by-element division of $A$ and $B$ | A ./ B | A / B |  |
| 83 | Compute $A^{-1} B$ | A $\$ B & solve(A, B)  \hline 84 & Square the matrix $A$ | $\mathrm{A}^{\wedge} 2$ | A \% \%\% A |
| 85 | Raise matrix $A$ to the $k^{\text {th }}$ power | $\mathrm{A}^{\wedge} \mathrm{k}$ | (No easy way to do this in $R$ other than repeated multiplication A \% $\%$ \% A \% $\%$ \% A...) |  |
| 86 | Raise each element of $A$ to the $k^{\text {th }}$ power | A. ${ }^{\text {k }}$ | $\mathrm{A}^{\wedge} \mathrm{k}$ |  |
| 87 | Rank of matrix $A$ | rank(A) | qr (A)\$rank |  |
| 88 | Set $\mathbf{w}$ to be a vector of eigenvalues of $\mathbf{A}$, and $\mathbf{V}$ a matrix containing the corresponding eigenvectors | [V, D] =eig(A) and then w=diag(D) since Matlab returns the eigenvalues on the diagonal of $\mathbf{D}$ | $\begin{aligned} & \text { tmp=eigen(A); w=tmp\$values; } \\ & \text { V=tmp\$vectors } \end{aligned}$ |  |
| 89 | Permuted $L U$ factorization of a matrix | $[\mathrm{L}, \mathrm{U}, \mathrm{P}]=\mathrm{lu}(\mathrm{A})$ then the matrices satisfy $P A=L U$. Note that this works even with non-square matrices | tmp=expand(lu(Matrix(A))); $\mathrm{L}=\mathrm{tmp} \$ \mathrm{~L} ; \mathrm{U}=\mathrm{tmp} \$ \mathrm{U}$; $\mathrm{P}=\mathrm{tmp} \$ \mathrm{P}$ then the matrices satisfy $A=P L U$, i.e. $P^{-1} A=L U$. Note that the $\mathbf{l u}$ and expand functions are part of the Matrix package (see item 316 for how to install/load packages). Also note that this doesn't seem to work correctly with non-square matrices. $\mathbf{L}, \mathbf{U}$, and $\mathbf{P}$ will be of class Matrix rather than class matrix; to make them the latter, instead do L=as.matrix(tmp\$L), $\mathrm{U}=\mathrm{as}$. matrix (tmp\$U), and P=as.matrix(tmp\$P) above. |  |


| No. | Description | Matlab | R |
| :---: | :---: | :---: | :---: |
| 90 | Singular-value decomposition: given $m \times n$ matrix $A$ with rank $r$, find $m \times r$ matrix $P$ with orthonormal columns, diagonal $r \times r$ matrix $S$, and $r \times n$ matrix $Q^{T}$ with orthonormal rows so that $P S Q^{T}=A$ | [P, S, Q] $=\operatorname{svd}(\mathrm{A}$, 'econ') | ```tmp=svd(A); U=tmp$u; V=tmp$v; S=diag(tmp$d)``` |
| 91 | Schur decomposition of square matrix, $A=Q T Q^{H}=Q T Q^{-1}$ where $Q$ is unitary (i.e. $Q^{H} Q=I$ ) and $T$ is upper triangular; $Q^{H}=\overline{Q^{T}}$ is the Hermitian (conjugate) transpose | [Q,T] = schur (A) | tmp=Schur(Matrix(A)); T=tmp@T; $Q=$ tmp@Q Note that Schur is part of the Matrix package (see item 316 for how to install/load packages). $\mathbf{T}$ and Q will be of class Matrix rather than class matrix; to make them the latter, instead do $\mathrm{T}=\mathrm{as}$. matrix (tmp@T) and $\mathrm{Q}=$ as.matrix (tmp@Q) above. |
| 92 | Cholesky factorization of a square, symmetric, positive definite matrix $A=R^{T} R$, where $R$ is upper-triangular | $\mathrm{R}=\operatorname{chol}(\mathrm{A})$ | $R=\operatorname{chol}(A)$ Note that chol is part of the Matrix package (see item 316 for how to install/load packages). |
| 93 | $Q R$ factorization of matrix $A$, where $Q$ is orthogonal (satisfying $Q Q^{T}=I$ ) and $R$ is upper-triangular | $[\mathrm{Q}, \mathrm{R}]=\mathrm{qr}(\mathrm{A})$ satisfying $Q R=A$, or $[\mathrm{Q}, \mathrm{R}, \mathrm{E}]=\mathrm{qr}(\mathrm{A})$ to do permuted $Q R$ factorization satisfying $A E=Q R$ | $\mathrm{z}=\mathrm{qr}(\mathrm{A})$; $\mathrm{Q}=\mathrm{qr} . \mathrm{Q}(\mathrm{z})$; R=qr.R(z); $\mathrm{E}=\operatorname{diag}(\mathrm{n})[, \mathrm{z}$ \$pivot] (where $\mathbf{n}$ is the number of columns in $A$ ) gives permuted $Q R$ factorization satisfying $A E=Q R$ |
| 94 | Vector norms | norm(v,1) for 1-norm $\\|\vec{v}\\|_{1}$, norm $(\mathrm{v}, 2)$ for Euclidean norm $\\|\vec{v}\\|_{2}, \operatorname{norm}(\mathrm{v}$, inf $)$ for infinity-norm $\\|\vec{v}\\|_{\infty}$, and norm(v, p) for $p$-norm $\\|\vec{v}\\|_{p}=\left(\sum\left\|v_{i}\right\|^{p}\right)^{1 / p}$ | R does not have a norm function for vectors; only one for matrices. But the following will work: norm(matrix(v),'1') for 1-norm $\\|\vec{v}\\|_{1}$, norm(matrix(v), 'i') for infinity-norm $\\|\vec{v}\\|_{\infty}$, and sum(abs(v) $\left.{ }^{\wedge}\right)^{\wedge}(1 / p)$ for $p$-norm $\\|\vec{v}\\|_{p}=\left(\sum\left\|v_{i}\right\|^{p}\right)^{1 / p}$ |
| 95 | Matrix norms | $\operatorname{norm}(\mathrm{A}, 1)$ for $\quad$-norm $\\|A\\|_{1}$, norm(A) for $\quad 2$-norm $\quad\\|A\\|_{2}$, $\operatorname{norm}(\mathrm{A}$, inf $) \quad$ for infinity-norm $\\|A\\|_{\infty}, \quad$ and $\quad \operatorname{norm}(\mathrm{A}$, 'fro') for Frobenius norm $\left(\sum_{i}\left(A^{T} A\right)_{i i}\right)^{1 / 2}$ | $\operatorname{norm}\left(\mathrm{A},{ }^{\prime} 1^{\prime}\right)$ for 1 -norm $\\|A\\|_{1}$, $\max (\operatorname{svd}(\mathrm{A}) \$ \mathrm{~d})$ for 2 -norm $\\|A\\|_{2}$, norm $\left(\mathrm{A}, \mathrm{I}^{\prime} \mathrm{i}^{\prime}\right)$ for infinity-norm $\\|A\\|_{\infty}$, and norm $\left(\mathrm{A}, \mathrm{I}^{\prime} \mathrm{f}\right)$ for Frobenius norm $\left(\sum_{i}\left(A^{T} A\right)_{i i}\right)^{1 / 2}$ |
| 96 | Condition number $\operatorname{cond}(A)=$ $\\|A\\|_{1}\left\\|A^{-1}\right\\|_{1}$ of $A$, using 1norm | cond (A,1) (Note: Matlab also has a function rcond (A) which computes reciprocal condition estimator using the 1-norm) | 1/rcond(A, '1') |
| 97 | Condition number cond $(A)=$ $\\|A\\|_{2}\left\\|A^{-1}\right\\|_{2}$ of $A$, using 2norm | cond (A, 2) | kappa(A, exact=TRUE) (leave out the "exact=TRUE" for an estimate) |
| 98 | Condition number cond $(A)=$ $\\|A\\|_{\infty}\left\\|A^{-1}\right\\|_{\infty}$ of $A$, using infinity-norm | cond(A,inf) | 1/rcond(A, 'I') |


| No. | Description | Matlab | R |
| :---: | :---: | :---: | :---: |
| 99 | Compute mean of all elements in vector or matrix | mean(v) for vectors, mean(A(:)) for matrices | mean(v) or mean(A) |
| 100 | Compute means of columns of a matrix | mean (A) | colMeans (A) |
| 101 | Compute means of rows of a matrix | mean (A, 2) | rowMeans (A) |
| 102 | Compute standard deviation of all elements in vector or matrix | std(v) for vectors, $\operatorname{std}(A(:))$ for matrices. This normalizes by $n-1$. Use std (v,1) to normalize by $n$. | $\operatorname{sd}(v)$ for vectors, $\operatorname{sd}(c(A))$ for matrices. This normalizes by $n-1$. |
| 103 | Compute standard deviations of columns of a matrix | $\operatorname{std}(A)$. This normalizes by $n-1$. Use std (A,1) to normalize by $n$ | sd (A). This normalizes by $n-1$. |
| 104 | Compute standard deviations of rows of a matrix | $\operatorname{std}(A, 0,2)$ to normalize by $n-1$, $\operatorname{std}(A, 1,2)$ to normalize by $n$ | $\begin{aligned} & \text { apply (A,1,sd). This normalizes by } \\ & n-1 \text {. } \end{aligned}$ |
| 105 | Compute variance of all elements in vector or matrix | $\operatorname{var}(\mathrm{v})$ for vectors, $\operatorname{var}(\mathrm{A}(:))$ for matrices. This normalizes by $n-1$. Use $\operatorname{var}(\mathrm{v}, 1)$ to normalize by $n$. | $\operatorname{var}(v)$ for vectors, $\operatorname{var}(c(A))$ for matrices. This normalizes by $n-1$. |
| 106 | Compute variance of columns of a matrix | $\operatorname{var}(\mathrm{A})$. This normalizes by $n-1$. Use $\operatorname{var}(A, 1)$ to normalize by $n$ | apply (A,2,var). This normalizes by $n-1$. |
| 107 | Compute variance of rows of a matrix | $\begin{aligned} & \operatorname{var}(\mathrm{A}, 0,2) \text { to normalize by } n-1, \\ & \operatorname{var}(\mathrm{~A}, 1,2) \text { to normalize by } n \end{aligned}$ | apply (A, 1, var). This normalizes by $n-1$. |
| 108 | Compute covariance for two vectors of observations | $\operatorname{cov}(\mathrm{v}, \mathrm{w})$ computes the $2 \times 2$ covariance matrix; the off-diagonal elements give the desired covariance | $\operatorname{cov}(\mathrm{v}, \mathrm{w})$ |
| 109 | Compute covariance matrix, giving covariances between columns of matrix $A$ | $\operatorname{cov}(\mathrm{A})$ | $\operatorname{var}(\mathrm{A})$ or $\operatorname{cov}(\mathrm{A})$ |
| 110 | Given matrices $A$ and $B$, build covariance matrix $C$ where $c_{i j}$ is the covariance between column $i$ of $A$ and column $j$ of $B$ | I don't know of a direct way to do this in Matlab. But one way is $[Y, X]=$ meshgrid $(\operatorname{std}(B), \operatorname{std}(A))$; X.*Y.*corr (A,B) | $\operatorname{cov}(\mathrm{A}, \mathrm{B})$ |
| 111 | Compute Pearson's linear correlation coefficient between elements of vectors $\mathbf{v}$ and $\mathbf{w}$ | corr (v,w) Note: $\mathbf{v}$ and $\mathbf{w}$ must be column vectors. To make it work regardless of whether they are row or column vectors, do $\operatorname{corr}(\mathrm{v}(:), \mathrm{w}(:))$ | $\operatorname{cor}(\mathrm{v}, \mathrm{w})$ |
| 112 | Compute Kendall's tau correlation statistic for vectors $\mathbf{v}$ and w | corr(v,w, 'type', 'kendall') | cor(v,w,method='kendall') |
| 113 | $\begin{array}{lrr} \hline \text { Compute } & \text { Spearman's } & \text { rho } \\ \text { correlation } & \text { statistic } & \text { for } \\ \text { vectors } \mathbf{v} \text { and } \mathbf{w} & \\ \hline \end{array}$ | corr(v,w, 'type', 'spearman') | cor(v,w,method='spearman') |
| 114 | Compute pairwise Pearson's correlation coefficient between columns of matrix A | corr (A) The 'type' argument may also be used as in the previous two items | cor (A) The method argument may also be used as in the previous two items |
| 115 | Compute matrix $C$ of pairwise Pearson's correlation coefficients between each pair of columns of matrices $A$ and $B$, i.e. so $c_{i j}$ is the correlation between column $i$ of $A$ and column $j$ of $B$ | corr (A,B) The 'type' argument may also be used as just above | $\operatorname{cor}(A, B)$ The method argument may also be used as just above |


| No. | Description | Matlab | R |
| :---: | :---: | :---: | :---: |
| 116 | Compute sum of all elements in vector or matrix | sum(v) for vectors, sum(A(:)) for matrices | sum(v) or sum(A) |
| 117 | Compute sums of columns of matrix | sum (A) | colSums (A) |
| 118 | Compute sums of rows of matrix | $\operatorname{sum}(\mathrm{A}, 2)$ | rowSums (A) |
| 119 | Compute matrix exponential $e^{A}=\sum_{k=0}^{\infty} A^{k} / k!$ | $\operatorname{expm}(\mathrm{A})$ | expm(Matrix(A)), but this is part of the Matrix package which you'll need to install (see item 316 for how to install/load packages). |
| 120 | Compute cumulative sum of values in vector | cumsum (v) | cumsum (v) |
| 121 | Compute cumulative sums of columns of matrix | cumsum (A) | apply (A, 2, cumsum) |
| 122 | Compute cumulative sums of rows of matrix | cumsum (A,2) | t(apply (A,1, cumsum)) |
| 123 | Compute cumulative sum of all elements of matrix (column-by-column) | cumsum(A(:)) | cumsum (A) |
| 124 | Cumulative product of elements in vector $\mathbf{v}$ | cumprod(v) (Can also be used in the various ways cumsum can) | cumprod(v) (Can also be used in the various ways cumsum can) |
| 125 | Cumulative minimum or maximum of elements in vector $\mathbf{v}$ | I don't know of an easy way to do this in Matlab | cummin(v) or cummax (v) |
| 126 | Compute differences between consecutive elements of vector $\mathbf{v}$. Result is a vector w 1 element shorter than $\mathbf{v}$, where element $i$ of $\mathbf{w}$ is element $i+1$ of $\mathbf{v}$ minus element $i$ of $\mathbf{v}$ | diff(v) | diff (v) |
| 127 | Make a vector $\mathbf{y}$ the same size as vector $\mathbf{x}$, which equals 4 everywhere that $\mathbf{x}$ is greater than 5 , and equals 3 everywhere else (done via a vectorized computation). | $z=[34] ; y=z((x>5)+1)$ | $\mathrm{y}=$ ifelse(x > 5, 4, 3) |
| 128 | Compute minimum of values in vector $\mathbf{v}$ | $\min (\mathrm{v})$ | $\min (\mathrm{v})$ |
| 129 | Compute minimum of all values in matrix $\mathbf{A}$ | $\min (\mathrm{A}(:))$ | $\min (\mathrm{A})$ |
| 130 | Compute minimum value of each column of matrix $\mathbf{A}$ | $\min (\mathrm{A})($ returns a row vector) | apply (A, $2, \mathrm{~min}$ ) (returns a vector) |
| 131 | Compute minimum value of each row of matrix $\mathbf{A}$ | $\min (A,[], 2)$ (returns a column vector) | apply (A,1,min) (returns a vector) |


| No. | Description | MATLAB | R |
| :--- | :--- | :--- | :--- |
| 132 | Given matrices A and B, <br> compute a matrix where each <br> element is the minimum of <br> the corresponding elements of <br> A and B | $\min (\mathrm{A}, \mathrm{B})$ | $\mathrm{pmin}(\mathrm{A}, \mathrm{B})$ |
| 133 | Given matrix A and scalar <br> $\mathbf{c}$, compute a matrix where <br> each element is the minimum <br> of $\mathbf{c}$ and the corresponding el- <br> ement of A | $\min (\mathrm{A}, \mathrm{c})$ | $\mathrm{pmin}(\mathrm{A}, \mathrm{c})$ |
| 134 | Find minimum among all val- <br> ues in matrices A and B | $\min ([\mathrm{A}(:) \quad ; \mathrm{B}(:)])$ | $\min (\mathrm{A}, \mathrm{B})$ |
| 135 | Find index of the first time <br> min(v) appears in v, and <br> store that index in ind | $[\mathrm{y}$, ind $=\min (\mathrm{v})$ | ind = which.min(v) |

Notes:

- Matlab and R both have a max function (and R has pmax and which.max as well) which behaves in the same ways as min but to compute maxima rather than minima.
- Functions like exp, sin, sqrt etc. will operate on arrays in both Matlab and R, doing the computations for each element of the matrix.

| No. | Description | Matlab | R |
| :---: | :---: | :---: | :---: |
| 136 | Number of rows in $A$ | size (A, 1) | nrow (A) |
| 137 | Number of columns in $A$ | size(A,2) | $\mathrm{ncol}(\mathrm{A})$ |
| 138 | Dimensions of $A$, listed in a vector | size(A) | $\operatorname{dim}(\mathrm{A})$ |
| 139 | Number of elements in vector v | length (v) | length (v) |
| 140 | Total number of elements in matrix $A$ | numel (A) | length(A) |
| 141 | Max. dimension of $A$ | length (A) | $\max (\operatorname{dim}(\mathrm{A})$ ) |
| 142 | Sort values in vector $\mathbf{v}$ | sort(v) | sort(v) |
| 143 | Sort values in $\mathbf{v}$, putting sorted values in $\mathbf{s}$, and indices in $\mathbf{i d x}$, in the sense that $\mathbf{s}[k]$ $=\mathrm{x}[\mathrm{idx}[\mathrm{k}]]$ | [s,idx] $=$ sort (v) | ```tmp=sort(v,index.return=TRUE); s=tmp$x; idx=tmp$ix``` |
| 144 | Sort the order of the rows of matrix $\mathbf{m}$ | sortrows (m) <br> This sorts according to the first column, then uses column 2 to break ties, then column 3 for remaining ties, etc. Complex numbers are sorted by $\mathbf{a b s}(\mathbf{x})$, and ties are then broken by angle(x). | m[order (m[,1]),] <br> This only sorts according to the first column. To use column 2 to break ties, and then column 3 to break further ties, do $m[\operatorname{order}(m[, 1], m[, 2], m[, 3])$, Complex numbers are sorted first by real part, then by imaginary part. |
| 145 | Sort order of rows of matrix $\mathbf{m}$, specifying to use columns c1, c2, c3 as the sorting "keys" | sortrows(m, [c1 c2 c2]) | $\begin{aligned} & \mathrm{m}[\text { order }(\mathrm{m}[, \mathrm{c} 1], \mathrm{m}[, \mathrm{c} 2], \\ & \mathrm{m}[, \mathrm{c} 3]),] \end{aligned}$ |


| No. | Description | Matlab | R |
| :---: | :---: | :---: | :---: |
| 146 | Same as previous item, but sort in decreasing order for columns c1 and c2 | sortrows(m, [-c1 -c2 c2]) | $\begin{aligned} & m[\text { order }(-m[, c 1],-m[, c 2], \\ & m[, c 3]),] \end{aligned}$ |
| 147 | Sort order of rows of matrix $\mathbf{m}$, and keep indices used for sorting | [y,i] = sortrows(m) | i=order (m[1,]) ; y=m[i,] |
| 148 | To count how many values in the vector $\mathbf{v}$ are between 4 and 7 (inclusive on the upper end) | sum( (v > 4) \& (v <= 7) ) | sum( $(v>4) \&(v<=~ 7))$ |
| 149 | Given vector $\mathbf{v}$, return list of indices of elements of $\mathbf{v}$ which are greater than 5 | find(v > 5) | which(v > 5) |
| 150 | Given matrix $\mathbf{A}$, return list of indices of elements of $\mathbf{A}$ which are greater than 5 , using single-indexing | find (A > 5) | which(A > 5) |
| 151 | Given matrix $\mathbf{A}$, generate vectors $\mathbf{r}$ and $\mathbf{c}$ giving rows and columns of elements of $\mathbf{A}$ which are greater than 5 | [r, c] $=$ find $(\mathrm{A}>5 \mathrm{~s})$ | $\begin{aligned} & \mathrm{w}=\text { which (A > 5, arr.ind=TRUE) ; } \\ & \mathrm{r}=\mathrm{w}[, 1] ; \mathrm{c}=\mathrm{w}[, 2] \end{aligned}$ |
| 152 | Given vector $\mathbf{x}$ (of presumably discrete values), build a vector $\mathbf{v}$ listing unique values in $\mathbf{x}$, and corresponding vector $\mathbf{c}$ indicating how many times those values appear in x | $\mathrm{v}=$ unique(x) ; $\mathrm{c}=$ hist (x, v$)$; | $\begin{aligned} & \mathrm{w}=\operatorname{table}(\mathrm{x}) ; \mathrm{c}=\mathrm{as} . \text { numeric }(\mathrm{w}) ; \\ & \mathrm{v}=\mathrm{as} . \operatorname{numeric}(\text { names }(\mathrm{w})) \end{aligned}$ |
| 153 | Given vector $\mathbf{x}$ (of presumably continuous values), divide the range of values into $k$ equally-sized bins, and build a vector $\mathbf{m}$ containing the midpoints of the bins and a corresponding vector $\mathbf{c}$ containing the counts of values in the bins | [c, m] = hist( $\mathrm{x}, \mathrm{k}$ ) | ```w=hist(x,seq(min(x),max(x), length.out=k+1), plot=FALSE); m=w$mids; c=w$counts``` |
| 154 | Convolution / polynomial multiplication (given vectors $\mathbf{x}$ and $\mathbf{y}$ containing polynomial coefficients, their convolution is a vector containing coefficients of the product of the two polynomials) | conv ( $\mathrm{x}, \mathrm{y}$ ) | convolve( $x, r e v(y)$,type='open') Note: the accuracy of this is not as good as Matlab; e.g. doing $\mathrm{v}=\mathrm{c}(1,-1)$; for (i in $2: 20$ ) $\mathrm{v}=\mathrm{convolve}$ (v, c (-i, 1) , type='open') to generate the $20^{\text {th }}$-degree Wilkinson polynomial $W(x)=\prod_{i=1}^{20}(x-i)$ gives a coefficient of $\approx-780.19$ for $x^{19}$, rather than the correct value -210 . |

### 3.4 Root-finding

| No. | Description | Matlab | R |
| :---: | :---: | :---: | :---: |
| 155 | Find roots of polynomial whose coefficients are stored in vector $\mathbf{v}$ (coefficients in $\mathbf{v}$ are highest-order first) | roots(v) | polyroot(rev(v)) (This function really wants the vector to have the constant coefficient first in $\mathbf{v}$; rev reverses their order to achieve this.) |
| 156 | Find zero (root) of a function $f(x)$ of one variable | Define function $\mathbf{f}(\mathbf{x})$, then do fzero( $f, x 0$ ) to search for a root near $\mathbf{x 0}$, or fzero (f, $[\mathrm{a} b]$ ) to find a root between $a$ and $b$, assuming the sign of $f(x)$ differs at $x=a$ and $x=b$. Default forward error tolerance (i.e. error in $x$ ) is machine epsilon $\epsilon_{\text {mach }}$. | Define function $\mathbf{f}(\mathbf{x})$, then do uniroot (f, $c(a, b))$ to find a root between $a$ and $b$, assuming the sign of $f(x)$ differs at $x=a$ and $x=b$. Default forward error tolerance (i.e. error in $x$ ) is fourth root of machine epsilon, $\left(\epsilon_{\text {mach }}\right)^{0.25}$. To specify e.g. a tolerance of $2^{-52}$, do uniroot ( $f$, $c(a, b)$, tol=2^-52). |

### 3.5 Function optimization/minimization

| No. | Description | Matlab | R |
| :---: | :---: | :---: | :---: |
| 157 | Find value $m$ which minimizes a function $f(x)$ of one variable within the interval from $a$ to $b$ | Define function $\mathbf{f}(\mathbf{x})$, then do $m=\text { fminbnd }(f, a, b)$ | Define function $\mathbf{f}(\mathbf{x})$, then do $m=\operatorname{optimize}(f, c(a, b))$ \$minimum |
| 158 | Find value $m$ which minimizes a function $f\left(x, p_{1}, p_{2}\right)$ with given extra parameters (but minimization is only occuring over the first argument), in the interval from $a$ to $b$. | Define function $\mathbf{f}(\mathbf{x}, \mathbf{p} \mathbf{1}, \mathbf{p 2})$, then use an "anonymous function": <br> \% first define values for p 1 <br> $\%$ and p2, and then do: <br> $m=f m i n b n d(@(x) f(x, p 1, p 2), a, b)$ | $\begin{aligned} & \text { Define function } \mathbf{f}(\mathrm{x}, \mathrm{p} 1, \mathrm{p} 2) \text {, then: } \\ & \text { \# first define values for } \mathrm{p} 1 \\ & \text { \# and p2, and then do: } \\ & m=o p t i m i z e(f, c(a, b), p 1=p 1 \text {, } \\ & \text { p2=p2) \$minimum } \end{aligned}$ |
| 159 | Find values of $x, y, z$ which minimize function $f(x, y, z)$, using a starting guess of $x=$ $1, y=2.2$, and $z=3.4$. | First write function $\mathbf{f}(\mathbf{v})$ which accepts a vector argument $\mathbf{v}$ containing values of $x, y$, and $z$, and returns the scalar value $f(x, y, z)$, then do: <br>  | First write function $\mathbf{f}(\mathbf{v})$ which accepts a vector argument $\mathbf{v}$ containing values of $x, y$, and $z$, and returns the scalar value $f(x, y, z)$, then do: <br> optim(c(1,2.2,3.4),f)\$par |
| 160 | Find values of $x, y, z$ which minimize function $f\left(x, y, z, p_{1}, p_{2}\right)$, using a starting guess of $x=1$, $y=2.2$, and $z=3.4$, where the function takes some extra parameters (useful e.g. for doing things like nonlinear least-squares optimization where you pass in some data vectors as extra parameters). | First write function $\mathbf{f}(\mathbf{v}, \mathbf{p} 1, \mathbf{p} 2)$ which accepts a vector argument $\mathbf{v}$ containing values of $x, y$, and $z$, along with the extra parameters, and returns the scalar value $f\left(x, y, z, p_{1}, p_{2}\right)$, then do: <br> fminsearch(@f,[112.2 3.4], ... [ ], p1, p2) <br> Or use an anonymous function: <br> fminsearch(@(x) $f(x, p 1, p 2), \ldots$ [1 2.2 .23 .4$]$ ) | First write function $\mathbf{f}(\mathbf{v}, \mathbf{p} 1, \mathbf{p} 2)$ which accepts a vector argument $\mathbf{v}$ containing values of $x, y$, and $z$, along with the extra parameters, and returns the scalar value $f\left(x, y, z, p_{1}, p_{2}\right)$, then do: <br> optim(c(1,2.2,3.4), f, p1=p1, p2=p2)\$par |

### 3.6 Numerical integration / quadrature

| No. | Description | Matlab | R |
| :---: | :---: | :---: | :---: |
| 161 | Numerically integrate function $f(x)$ over interval from $a$ to $b$ | quad (f,a,b) uses adaptive Simpson's quadrature, with a default absolute tolerance of $10^{-6}$. To specify absolute tolerance, use quad (f,a,b,tol) | integrate(f,a,b) uses adaptive quadrature with default absolute and relative error tolerances being the fourth root of machine epsilon, $\left(\epsilon_{\text {mach }}\right)^{0.25} \approx 1.22 \times 10^{-4}$. Tolerances can be specified by using integrate(f,a,b, rel.tol=tol1, abs.tol=tol2). Note that the function $\mathbf{f}$ must be written to work even when given a vector of $x$ values as its argument. |
| 162 | Simple trapezoidal numerical integration using $(x, y)$ values in vectors $\mathbf{x}$ and $\mathbf{y}$ | $\operatorname{trapz}(\mathrm{x}, \mathrm{y})$ | $\begin{aligned} & \operatorname{sum}(\operatorname{diff}(x) *(y[-l e n g t h(y)]+ \\ & y[-1]) / 2) \end{aligned}$ |

### 3.7 Curve fitting

| No. | Description | Matlab | R |
| :---: | :---: | :---: | :---: |
| 163 | Fit the line $y=c_{1} x+c_{0}$ to data in vectors $\mathbf{x}$ and $\mathbf{y}$. | $\mathrm{p}=$ polyfit( $\mathrm{x}, \mathrm{y}, 1$ ) <br> The return vector $\mathbf{p}$ has the coefficients in descending order, i.e. $\mathbf{p}(\mathbf{1})$ is $c_{1}$, and $\mathbf{p}(2)$ is $c_{0}$. | $p=\operatorname{coef}(\operatorname{lm}(y \sim x))$ <br> The return vector $\mathbf{p}$ has the coefficients in ascending order, i.e. $\mathbf{p}[1]$ is $c_{0}$, and $\mathbf{p}[2]$ is $c_{1}$. |
| 164 | Fit the quadratic polynomial $y=c_{2} x^{2}+c_{1} x+c_{0}$ to data in vectors $\mathbf{x}$ and $\mathbf{y}$. | $\mathrm{p}=\operatorname{polyfit}(\mathrm{x}, \mathrm{y}, 2)$ <br> The return vector $\mathbf{p}$ has the coefficients in descending order, i.e. $\mathbf{p}(\mathbf{1})$ is $c_{2}, \mathbf{p}(2)$ is $c_{1}$, and $\mathbf{p}(3)$ is $c_{0}$. | $\mathrm{p}=\operatorname{coef}\left(\operatorname{lm}\left(\mathrm{y} \sim \mathrm{x}+\mathrm{I}\left(\mathrm{x}^{\wedge} 2\right)\right)\right)$ <br> The return vector $\mathbf{p}$ has the coefficients in ascending order, i.e. $p[1]$ is $c_{0}, \mathbf{p}[2]$ is $c_{1}$, and $\mathbf{p}[3]$ is $c_{2}$. |
| 165 | Fit $n^{\text {th }}$ degree polynomial $y=c_{n} x^{n}+c_{n-1} x^{n-1}+\ldots+$ $c_{1} x+c_{0}$ to data in vectors $\mathbf{x}$ and $\mathbf{y}$. | $\mathrm{p}=\operatorname{polyfit}(\mathrm{x}, \mathrm{y}, \mathrm{n})$ <br> The return vector $\mathbf{p}$ has the coefficients in descending order, $\mathbf{p}(\mathbf{1})$ is $c^{n}, \mathbf{p}(\mathbf{2})$ is $c^{n-1}$, etc. | There isn't a simple function built into the standard R distribution to do this, but see the polyreg function in the mda package (see item 316 for how to install/load packages). |
| 166 | Fit the quadratic polynomial with zero intercept, $y=$ $c_{2} x^{2}+c_{1} x$ to data in vectors $\mathbf{x}$ and $\mathbf{y}$. | (I don't know a simple way do this in Matlab, other than to write a function which computes the sum of squared residuals and use fminsearch on that function. There is likely an easy way to do it in the Statistics Toolbox.) | $\mathrm{p}=\operatorname{coef}\left(\operatorname{lm}\left(\mathrm{y} \sim-1+\mathrm{x}+\mathrm{I}\left(\mathrm{x}^{\wedge} 2\right)\right)\right)$ <br> The return vector $\mathbf{p}$ has the coefficients in ascending order, i.e. $\mathbf{p}[1]$ is $c_{1}$, and $\mathbf{p}[2]$ is $c_{2}$. |
| 167 | Fit natural cubic spline $\left(S^{\prime \prime}(x)=0\right.$ at both endpoints) to points $\left(x_{i}, y_{i}\right)$ whose coordinates are in vectors $\mathbf{x}$ and $\mathbf{y}$; evaluate at points whose $x$ coordinates are in vector $\mathbf{x x}$, storing corresponding $y$ 's in yy | $\mathrm{pp}=$ csape ( $\mathrm{x}, \mathrm{y}$, 'variational') ; <br> $y y=p p v a l(p p, x x)$ but note that csape is in Matlab's Spline Toolbox | ```tmp=spline(x,y,method='natural', xout=xx); yy=tmp$y``` |
| 168 | Fit cubic spline using Forsythe, Malcolm and Moler method (third derivatives at endpoints match third derivatives of exact cubics through the four points at each end) to points $\left(x_{i}, y_{i}\right)$ whose coordinates are in vectors $\mathbf{x}$ and $\mathbf{y}$; evaluate at points whose $x$ coordinates are in vector $\mathbf{x x}$, storing corresponding $y$ 's in yy | I'm not aware of a function to do this in Matlab | $\begin{aligned} & \text { tmp=spline }(x, y, x o u t=x x) ; \\ & y y=\operatorname{tmp} \$ y \end{aligned}$ |


| No. | Description | Matlab | R |
| :---: | :---: | :---: | :---: |
| 169 | Fit cubic spline such that first derivatives at endpoints match first derivatives of exact cubics through the four points at each end) to points $\left(x_{i}, y_{i}\right)$ whose coordinates are in vectors $\mathbf{x}$ and $\mathbf{y}$; evaluate at points whose $x$ coordinates are in vector $\mathbf{x x}$, storing corresponding $y$ 's in yy | pp=csape (x,y); yy=ppval(pp,xx) but csape is in Matlab's Spline Toolbox | I'm not aware of a function to do this in R |
| 170 | Fit cubic spline with periodic boundaries, i.e. so that first and second derivatives match at the left and right ends (the first and last $y$ values of the provided data should also agree), to points $\left(x_{i}, y_{i}\right)$ whose coordinates are in vectors $\mathbf{x}$ and $\mathbf{y}$; evaluate at points whose $x$ coordinates are in vector $\mathbf{x x}$, storing corresponding $y$ 's in yy | pp=csape(x,y,'periodic'); <br> $y y=p p v a l(p p, x x)$ but csape is in Matlab's Spline Toolbox | $\begin{aligned} & \text { tmp=spline }(x, y, m e t h o d= \\ & \text { 'periodic', xout }=x x) ; \text { y }=\text { tmp } \$ y \end{aligned}$ |
| 171 | Fit cubic spline with "not-a-knot" conditions (the first two piecewise cubics coincide, as do the last two), to points $\left(x_{i}, y_{i}\right)$ whose coordinates are in vectors $\mathbf{x}$ and $\mathbf{y}$; evaluate at points whose $x$ coordinates are in vector $\mathbf{x x}$, storing corresponding $y$ 's in yy | $y \mathrm{y}=$ spline $(\mathrm{x}, \mathrm{y}, \mathrm{xx})$ | I'm not aware of a function to do this in $R$ |

## 4 Conditionals, control structure, loops

$\left.\left.\begin{array}{|l|l|l|l|}\hline \text { No. } & \text { Description } & \text { MATLAB } & R \\ \hline 172 & \begin{array}{l}\text { "for" loops over values in a } \\ \text { vector v (the vector v is of- } \\ \text { ten constructed via a:b) }\end{array} & \begin{array}{l}\text { for } i=v \\ \text { command1 } \\ \text { command2 } \\ \text { end }\end{array} & \begin{array}{l}\text { If only one command inside the loop: } \\ \text { for (i in v) } \\ \text { command }\end{array} \\ \text { or }\end{array}\right\} \begin{array}{l}\text { for (i in v) command } \\ \text { If multiple commands inside the loop: } \\ \text { for (i in v) \{ } \\ \text { command1 } \\ \text { command2 }\end{array}\right\}$

| No. | Description | Matlab | R |
| :---: | :---: | :---: | :---: |
| 173 | "if" statements with no else clause | if cond <br> command1 <br> command2 <br> end | If only one command inside the clause: <br> if (cond) <br> command <br> or <br> if (cond) command <br> If multiple commands: <br> if (cond) \{ <br> command1 <br> command2 <br> \} |
| 174 | "if/else" statement | ```if cond command1 command2 else command3 command4 end Note: Matlab also has an "elseif" statement, e.g.: if cond1 command1 elseif cond2 command2 elseif cond3 command3 else command4 end``` | ```If one command in clauses: if (cond) command1 else command2 or if (cond) cmd1 else cmd2 If multiple commands: if (cond) { command1 command2 } else { command3 command4 }``` <br> Warning: the "else" must be on the same line as command1 or the "\}" (when typed interactively at the command prompt), otherwise R thinks the "if" statement was finished and gives an error. <br> R does not have an "elseif" statement. |

Logical comparisons which can be used on scalars in "if" statements, or which operate element-byelement on vectors/matrices:

| MATLAB | R | Description |
| :--- | :--- | :--- |
| $\mathbf{x}<\mathbf{a}$ | $\mathbf{x}<\mathbf{a}$ | True if $x$ is less than $a$ |
| $\mathbf{x}>\mathbf{a}$ | $\mathbf{x}>\mathbf{a}$ | True if $x$ is greater than $a$ |
| $\mathbf{x}<=\mathbf{a}$ | $\mathbf{x}<=\mathbf{a}$ | True if $x$ is less than or equal to $a$ |
| $\mathbf{x}>=\mathbf{a}$ | $\mathbf{x}>=\mathbf{a}$ | True if $x$ is greater than or equal to $a$ |
| $\mathbf{x}==\mathbf{a}$ | $\mathbf{x}==\mathbf{a}$ | True if $x$ is equal to $a$ |
| $\mathbf{x}^{\sim}=\mathbf{a}$ | $\mathbf{x}!=\mathbf{a}$ | True if $x$ is not equal to $a$ |

Scalar logical operators:

| Description | MATLAB | R |
| :--- | :--- | :--- |
| a AND b | $\mathrm{a} \& \& \mathrm{~b}$ | a \&\& b |
| a OR b | $\mathrm{a} \mathrm{\|\mid} \mathrm{~b}$ | $\mathrm{a}\|\mid \mathrm{b}$ |
| a XOR b | $\operatorname{xor}(\mathrm{a}, \mathrm{b})$ | $\operatorname{xor}(\mathrm{a}, \mathrm{b})$ |
| NOT a | $\sim \mathrm{a}$ | $!\mathrm{a}$ |

The \&\& and || operators are short-circuiting, i.e. \&\& stops as soon as any of its terms are FALSE, and \| stops as soon as any of its terms are TRUE.

Matrix logical operators (they operate element-by-element):

| Description | MATLAB | R |
| :--- | :--- | :--- |
| a AND b | $\mathrm{a} \& \mathrm{~b}$ | $\mathrm{a} \& \mathrm{~b}$ |
| a OR b | $\mathrm{a} \mathrm{\mid} \mathrm{~b}$ | $\mathrm{a} \mid \mathrm{b}$ |
| a XOR b | $\operatorname{xor}(\mathrm{a}, \mathrm{b})$ | $\operatorname{xor}(\mathrm{a}, \mathrm{b})$ |
| NOT a | $\sim \mathrm{a}$ | $!\mathrm{a}$ |


| No. | Description | Matlab | R |
| :---: | :---: | :---: | :---: |
| 175 | To test whether a scalar value $\mathbf{x}$ is between 4 and 7 (inclusive on the upper end) | if ( $(x>4) \& \&(x<=7))$ |  |
| 176 | To count how many values in the vector $\mathbf{x}$ are between 4 and 7 (inclusive on the upper end) | $\operatorname{sum}((x>4) \&(x<=7))$ | $\operatorname{sum}((x>4) \&(x<=7))$ |
| 177 | Test whether all values in a logical/boolean vector are TRUE | all (v) | all (v) |
| 178 | Test whether any values in a logical/boolean vector are TRUE | any (v) | any (v) |


| No. | Description | Matlab | R |
| :---: | :---: | :---: | :---: |
| 179 | "while" statements to do iteration (useful when you don't know ahead of time how many iterations you'll need). E.g. to add uniform random numbers between 0 and 1 (and their squares) until their sum is greater than 20 : | ```mysum = 0; mysumsqr = 0; while (mysum < 20) r = rand; mysum = mysum + r; mysumsqr = mysumsqr + r^2; end``` | ```mysum = 0 mysumsqr = 0 while (mysum < 20) { r = runif(1) mysum = mysum + r mysumsqr = mysumsqr + r^2 }``` <br> (As with "if" statements and "for" loops, the curly brackets are not necessary if there's only one statement inside the "while" loop.) |
| 180 | More flow control: these commands exit or move on to the next iteration of the innermost while or for loop, respectively. | break and continue | break and next |
| 181 | "Switch" statements for integers | ```switch (x) case 10 disp('ten') case {12,13} disp('dozen (bakers?)') otherwise disp('unrecognized') end``` | $R$ doesn't have a switch statement capable of doing this. It has a function which is fairly limited for integers, but can which do string matching. See ?switch for more. But a basic example of what it can do for integers is below, showing that you can use it to return different expressions based on whether a value is $1,2, \ldots$. <br> mystr $=$ switch(x, 'one', 'two', <br> 'three'); print(mystr) <br> Note that switch returns NULL if $\mathbf{x}$ is larger than 3 in the above case. Also, continuous values of $\mathbf{x}$ will be truncated to integers. |

## 5 Functions, ODEs

| No. | Description | Matlab | R |
| :---: | :---: | :---: | :---: |
| 182 | Implement a function $\operatorname{add}(x, y)$ | Put the following in add.m: <br> function retval=add ( $\mathrm{x}, \mathrm{y}$ ) <br> retval = $x+y$; <br> Then you can do e.g. add $(2,3)$ | Enter the following, or put it in a file and source that file: ```add = function(x,y) { return(x+y) }``` <br> Then you can do e.g. add $(2,3)$. Note, the curly brackets aren't needed if your function only has one line. Also, the return keyword is optional in the above example, as the value of the last expression in a function gets returned, so just $\mathbf{x}+\mathbf{y}$ would work too. |
| 183 | Implement a function $\mathbf{f}(\mathbf{x}, \mathbf{y}, \mathbf{z})$ which returns multiple values, and store those return values in variables $\mathbf{u}$ and $\mathbf{v}$ | Write function as follows: $\begin{aligned} & \text { function }[\mathrm{a}, \mathrm{~b}]=\mathrm{f}(\mathrm{x}, \mathrm{y}, \mathrm{z}) \\ & \mathrm{a}=\mathrm{x} * \mathrm{y}+\mathrm{z} ; \quad \mathrm{b}=2 * \sin (\mathrm{x}-\mathrm{z}) ; \end{aligned}$ <br> Then call the function by doing: $[u, v]=f(2,8,12)$ | Write function as follows: ```f = function(x,y,z) { a = x*y+z; b=2*sin(x-z) return(list(a,b)) }``` <br> Then call the function by doing: $\quad \operatorname{tmp}=f(2,8,12) ; u=\operatorname{tmp}[[1]]$; $\mathrm{v}=\mathrm{tmp}[[2]]$. The above is most general, and will work even when $\mathbf{u}$ and $\mathbf{v}$ are different types of data. If they are both scalars, the function could simply return them packed in a vector, i.e. return $(c(a, b))$. If they are vectors of the same size, the function could return them packed together into the columns of a matrix, i.e. return (cbind $(a, b))$. |


| No. | Description | Matlab | R |
| :---: | :---: | :---: | :---: |
| 184 | Numerically solve ODE $d x / d t=5 x$ from $t=3$ to $t=12$ with initial condition $x(3)=7$ | First implement function <br> function retval $=f(t, x)$ <br> retval = 5*x; <br> Then do ode45(@f,[3,12],7) to plot solution, or $[t, x]=o d e 45(@ f,[3,12], 7)$ to get back vector $\mathbf{t}$ containing time values and vector $\mathbf{x}$ containing corresponding function values. If you want function values at specific times, e.g. $3,3.1,3.2, \ldots, 11.9,12$, you can do $[t, x]=o d e 45(@ f, 3: 0.1: 12,7)$. Note: in older versions of Matlab, use ' f ' instead of ©f. | First implement function <br> $\mathrm{f}=$ function(t, x, parms) \{ return(list( $5 * \mathrm{x}$ )) \} <br> Then do $y=1 \operatorname{soda}(7, \operatorname{seq}(3,12$, $0.1)$, f,NA) to obtain solution values at times $3,3.1,3.2, \ldots, 11.9,12$. The first column of $\mathbf{y}$, namely $\mathbf{y}[1]$ contains the time values; the second column $y[, 2]$ contains the corresponding function values. Note: lsoda is part of the deSolve package (see item 316 for how to install/load packages). |
| 185 | Numerically solve system of ODEs $d w / d t=5 w, d z / d t=$ $3 w+7 z$ from $t=3$ to $t=12$ with initial conditions $w(3)=$ $7, z(3)=8.2$ | First implement function <br> function retval=myfunc (t, $x$ ) <br> $\mathrm{w}=\mathrm{x}(1) ; \quad \mathrm{z}=\mathrm{x}(2)$; <br> retval $=$ zeros $(2,1)$; <br> retval(1) $=5 * \mathrm{w}$; <br> retval(2) $=3 * \mathrm{w}+7 * \mathrm{z}$; <br> Then do ode45(@myfunc, $[3,12],[7 ;$ <br> 8.2]) to plot solution, or $[t, x]=o d e 45$ (@myfunc, [3, 12] , [7; <br> 8.2]) to get back vector $\mathbf{t}$ containing time values and matrix $\mathbf{x}$, whose first column containing corresponding $w(t)$ values and second column contains $z(t)$ values. If you want function values at specific times, e.g. $3,3.1,3.2, \ldots, 11.9,12$, you can do $[\mathrm{t}, \mathrm{x}]=$ ode45(@myfunc , 3:0.1:12, [7 8.2]). Note: in older versions of Matlab, use ' $f$ ' instead of ©f. | First implement function <br> myfunc $=$ function(t, $x$, parms) \{ $\mathrm{w}=\mathrm{x}[1] ; \quad \mathrm{z}=\mathrm{x}[2]$; return(list(c(5*W, $\left.3 *{ }_{\mathrm{w}}+7 * \mathrm{z}\right)$ )) \} <br> Then do $\mathrm{y}=1 \operatorname{soda}(\mathrm{c}(7,8.2)$, seq(3,12, 0.1), myfunc,NA) to obtain solution values at times $3,3.1,3.2, \ldots, 11.9,12$. The first column of $\mathbf{y}$, namely $\mathbf{y}[, 1]$ contains the time values; the second column $\mathbf{y}[, 2]$ contains the corresponding values of $w(t)$; and the third column contains $z(t)$. Note: lsoda is part of the deSolve package (see item 316 for how to install/load packages). |
| 186 | Pass parameters such as $r=$ 1.3 and $K=50$ to an ODE function from the command line, solving $d x / d t=r x(1-$ $x / K)$ from $t=0$ to $t=20$ with initial condition $x(0)=$ 2.5. | First implement function <br> function retval=func2(t, $x, r, K$ ) <br> retval $=r * x *(1-x / K)$ <br> Then do ode45(@func2, [0 20], 2.5, [ ] , 1.3, 50). The empty matrix is necessary between the initial condition and the beginning of your extra parameters. | First implement function ```func2=function(t,x,parms) { r=parms[1]; K=parms [2] return(list(r*x*(1-x/K))) }``` <br> Then do $\begin{aligned} & y=1 \text { soda }(2.5, \operatorname{seq}(0,20,0.1) \\ & \text { func2, } c(1.3,50)) \end{aligned}$ <br> Note: lsoda is part of the deSolve package (see item 316 for how to install/load packages). |

## 6 Probability and random values

| No. | Description | Matlab | R |
| :---: | :---: | :---: | :---: |
| 187 | Generate a continuous uniform random value between 0 and 1 | rand | runif (1) |
| 188 | Generate vector of $n$ uniform random vals between 0 and 1 | $\operatorname{rand}(\mathrm{n}, 1)$ or $\operatorname{rand}(1, n)$ | runif (n) |
| 189 | Generate $m \times n$ matrix of uniform random values between 0 and 1 | rand (m, n ) | matrix (runif (m*n), m, n) or just matrix (runif (m*n),m) |
| 190 | Generate $m \times n$ matrix of continuous uniform random values between $a$ and $b$ | a+rand $(m, n) *(b-a)$ or if you have the Statistics toolbox then unifrnd (a,b,m,n) | matrix(runif (m*n, a, b) , m) |
| 191 | Generate a random integer between 1 and $k$ | floor (k*rand) + 1 | floor(k*runif(1)) + $1 \quad$ Note: sample(k) [1] would also work, but I believe in general will be less efficient, because that actually generates many random numbers and then just uses one of them. |
| 192 | Generate $m \times n$ matrix of discrete uniform random integers between 1 and $k$ | floor (k*rand(m,n))+1 or if you have the Statistics toolbox then unidrnd (k,m,n) | floor(k*matrix(runif(m*n),m))+1 |
| 193 | Generate $m \times n$ matrix where each entry is 1 with probability $p$, otherwise is 0 | (rand $(\mathrm{m}, \mathrm{n})<\mathrm{p}) * 1$ Note: multiplying by 1 turns the logical (true/false) result back into numeric values. You could also do double (rand (m,n) <p) | (matrix(runif $(m, n), m)<p) * 1$ <br> (Note: multiplying by 1 turns the logical (true/false) result back into numeric values; using as.numeric() to do it would lose the shape of the matrix.) |
| 194 | Generate $m \times n$ matrix where each entry is $a$ with probability $p$, otherwise is $b$ | $\mathrm{b}+(\mathrm{a}-\mathrm{b}) *(\mathrm{rand}(\mathrm{m}, \mathrm{n})<\mathrm{p})$ | $\begin{aligned} & \mathrm{b}+(\mathrm{a}-\mathrm{b}) *(\text { matrix } \\ & \text { runif }(\mathrm{m}, \mathrm{n}), \mathrm{m})<\mathrm{p}) \end{aligned}$ |
| 195 | Generate a random integer between $a$ and $b$ inclusive | floor ( $(\mathrm{b}-\mathrm{a}+1) * \mathrm{rand})+\mathrm{a}$ or if you have the Statistics toolbox then unidrnd ( $\mathrm{b}-\mathrm{a}+1$ ) $+\mathrm{a}-1$ | floor((b-a+1)*runif(1))+a |
| 196 | Flip a coin which comes up heads with probability $p$, and perform some action if it does come up heads | ```if (rand < p) ...some commands... end``` | ```if (runif(1) < p) \{ ...some commands... \}``` |
| 197 | Generate a random permutation of the integers $1,2, \ldots, n$ | randperm(n) | sample (n) |
| 198 | Generate a random selection of $k$ unique integers between 1 and $n$ (i.e. sampling without replacement) | [s,idx]=sort(rand $(n, 1))$; $r i=i d x(1: k)$ or another way is ri=randperm(n); ri=ri(1:k). Or if you have the Statistics Toolbox, then randsample ( $\mathrm{n}, \mathrm{k}$ ) | ri=sample(n,k) |
| 199 | Choose $k$ values (with replacement) from the vector $\mathbf{v}$, storing result in $\mathbf{w}$ | $\begin{aligned} & \mathrm{L}=\text { length }(\mathrm{v}) \text {; } \\ & \mathrm{w}=\mathrm{v}(\mathrm{floor}(\mathrm{~L} * \mathrm{rand}(\mathrm{k}, 1))+1) \text { Or, } \\ & \text { if you have the Statistics Toolbox, } \\ & \mathrm{w}=\mathrm{randsample}(\mathrm{v}, \mathrm{k}, \text { replace=true) } \end{aligned}$ | w=sample (v,k,replace=TRUE) |


| No. | Description | MATLAB | R |
| :--- | :--- | :--- | :--- |
| 200 | Choose $k$ values (without re- <br> placement) from the vector v, <br> storing result in w | L=length(v); ri=randperm(L); if <br> ri=ri(1:k); w=v(ri) Or, if <br> you have the Statistics Toolbox, <br> w=randsample(v,k,replace=false) | w=sample(v,k,replace=FALSE) |
| 201 | Set the random-number gen- <br> erator back to a known state <br> (useful to do at the beginning <br> of a stochastic simulation <br> when debugging, so you'll get <br> the same sequence of random <br> ning in Matlab 7.7, use this in- <br> numbers each time) | stead: RandStream('mt19937ar', <br> 'Seed', 12) though the previous <br> method is still supported for now. |  |

Note that the "*rnd," "*pdf," and "*cdf" functions described below are all part of the Matlab Statistics Toolbox, and not part of the core Matlab distribution.

| No. | Description | Matlab | R |
| :---: | :---: | :---: | :---: |
| 202 | Generate a random value from the $\operatorname{binomial}(n, p)$ distribution | binornd (n, p ) | rbinom (1, $\mathrm{n}, \mathrm{p}$ ) |
| 203 | Generate a random value from the Poisson distribution with parameter $\lambda$ | poissrnd(lambda) | rpois(1,lambda) |
| 204 | Generate a random value from the exponential distribution with mean $\mu$ | exprnd(mu) or -mu*log(rand) will work even without the Statistics Toolbox. | $\mathrm{rexp}(1,1 / \mathrm{mu})$ |
| 205 | Generate a random value from the discrete uniform distribution on integers $1 \ldots k$ | unidrnd(k) or floor (rand*k)+1 will work even without the Statistics Toolbox. | sample (k,1) |
| 206 | Generate $n$ iid random values from the discrete uniform distribution on integers $1 \ldots k$ | unidrnd ( $k, n, 1$ ) floor $(\operatorname{rand}(\mathrm{n}, 1) * \mathrm{k})+1$ will work even without the Statistics Toolbox. | sample(k,n,replace=TRUE) |
| 207 | Generate a random value from the continuous uniform distribution on the interval $(a, b)$ | unifrnd (a,b) or (b-a)*rand +a will work even without the Statistics Toolbox. | runif (1,a,b) |
| 208 | Generate a random value from the normal distribution with mean $\mu$ and standard deviation $\sigma$ | normrnd(mu,sigma) or mu + sigma*randn will work even without the Statistics Toolbox. | rnorm(1,mu,sigma) |
| 209 | Generate a random vector from the multinomial distribution, with n trials and probability vector $\mathbf{p}$ | mnrnd( $\mathrm{n}, \mathrm{p}$ ) | rmultinom(1, $\mathrm{n}, \mathrm{p}$ ) |
| 210 | Generate $\mathbf{j}$ random vectors from the multinomial distribution, with n trials and probability vector $\mathbf{p}$ | $\operatorname{mnrnd}(\mathrm{n}, \mathrm{p}, \mathrm{j})$ <br> The vectors are returned as rows of a matrix | rmultinom(j, n, p) <br> The vectors are returned as columns of a matrix |

Notes:

- The Matlab "*rnd" functions above can all take additional $\mathbf{r}, \mathbf{c}$ arguments to build an $r \times c$ matrix of iid random values. E.g. poissrnd ( $3.5,4,7$ ) for a $4 \times 7$ matrix of iid values from the Poisson distribution with mean $\lambda=3.5$. The unidrnd $(\mathrm{k}, \mathrm{n}, 1)$ command above is an example of this, to generate a $k \times 1$ column vector.
- The first parameter of the R " $r$ " functions above specifies how many values are desired. E.g. to generate 28 iid random values from a Poisson distribution with mean 3.5 , use rpois $(28,3.5)$. To get a $4 \times 7$ matrix of such values, use matrix (rpois $(28,3.5), 4$ ).

| No. | Description | Matlab | R |
| :---: | :---: | :---: | :---: |
| 211 | Compute probability that a random variable from the $\operatorname{Binomial}(n, p) \quad$ distribution has value $\mathbf{x}$ (i.e. the density, or pdf). | binopdf( $x, n, p$ ) nchoosek ( $\mathrm{n}, \mathrm{x}$ ) *p^x*(1-p)~(n-x) will work even without the Statistics Toolbox, as long as $\mathbf{n}$ and $\mathbf{x}$ are non-negative integers and $0 \leq \mathbf{p}$ $\leq 1$. | dbinom(x,n,p) |
| 212 | Compute probability that a random variable from the Poisson $(\lambda)$ distribution has value $\mathbf{x}$. | poisspdf(x,lambda) <br> $\exp (-1$ ambda) *lambda^x / <br> factorial(x) will work even without the Statistics Toolbox, as long as $\mathbf{x}$ is a non-negative integer and lambda $\geq 0$. | dpois(x,lambda) |
| 213 | Compute probability density function at x for a random variable from the exponential distribution with mean $\mu$. | exppdf ( $\mathrm{x}, \mathrm{mu}$ ) <br> ( $\mathrm{x}>=0$ ) $* \exp (-\mathrm{x} / \mathrm{mu}) / \mathrm{mu}$ will work even without the Statistics Toolbox, as long as $\mathbf{m u}$ is positive. | $\operatorname{dexp}(\mathrm{x}, 1 / \mathrm{mu})$ |
| 214 | Compute probability density function at $\mathbf{x}$ for a random variable from the Normal distribution with mean $\mu$ and standard deviation $\sigma$. | $\begin{aligned} & \text { normpdf }(x, \text { mu }, \text { sigma }) \\ & \exp \left(-(x-m u)^{\wedge} 2 /(2 * \text { sigma } 2)\right) / \\ & \text { (sqrt }(2 * \mathrm{pi}) * \text { sigma }) \text { will work even } \\ & \text { without the Statistics Toolbox. } \end{aligned}$ | dnorm(x,mu,sigma) |
| 215 | Compute probability density function at $\mathbf{x}$ for a random variable from the continuous uniform distribution on interval $(a, b)$. | unifpdf( $x, a, b)$ $((x>=a) \& \&(x<=b)) /(b-a) \quad$ will work even without the Statistics Toolbox. | dunif( $\mathrm{x}, \mathrm{a}, \mathrm{b}$ ) |
| 216 | Compute probability that a random variable from the discrete uniform distribution on integers $1 \ldots n$ has value $\mathbf{x}$. | unidpdf( $\mathrm{x}, \mathrm{n}$ ) or ( $(\mathrm{x}==\mathrm{floor}(\mathrm{x}))$ \&\& $(x>=1) \& \&(x<=n)) / n$ will work even without the Statistics Toolbox, as long as $\mathbf{n}$ is a positive integer. | $\begin{aligned} & ((x==r o u n d(x)) \& \&(x>=1) \& \& \\ & (x<=n)) / n \end{aligned}$ |
| 217 | Compute probability that a random vector from the multinomial distribution with probability vector $\vec{p}$ has the value $\vec{x}$ | $\operatorname{mnpdf}(x, p)$ <br> Note: vector $\mathbf{p}$ must sum to one. Also, $\mathbf{x}$ and $\mathbf{p}$ can be vectors of length $k$, or if one or both are $m \times k$ matrices then the computations are performed for each row. | dmultinom(x, prob=p) |

Note: one or more of the parameters in the above "*pdf" (Matlab) or "d*" (R) functions can be vectors, but they must be the same size. Scalars are promoted to arrays of the appropriate size.

The corresponding CDF functions are below:

| No. | Description | Matlab | R |
| :---: | :---: | :---: | :---: |
| 218 | Compute probability that a random variable from the $\operatorname{Binomial}(n, p)$ distribution is less than or equal to $\mathbf{x}$ (i.e. the cumulative distribution function, or cdf). | binocdf( $x, n, p$ ). Without the Statistics Toolbox, as long as $\mathbf{n}$ is a non-negative integer, this will work: $r=$ 0:floor(x); sum(factorial(n)./ (factorial(r).*factorial(n-r)) .*p. ^r.*(1-p).^(n-r)). <br> (Un- <br> fortunately, MATLAB's nchoosek function won't take a vector argument for $\mathbf{k}$.) | pbinom(x, $\mathrm{n}, \mathrm{p})$ |
| 219 | Compute probability that a random variable from the $\operatorname{Poisson}(\lambda)$ distribution is less than or equal to $\mathbf{x}$. | poisscdf(x,lambda). out the Statistics Toolbox, as long as lambda $\geq 0$ this will work: $r=0: f l o o r(x) ;$ $\operatorname{sum}\left(\exp (-l a m b d a) * l a m b d a .^{\wedge} r\right.$ $. / f a c t o r i a l(r))$ | ppois(x,lambda) |
| 220 | Compute cumulative distribution function at $\mathbf{x}$ for a random variable from the exponential distribution with mean $\mu$. | $\operatorname{expcdf}(x, m u)$ or <br> $(x>=0) *(1-\exp (-x / m u))$ will work even without the Statistics Toolbox, as long as mu is positive. | $\operatorname{pexp}(\mathrm{x}, 1 / \mathrm{mu})$ |
| 221 | Compute cumulative distribution function at $\mathbf{x}$ for a random variable from the Normal distribution with mean $\mu$ and standard deviation $\sigma$. | normcdf( $x, m u$, sigma) or $1 / 2-$ $\operatorname{erf}(-(x-m u) /($ sigma*sqrt (2))) $/ 2$ will work even without the Statistics Toolbox, as long as sigma is positive. | pnorm(x,mu,sigma) |
| 222 | Compute cumulative distribution function at $\mathbf{x}$ for a random variable from the continuous uniform distribution on interval $(a, b)$. | unifcdf ( $x, a, b$ ) or $(x>a) *(\min (x, b)-a) /(b-a) \quad$ will work even without the Statistics Toolbox, as long as $\mathbf{b}>\mathbf{a}$. | punif (x,a,b) |
| 223 | Compute probability that a random variable from the discrete uniform distribution on integers $1 \ldots n$ is less than or equal to $\mathbf{x}$. | unidcdf ( $\mathrm{x}, \mathrm{n}$ ) or ( $\mathrm{x}>=1$ ) $* \min (\mathrm{floor}(\mathrm{x}), \mathrm{n}) / \mathrm{n} \quad$ will work even without the Statistics Toolbox, as long as $\mathbf{n}$ is a positive integer. | ( $\mathrm{x}>=1$ ) $* \min (\mathrm{floor}(\mathrm{x}), \mathrm{n}) / \mathrm{n}$ |

## 7 Graphics

### 7.1 Various types of plotting

| No. | Description | Matlab | R |
| :---: | :---: | :---: | :---: |
| 224 | Create a new figure window | figure | dev.new() Notes: internally, on Windows this calls windows(), on MacOS it calls quartz(), and on Linux it calls x11(). x11() is also available on MacOS. In R sometime after 2.7.0, X11 graphics started doing antialising by default, which makes plots look smoother but takes longer to draw. If you are using R on Linux (which uses X11 graphics by default) or X11 graphics on MacOS and notice that figure plotting is extremely slow (especially if making many plots), do this before calling dev.new(): X11.options(type='Xlib') X11.options(antialias='none'). Or just use e.g. x11 (type='Xlib') to make new figure windows. They are uglier (lines are more jagged), but render much more quickly. |
| 225 | Select figure number $n$ | figure (n) (will create the figure if it doesn't exist) | dev.set(n) (returns the actual device selected; will be different from $n$ if there is no figure device with number $n$ ) |
| 226 | Determine which figure window is currently active | gcf | dev.cur() |
| 227 | List open figure windows | get (0,'children') (The 0 handle refers to the root graphics object.) | dev.list() |
| 228 | Close figure window(s) | close to close the current figure window, close(n) to close a specified figure, and close all to close all figures | dev.off() to close the currently active figure device, $\operatorname{dev}$. off $(n)$ to close a specified one, and graphics.off() to close all figure devices. |
| 229 | Plot points using open circles | plot(x,y, 'o') | plot (x,y) |
| 230 | Plot points using solid lines | plot (x,y) | plot(x,y,type='l') (Note: that's a lower-case 'L', not the number 1) |
| 231 | Plotting: color, point markers, linestyle | plot(x,y,str) where str is a string specifying color, point marker, and/or linestyle (see table below) (e.g. 'gs--' for green squares with dashed line) | ```plot(x,y,type=str1, pch=arg2,col=str3, lty=arg4)``` <br> See tables below for possible values of the 4 parameters |
| 232 | Plotting with logarithmic axes | semilogx, semilogy, and loglog functions take arguments like plot, and plot with logarithmic scales for $x, y$, and both axes, respectively | plot(..., log='x'), plot(..., log='y'), and plot(..., log='xy') plot with logarithmic scales for $x, y$, and both axes, respectively |


| No. | Description | Matlab | R |
| :---: | :---: | :---: | :---: |
| 233 | Make bar graph where the $x$ coordinates of the bars are in $\mathbf{x}$, and their heights are in $\mathbf{y}$ | bar ( $\mathrm{x}, \mathrm{y}$ ) Or just bar ( y ) if you only want to specify heights. Note: if $A$ is a matrix, bar (A) interprets each column as a separate set of observations, and each row as a different observation within a set. So a $20 \times 2$ matrix is plotted as 2 sets of 20 observations, while a $2 \times 20$ matrix is plotted as 20 sets of 2 observations. | Can't do this in R; but barplot(y) makes a bar graph where you specify the heights, barplot ( $\mathrm{y}, \mathrm{w}$ ) also specifies the widths of the bars, and hist can make plots like this too. |
| 234 | Make histogram of values in x | hist (x) | hist(x) |
| 235 | Given vector $\mathbf{x}$ containing integer values, make a bar graph where the $x$ coordinates of bars are the values, and heights are the counts of how many times the values appear in $\mathbf{x}$ | $\begin{aligned} & \mathrm{v}=\mathrm{unique}(\mathrm{x}) ; \mathrm{c}=\text { hist }(\mathrm{x}, \mathrm{v}) \text {; } \\ & \text { bar }(\mathrm{v}, \mathrm{c}) \end{aligned}$ | barplot(table(x)) |
| 236 | Given vector $\mathbf{x}$ containing continuous values, lump the data into $k$ bins and make a histogram / bar graph of the binned data | [ $\mathrm{c}, \mathrm{m}]=\operatorname{hist}(\mathrm{x}, \mathrm{k})$; $\operatorname{bar}(\mathrm{m}, \mathrm{c})$ or for slightly different plot style use hist ( $\mathrm{x}, \mathrm{k}$ ) | $\begin{aligned} & \text { hist }(x, \operatorname{seq}(\min (x), \max (x), \\ & \text { length.out }=k+1)) \end{aligned}$ |
| 237 | Make a plot containing errorbars of height $\mathbf{s}$ above and below $(x, y)$ points | errorbar (x,y,s) | errbar ( $\mathrm{x}, \mathrm{y}, \mathrm{y}+\mathrm{s}, \mathrm{y}-\mathrm{s}$ ) Note: errbar is part of the Hmisc package (see item 316 for how to install/load packages). |
| 238 | Make a plot containing errorbars of height $\mathbf{a}$ above and $\mathbf{b}$ below ( $x, y$ ) points | errorbar (x,y,b,a) | errbar( $\mathrm{x}, \mathrm{y}, \mathrm{y}+\mathrm{a}, \mathrm{y}-\mathrm{b}$ ) Note: errbar is part of the Hmisc package (see item 316 for how to install/load packages). |
| 239 | Other types of 2-D plots | stem ( $\mathrm{x}, \mathrm{y}$ ) and $\operatorname{stairs}(\mathrm{x}, \mathrm{y})$ for other types of 2-D plots. polar(theta,r) to use polar coordinates for plotting. | pie(v) |


| No. | Description | Matlab | R |
| :---: | :---: | :---: | :---: |
| 240 | Make a 3-D plot of some data points with given $x, y, z$ coordinates in the vectors $\mathbf{x}, \mathbf{y}$, and $\mathbf{z}$. | plot3( $x, y, z$ ) This works much like plot, as far as plotting symbols, linetypes, and colors. | cloud( $z^{\sim} x * y$ ) You can also use arguments pch and col as with plot. To make a 3-D plot with lines, do cloud( $z^{\sim} x * y, t y p={ }^{\prime} l^{\prime}$, panel.cloud=panel.3dwire) |
| 241 | Surface plot of data in matrix A | $\operatorname{surf}(A)$ <br> You can then click on the small curved arrow in the figure window (or choose "Rotate 3D" from the "Tools" menu), and then click and drag the mouse in the figure to rotate it in three dimensions. | persp(A) <br> You can include shading in the image via e.g. persp(A,shade=0.5). There are two viewing angles you can also specify, among other parameters, e.g. persp(A, shade=0.5, theta=50, phi=35). |
| 242 | Surface plot of $f(x, y)=$ $\sin (x+y) \sqrt{y}$ for 100 values of $x$ between 0 and 10, and 90 values of $y$ between 2 and 8 | $\begin{aligned} & \mathrm{x}=\operatorname{linspace}(0,10,100) ; \\ & \mathrm{y}=\operatorname{linspace}(2,8,90) ; \\ & {[\mathrm{X}, \mathrm{Y}]=\operatorname{meshgrid}(\mathrm{x}, \mathrm{y}) ;} \\ & \mathrm{Z}=\sin (\mathrm{X}+\mathrm{Y}) . * \operatorname{sqrt}(\mathrm{Y}) ; \\ & \operatorname{surf}(\mathrm{X}, \mathrm{Y}, \mathrm{Z}) \\ & \text { shading flat } \end{aligned}$ | $\begin{aligned} & x=\operatorname{seq}(0,10, l e n=100) \\ & y=\operatorname{seq}(2,8, l e n=90) \\ & f=\operatorname{function}(x, y) \\ & \quad \text { return }(\sin (x+y) * \operatorname{sqrt}(y)) \\ & z=\operatorname{outer}(x, y, f) \\ & \operatorname{persp}(x, y, z) \end{aligned}$ |
| 243 | Other ways of plotting the data from the previous command | $\operatorname{mesh}(X, Y, Z)$,$\operatorname{surfl}(X, Y, Z), \quad \operatorname{surfc}(X, Y, Z)$,$\operatorname{pcolor}(X, Y, Z)$,waterfall $(X, Y, Z)$.slice command.$l$ |  |
| 244 | Set axis ranges in a figure window | axis([x1 x2 y1 y2]) | You have to do this whenyou make the plot,plot $(x, y, x l i m=c(x 1, x 2)$, <br> ylim $=c(y 1, y 2))$ |
| 245 | Add title to plot | title('somestring') | title(main='somestring') <br> adds a main <br> title, <br> title(sub='somestring') adds <br> a subtitle. You can also include main $=$ and sub $=$ arguments in a plot command. |
| 246 | Add axis labels to plot | xlabel('somestring') and ylabel('somestring') | title(xlab='somestring', <br> ylab='anotherstr'). You can <br> also include $\mathrm{xlab}=$ and $\mathrm{ylab}=$ arguments in a plot command. |


| No. | Description | Matlab | R |
| :---: | :---: | :---: | :---: |
| 247 | Include Greek letters or symbols in plot axis labels | You can use basic TeX commands, e.g. plot(x,y); <br> xlabel(' ${ }^{\text {phi^2 }}+\backslash$ mu_\{i,j\}') or xlabel('fecundity \phi') See also help tex and parts of doc text_props for more about building labels using general LaTeX commands | ```plot(x,y,xlab= expression(phi^2 + mu['i,j'])) or plot(x,y,xlab=expression( paste('fecundity ', phi))) See also help(plotmath) and p. 98 of the R Graphics book by Paul Murrell for more.``` |
| 248 | Change font size to 16 in plot labels | For the legends and numerical axis labels, use set(gca, 'FontSize', 16), and for text labels on axes do e.g. xlabel('my x var', 'FontSize', 16) | For on-screen graphics, do $\operatorname{par}(\mathrm{ps}=16)$ followed by e.g. a plot command. For PostScript or PDF plots, add a pointsize=16 argument, e.g. pdf('myfile.pdf', width=8, height=8, pointsize=16) (see items 264 and 265) |
| 249 | Add grid lines to plot | grid on (and grid off to turn off) | grid() Note that if you'll be printing the plot, the default style for grid-lines is to use gray dotted lines, which are almost invisible on some printers. You may want to do e.g. grid(lty='dashed', col='black') to use black dashed lines which are easier to see. |
| 250 | Add a text label to a plot | text(x,y, 'hello') | text (x,y, 'hello') |
| 251 | Add set of text labels to a plot. $\mathbf{x v}$ and $\mathbf{y v}$ are vectors. | $\begin{aligned} & \mathrm{s}=\{\text { 'hi', 'there'\}; } \\ & \text { text (xv, yv,s) } \end{aligned}$ | $\begin{aligned} & \text { s=c('hi', 'there'); } \\ & \text { text(xv,yv,s) } \end{aligned}$ |
| 252 | Add an arrow to current plot, with tail at $(x t, y t)$ and head at ( $x h, y h$ ) | annotation('arrow', [xt xh], [yt yh]) Note: coordinates should be normalized figure coordinates, not coordinates within your displayed axes. Find and download from The Mathworks the file dsxy2figxy.m which converts for you, then do this: [fx,fy]=dsxy2figxy([xt xh], [yt yh]); annotation('arrow', fx, fy) | arrows(xt, yt, xh, yh) |
| 253 | Add a double-headed arrow to current plot, with coordinates $(x 0, y 0)$ and $(x 1, y 1)$ | annotation('doublearrow', [x0 x1], [y0 y1]) See note in previous item about normalized figure coordinates. | arrows (x0, y0, x1, y1, code=3) |
| 254 | Add figure legend to top-left corner of plot | legend('first', 'second', <br> 'Location', 'NorthWest') | ```legend('topleft', legend=c('first', 'second'), col=c('red', 'blue'), pch=c('*','o'))``` |

MATLAB note: sometimes you build a graph piece-by-piece, and then want to manually add a legend which doesn't correspond with the order you put things in the plot. You can manually construct a legend by plotting "invisible" things, then building the legend using them. E.g. to make a legend with black stars and solid lines, and red circles and dashed lines: h1=plot ( 0,0, 'k*-') ; set(h1,'Visible', 'off'); h2=plot ( 0,0, ' $k *-'$ ) ; set (h2, 'Visible', 'off'); legend([h1 h2], 'blah, 'whoa'). Just be sure to choose coordinates for your "invisible" points within the current figure's axis ranges.

| No. | Description | Matlab | R |
| :---: | :---: | :---: | :---: |
| 255 | Adding more things to a figure | hold on means everything plotted from now on in that figure window is added to what's already there. hold off turns it off. clf clears the figure and turns off hold. | points(...) and lines(...) work like plot, but add to what's already in the figure rather than clearing the figure first. points and lines are basically identical, just with different default plotting styles. Note: axes are not recalculated/redrawn when adding more things to a figure. |
| 256 | Plot multiple data sets at once | plot $(x, y)$ where $x$ and $y$ are $2-D$ matrices. Each column of $\mathbf{x}$ is plotted against the corresponding column of $\mathbf{y}$. If $\mathbf{x}$ has only one column, it will be re-used. | matplot ( $\mathrm{x}, \mathrm{y}$ ) where x and y are 2-D matrices. Each column of $\mathbf{x}$ is plotted against the corresponding column of $\mathbf{y}$. If $\mathbf{x}$ has only one column, it will be re-used. |
| 257 | Plot $\sin (2 x)$ for $x$ between 7 and 18 | fplot('sin(2*x)', [7 18]) | curve ( $\sin (2 * x), 7,18,200)$ makes the plot, by sampling the value of the function at 200 values between 7 and 18 (if you don't specify the number of points, 101 is the default). You could do this manually yourself via commands like $\quad \operatorname{tmpx}=\operatorname{seq}(7,18,1 e n=200)$; plot (tmpx, $\sin (2 * \operatorname{tmpx})$ ). |
| 258 | Plot color image of integer values in matrix $\mathbf{A}$ | image (A) to use array values as raw indices into colormap, or imagesc(A) to automatically scale values first (these both draw row 1 of the matrix at the top of the image); or pcolor(A) (draws row 1 of the matrix at the bottom of the image). After using pcolor, try the commands shading flat or shading interp. | image (A) (it rotates the matrix 90 degrees counterclockwise: it draws row 1 of $A$ as the left column of the image, and column 1 of $A$ as the bottom row of the image, so the row number is the $x$ coord and column number is the $y$ coord). It also rescales colors. If you are using a colormap with $k$ entries, but the value $k$ does not appear in $A$, use image $(\mathrm{A}, \mathrm{zlim}=\mathrm{c}(1, \mathrm{k}))$ to avoid rescaling of colors. Or e.g. image $(A, z l i m=c(0, k-1))$ if you want values 0 through $k-1$ to be plotted using the $k$ colors. |
| 259 | Add colorbar legend to image plot | colorbar, after using image or pcolor. | Use filled.contour(A) rather than image (A), although it "blurs" the data via interpolation, or use levelplot(A) from the lattice package (see item 316 for how to load packages). To use a colormap with the latter, do e.g. levelplot(A,col.regions= terrain.colors(100)). |
| 260 | Set colormap in image | colormap (hot). Instead of hot, you can also use gray, flag, jet (the default), cool, bone, copper, pink, hsv, prism. By default, the length of the new colormap is the same as the currently-installed one; use e.g. colormap(hot(256)) to specify the number of entries. | image(A, col=terrain.colors(100)) The parameter 100 specifies the length of the colormap. Other colormaps are heat.colors(), topo.colors(), and cm.colors(). |


| No. | Description | Matlab | R |
| :---: | :---: | :---: | :---: |
| 261 | Build your own colormap using Red/Green/Blue triplets | Use an $n \times 3$ matrix; each row gives R,G,B intensities between 0 and 1. Can use as argument with colormap. E.g. for 2 colors: mycmap $=\left[\begin{array}{lllllll}0.5 & 0.8 & 0.2 & ; & 0.2 & 0.2 & 0.7\end{array}\right]$ | Use a vector of hexadecimal strings, each beginning with '\#' and giving R,G,B intensities between 00 and FF. E.g. c('\#80CC33', '\#3333B3'); can use as argument to $\mathbf{c o l}=$ parameter to image. You can build such a vector of strings from vectors of Red, Green, and Blue intensities (each between 0 and 1) as follows (for a 2-color example): $\quad r=c(0.5,0.2)$; $\mathrm{g}=\mathrm{c}(0.8,0.2)$; $\mathrm{b}=\mathrm{c}(0.2,0.7)$; mycolors=rgb(r,g,b). |

Matlab plotting specifications, for use with plot, fplot, semilogx, semilogy, loglog, etc:

| Symbol | Color | Symbol | Marker | Symbol | Linestyle |
| :---: | :--- | :---: | :--- | :---: | :--- |
| b | blue | $\cdot$ | point (.) | - | solid line |
| g | green | $\circ$ | circle (o) | $:$ | dotted line |
| r | red | x | cross $(\times)$ | .- | dash-dot line |
| c | cyan | + | plus sign $(+)$ | -- | dashed line |
| m | magenta | $*$ | asterisk $(*)$ |  |  |
| y | yellow | s | square ( $\square)$ |  |  |
| k | black | d | diamond ( $\diamond)$ |  |  |
| w | white | v | triangle (down) $(\nabla)$ |  |  |
|  |  | $\sim$ | triangle (up) $(\triangle)$ |  |  |
|  |  | $<$ | triangle (left) $(\triangleleft)$ |  |  |
|  |  | $>$ | triangle (right) $(\triangleright)$ |  |  |
|  |  | p | pentragram star |  |  |
|  |  | h | hexagram star |  |  |

R plotting specifications for col (color), pch (plotting character), and type arguments, for use with plot, matplot, points, and lines:

| col | Description | pch | Description | type | Description |
| :---: | :--- | :--- | :--- | :--- | :--- |
| 'blue' | Blue | 'a' | a (similarly for other <br> characters, but see '.' <br> below for an exception | p | points |
| 'green' | Green | 19 | solid circle | l | lines |
| 'red' | Red | 20 | bullet (smaller circle) | b | both |
| 'cyan' | Cyan | 21 | open circle | c | lines part only of "b" |
| 'magenta' | Magenta | 22 | square | o | lines, points overplotted |
| 'yellow' | Yellow | 23 | diamond | h | histogram-like lines |
| 'black' | Black | 24 | triangle point-up | s | steps |
| '\#RRGGBB' | hexadecimal specifica- <br> tion of Red, Green, <br> Blue | 25 | triangle point-down | S | another kind of steps |
| (Other names) | See colors() for list of <br> available color names. | '.' | rectangle of size 0.01 <br> inch, 1 pixel, or 1 point <br> (1/72 inch) depending <br> on device | n | no plotting |
|  | (See table on next page <br> for more) |  |  |  |  |

R plotting specifications for lty (line-type) argument, for use with plot, matplot, points, and lines:

| lty | Description |
| :---: | :--- |
| 0 | blank |
| 1 | solid |
| 2 | dashed |
| 3 | dotted |
| 4 | dotdash |
| 5 | longdash |
| 6 | twodash |



R plotting characters, i.e. values for pch argument (from the book $R$ Graphics, by Paul Murrell, Chapman \& Hall / CRC, 2006)

| No. | Description | Matlab | R |
| :---: | :---: | :---: | :---: |
| 262 | Divide up a figure window into smaller sub-figures | subplot ( $\mathrm{m}, \mathrm{n}, \mathrm{k}$ ) divides the current figure window into an $m \times n$ array of subplots, and draws in subplot number $k$ as numbered in "reading order," i.e. left-to-right, top-tobottom. E.g. subplot $(2,3,4)$ selects the first sub-figure in the second row of a $2 \times 3$ array of sub-figures. You can do more complex things, e.g. subplot (5,5,[1 2 67]) selects the first two subplots in the first row, and first two subplots in the second row, i.e. gives you a bigger subplot within a $5 \times 5$ array of subplots. (If you that command followed by e.g. subplot ( $5,5,3$ ) you'll see what's meant by that.) | There are several ways to do this, e.g. using layout or split.screen, although they aren't quite as friendly as Matlab 's. E.g. if you let $A=$ $\left[\begin{array}{lll}1 & 1 & 2 \\ 1 & 1 & 3 \\ 4 & 5 & 6\end{array}\right]$, then layout(A) will divide the figure into 6 sub-figures: you can imagine the figure divide into a $3 \times 3$ matrix of smaller blocks; subfigure 1 will take up the upper-left $2 \times 2$ portion, and sub-figures $2-6$ will take up smaller portions, according to the positions of those numbers in the matrix $A$. Consecutive plotting commands will draw into successive subfigures; there doesn't seem to be a way to explicitly specify which sub-figure to draw into next. <br> To use split.screen, you can do e.g. split.screen $(c(2,1))$ to split into a $2 \times 1$ matrix of subfigures (numbered 1 and 2). Then split.screen $(c(1,3), 2)$ splits subfigure 2 into a $1 \times 3$ matrix of smaller sub-figures (numbered 3, 4, and 5). screen(4) will then select sub-figure number 4 , and subsequent plotting commands will draw into it. <br> A third way to accomplish this is via the commands par(mfrow=) or $\operatorname{par}(m f c o l=)$ to split the figure window, and $\operatorname{par}(\mathrm{mfg}=)$ to select which sub-figure to draw into. <br> Note that the above methods are all incompatible with each other. |
| 263 | Force graphics windows to update | drawnow (Matlab normally only updates figure windows when a script/function finishes and returns control to the Matlab prompt, or under a couple of other circumstances. This forces it to update figure windows to reflect any recent plotting commands.) | $R$ automatically updates graphics windows even before functions/scripts finish executing, so it's not necessary to explictly request it. But note that some graphics functions (particularly those in the lattice package) don't display their results when called from scripts or functions; e.g. rather than levelplot(...) you need to do print(levelplot(...)). Such functions will automatically display their plots when called interactively from the command prompt. |

### 7.2 Printing/saving graphics

| No. | Description | Matlab | R |
| :---: | :---: | :---: | :---: |
| 264 | To print/save to a PDF file named fname.pdf | print -dpdf fname saves the contents of currently active figure window | First do pdf('fname.pdf'). Then, do various plotting commands to make your image, as if you were plotting in a window. Finally, do dev.off() to close/save the PDF file. To print the contents of the active figure window, do dev.copy(device=pdf, file='fname.pdf'); dev.off(). <br> (But this will not work if you've turned off the display list via dev.control(displaylist= 'inhibit').) |
| 265 | To print/save to a PostScript file fname.ps or fname.eps | print -dps fname for black \& white PostScript; print -dpsc fname for color PostScript; print -deps fname for black \& white Encapsulated PostScript; print -depsc fname for color Encapsulated PostScript. The first two save to fname.ps, while the latter two save to fname.eps. | postscript('fname.eps'), followed by your plotting commands, followed by dev.off() to close/save the file. Note: you may want to use postscript('fname.eps', horizontal=FALSE) to save your figure in portrait mode rather than the default landscape mode. To print the contents of the active figure window, do dev.copy(device=postscript, file='fname.eps'); dev.off(). <br> (But this will not work if you've turned off the display list via dev.control(displaylist= 'inhibit').) You can also include the horizontal=FALSE argument with dev.copy(). |
| 266 | To print/save to a JPEG file fname.jpg with jpeg quality $=90$ (higher quality looks better but makes the file larger) | print -djpeg90 fname | jpeg('fname.jpg', quality=90), followed by your plotting commands, followed by dev.off() to close/save the file. |

### 7.3 Animating cellular automata / lattice simulations

| No. | Description | Matlab | R |
| :---: | :---: | :---: | :---: |
| 267 | To display images of cellular automata or other lattice simulations while running in real time | Repeatedly use either pcolor or image to display the data. Don't forget to call drawnow as well, otherwise the figure window will not be updated with each image. | If you simply call image repeatedly, there is a great deal of flickering/flashing. To avoid this, after drawing the image for the first time using e.g. image(A), from then on only use image(A, add=TRUE), which avoids redrawing the entire image (and the associated flicker). However, this will soon consume a great deal of memory, as all drawn images are saved in the image buffer. There are two solutions to that problem: (1) every $k$ time steps, leave off the "add=TRUE" argument to flush the image buffer (and get occasional flickering), where you choose $k$ to balance the flickering vs. memory-usage tradeoff; or (2) after drawing the first image, do dev.control(displaylist= 'inhibit') to prohibit retaining the data. However, the latter solution means that after the simulation is done, the figure window will not be redrawn if it is resized, or temporarily obscured by another window. call to dev.control(displaylist= 'enable') and then one final image(A) at the end of the simulation will re-enable re-drawing after resizing or obscuring, without consuming extra memory.) |

## 8 Working with files

| No. | Description | Matlab | R |
| :---: | :---: | :---: | :---: |
| 268 | Create a folder (also known as a "directory") | mkdir dirname | dir.create('dirname') |
| 269 | Set/change working directory | cd dirname | setwd('dirname') |
| 270 | See list of files in current working directory | dir | dir () |
| 271 | Run commands in file 'foo.m' or 'foo.R' respectively | foo | source('foo.R') |
| 272 | Read data from text file "data.txt" into matrix $A$ | A=load('data.txt') or A=importdata('data.txt') Note that both routines will ignore comments (anything on a line following a "\%" character) | ```A=as.matrix(read.table( 'data.txt')) This will ignore comments (anything on a line following a "#" character). To ig- nore comments indicated by "%", do A=as.matrix(read.table( 'data.txt', comment.char='%'))``` |
| 273 | Write data from matrix $A$ into text file "data.txt" | save data.txt A -ascii | $\begin{aligned} & \text { write(A, file='data.txt', } \\ & \text { ncolumn=dim(A)[2]) } \end{aligned}$ |

## 9 Miscellaneous

### 9.1 Variables

| No. | Description | Matlab | R |
| :---: | :---: | :---: | :---: |
| 274 | Assigning to variables | $\mathrm{x}=5$ | x <- 5 or $\mathrm{x}=5$ Note: for compatibility with S-plus, many people prefer the first form. |
| 275 | From within a function, assign a value to variable $\mathbf{y}$ in the base environment (i.e. the command prompt environment) | assignin('base', 'y', 7) | $\mathrm{y} \ll-7$ |
| 276 | From within a function, access the value of variable $\mathbf{y}$ in the base environment (i.e. the command prompt environment) | evalin('base', 'y') | get('y', envir=globalenv()) Though note that inside a function, if there isn't a local variable $\mathbf{y}$, then just the expression y will look for one in the base environment, but if there is a local $\mathbf{y}$ then that one will be used instead. |
| 277 | Short list of defined variables | who | ls() |
| 278 | Long list of defined variables | whos | ls.str() |
| 279 | See detailed info about the variable ab | whos ab | str (ab) |
| 280 | See detailed info about all variables with "ab" in their name | whos *ab* | ls.str (pattern='ab') |
| 281 | Open graphical data editor, to edit the value of variable A (useful for editing values in a matrix, though it works for non-matrix variables as well) | openvar(A), or double-click on the variable in the Workspace pane (if it's being displayed) of your MatLABdesktop | fix (A) |
| 282 | Clear one variable | clear x | rm(x) |
| 283 | Clear two variables | clear x y | rm( $\mathrm{x}, \mathrm{y}$ ) |
| 284 | Clear all variables | clear all | rm(list=ls()) |
| 285 | See what type of object x is | class (x) | class (x) |
| 286 | (Variable names) | Variable names must begin with a letter, but after that they may contain any combination of letters, digits, and the underscore character. Names are case-sensitive. | Variable names may contain letters, digits, the period, and the underscore character. They cannot begin with a digit or underscore, or with a period followed by a digit. Names are casesensitive. |
| 287 | Result of last command | ans contains the result of the last command which did not assign its value to a variable. E.g. after $2+5$; $x=3$, then ans will contain 7 . | .Last.value contains the result of the last command, whether or not its value was assigned to a variable. E.g. after $2+5$; $x=3$, then .Last.value will contain 3. |

### 9.2 Strings and Misc.

| No. | Description | Matlab | R |
| :---: | :---: | :---: | :---: |
| 288 | Line continuation | If you want to break up a Matlab command over more than one line, end all but the last line with three periods: ". . ". E.g.: $x=3+\ldots$ <br> or $\begin{gathered} x=3 \ldots \\ \\ +4 \end{gathered}$ | In R, you can spread commands out over multiple lines, and nothing extra is necessary. $R$ will continue reading input until the command is complete. However, this only works when the syntax makes it clear that the first line was not complete. E.g.: $x=3+$ <br> 4 <br> works, but $\begin{aligned} x= & 3 \\ & +4 \end{aligned}$ <br> does not treat the second line as a continuation of the first. |
| 289 | Controlling formatting of output | ```format short g and format long g are handy; see help format``` | options(digits=6) tells R you'd like to use 6 digits of precision in values it displays (it is only a suggestion, not strictly followed) |
| 290 | Exit the program | quit or exit | q() or quit() |
| 291 | Comments | \% this is a comment | \# this is a comment |
| 292 | Display a string | disp('hi there') or to <br> omit trailing newline use  <br> fprintf('hi there')   | print('hi there') |
| 293 | Display a string containing single quotes | disp('It''s nice') to omit trailing newline fprintf('It''s nice') | ```print('It\'s nice') print("It's nice")``` |
| 294 | Give prompt and read numerical input from user | $\mathrm{x}=$ input('Enter data:') | print('Enter data:'); x=scan() But note: if in a script and you use the Edit $\rightarrow$ Execute menu item to run it, the selected text after the scan statement will be used as source for the input, rather than keyboard. |
| 295 | Give prompt and read character (string) input from user | x = input('Enter string:', 's') | x = readline('Enter string:') |
| 296 | Concatenate strings | ['two hal' 'ves'] | paste('two hal', 'ves', sep='') |
| 297 | Concatenate strings stored in a vector | v=\{'two ', 'halves'\}; <br> strcat(v\{:\}) But note that this drops trailing spaces on strings. To avoid that, instead do strcat([v\{:\}]) | ```v=c('two ', 'halves'); paste(v, collapse='')``` |
| 298 | Extract substring of a string | $\begin{aligned} & \text { text1='hi there'; } \\ & \text { text2=text }(2: 6) \end{aligned}$ | ```text1='hi there'; text2=substr(text1,2,6)``` |
| 299 | Determine whether elements of a vector are in a set, and give positions of corresponding elements in the set. | Then loc contains the locations of last occurrences of elements of $\mathbf{x}$ in the set $\mathbf{y}$, and 0 for unmatched elements. |  'aa'); loc=match(x,y) Then loc contains the locations of first occurences of elements of $\mathbf{x}$ in the set $\mathbf{y}$, and NA for unmatched elements. |


| No. | Description | Matlab | R |
| :---: | :---: | :---: | :---: |
| 300 | Convert number to string | num2str (x) | as.character (x) |
| 301 | Use sprintf to create a formatted string. Use \%d for integers ("d" stands for "decimal", i.e. base 10 ), $\% \mathbf{f}$ for floating-point numbers, \%e for scientific-notation floating point, $\% \mathrm{~g}$ to automatically choose $\% \mathbf{e}$ or $\% \mathbf{f}$ based on the value. You can specify field-widths/precisions, e.g. $\% 5 \mathrm{~d}$ for integers with padding to 5 spaces, or $\% \mathbf{\%} \mathbf{7 f}$ for floating-point with 7 digits of precision. There are many other options too; see the docs. | $\begin{aligned} & \mathrm{x}=2 \text {; } \mathrm{y}=3.5 \text {; } \\ & \mathrm{s}=\text { sprintf }\left({ }^{\prime} \mathrm{x} \text { is } \% \mathrm{~d}, \mathrm{y}=\% \mathrm{~g} \text { ', } \ldots\right. \\ & \quad \mathrm{x}, \mathrm{y}) \end{aligned}$ | $\begin{aligned} & \mathrm{x}=2 ; \mathrm{y}=3.5 \\ & \mathrm{~s}=\operatorname{sprintf}\left(\mathrm{s}^{\mathrm{x}} \text { is } \% \mathrm{~d}, \mathrm{y} \text { is } \% \mathrm{~g}\right. \text { ', } \\ & \mathrm{x}, \mathrm{y}) \end{aligned}$ |
| 302 | Machine epsilon $\epsilon_{\text {mach }}$, i.e. difference between 1 and the next largest double-precision floating-point number | eps (See help eps for various other things eps can give.) | .Machine\$double.eps |
| 303 | Pause for $x$ seconds | pause (x) | Sys.sleep(x) |
| 304 | Wait for user to press any key | pause | Don't know of a way to do this in R, but scan (quiet=TRUE) will wait until the user presses the Enter key |
| 305 | Measure CPU time used to do some commands | $\begin{aligned} & \text { t1=cputime; ...commands... ; } \\ & \text { cputime-t1 } \end{aligned}$ | ```t1=proc.time(); ...commands... ; (proc.time()-t1)[1]``` |
| 306 | Measure elapsed ("wallclock") time used to do some commands | ```tic; ...commands... ; toc or t1=clock; ...commands... ; etime(clock,t1)``` | ```t1=proc.time(); ...commands... ; (proc.time()-t1)[3]``` |
| 307 | Print an error message an interrupt execution | error('Problem!') | stop('Problem!') |
| 308 | Print a warning message | warning('Smaller problem!') | warning('Smaller problem!') |
| 309 | Putting multiple statements on one line | Separate statements by commas or semicolons. A semicolon at the end of a statement suppresses display of the results (also useful even with just a single statement on a line), while a comma does not. | Separate statements by semicolons. |
| 310 | Evaluate contents of a string $\mathbf{s}$ as command(s). | eval (s) | eval (parse(text=s)) |
| 311 | Get a command prompt for debugging, while executing a script or function. While at that prompt, you can type expressions to see the values of variables, etc. | Insert the command keyboard in your file. Note that your prompt will change to $\mathbf{K} \gg$. When you are done debugging and want to continue executing the file, type return. | Insert the command browser() in your file. Note that your prompt will change to Browse[1]>. When you are done debugging and want to continue executing the file, either type c or just press return (i.e. enter a blank line). Note, if you type n, you enter the step debugger. |


| No. | Description | Matlab | R |
| :---: | :---: | :---: | :---: |
| 312 | Show where a command is | which sqrt shows you where the file defining the sqrt function is (but note that many basic functions are "built in," so the Matlab function file is really just a stub containing documentation). This is useful if a command is doing something strange, e.g. sqrt isn't working. If you've accidentally defined a variable called sqrt, then which sqrt will tell you, so you can clear sqrt to erase it so that you can go back to using the function sqrt. | R does not execute commands directly from files, so there is no equivalent command. |
| 313 | Query/set the search path. | path displays the current search path (the list of places Matlab searches for commands you enter). To add a directory ~/foo to the beginning of the search path, do <br> addpath ~/foo -begin <br> or to add it to the end of the path, do addpath ~/foo -end (Note: you should generally add the full path of a directory, i.e. in Linux or Mac OS-X something like ~/foo as above or of the form /usr/local/lib/foo, while under Windows it would be something like $\mathbf{C}$ :/foo) | R does not use a search path to look for files. |
| 314 | Startup sequence | If a file startup.m exists in the startup directory for Matlab, its contents are executed. (See the Matlab docs for how to change the startup directory.) | If a file .Rprofile exists in the current directory or the user's home directory (in that order), its contents are sourced; saved data from the file .RData (if it exists) are then loaded. If a function .First() has been defined, it is then called (so the obvious place to define this function is in your .Rprofile file). |
| 315 | Shutdown sequence | Upon typing quit or exit, Matlab will run the script finish.m if present somewhere in the search path. | Upon typing q() or quit (), $R$ will call the function .Last() if it has been defined (one obvious place to define it would be in the .Rprofile file) |


| No. | Description | Matlab | R |
| :---: | :---: | :---: | :---: |
| 316 | Install and load a package. | Matlab does not have packages. It has toolboxes, which you can purchase and install. "Contributed" code (written by end users) can simply be downloaded and put in a directory which you then add to MATLAB's path (see item 313 for how to add things to Matlab's path). | To install e.g. the deSolve package, you can use the command install.packages('deSolve'). You then need to load the package in order to use it, via the command library('deSolve'). When running R again later you'll need to load the package again to use it, but you should not need to re-install it. Note that the lattice package is typically included with binary distributions of $R$, so it only needs to be loaded, not installed. |

## 10 Spatial Modeling

| No. | Description | Matlab | R |
| :---: | :---: | :---: | :---: |
| 317 | Take an $L \times \mathrm{L}$ matrix $\mathbf{A}$ of 0s and 1s, and "seed" fraction $p$ of the 0s (turn them into 1s), not changing entries which are already 1. | $\mathrm{A}=(\mathrm{A} \mid(\operatorname{rand}(\mathrm{L})<\mathrm{p}))^{1}$; | $\begin{aligned} & \mathrm{A}=\left(\mathrm{A} \mid \quad \text { (matrix(runif }\left(\mathrm{L}^{\wedge} 2\right), \mathrm{L}\right) \\ & <\mathrm{p})) * 1 \end{aligned}$ |
| 318 | Take an $L \times L$ matrix $\mathbf{A}$ of 0s and 1 s , and "kill" fraction $p$ of the 1 s (turn them into 0 s ), not changing the rest of the entries | $\mathrm{A}=(\mathrm{A} \&(\operatorname{rand}(\mathrm{~L})<1-\mathrm{p}))^{1}$; | $\begin{aligned} & \mathrm{A}=\left(\mathrm{A} \&\left(\text { matrix (runif }\left(\mathrm{L}^{\wedge} 2\right), \mathrm{L}\right)\right. \\ & <1-\mathrm{p})) * 1 \end{aligned}$ |
| 319 | Do "wraparound" on a coordinate newx that you've already calculated. You can replace newx with $\mathbf{x}+\mathbf{d x}$ if you want to do wraparound on an offset $x$ coordinate. | $\bmod ($ newx $-1, L)+1$ Note: for portability with other languages such as C which handle MOD of negative values differently, you may want to get in the habit of instead doing $\bmod ($ newx $-1+L, L)+1$ | ((newx-1) \%\% L) + 1 Note: for portability with other languages such as C which handle MOD of negative values differently, you may want to get in the habit of instead doing $(($ newx $-1+\mathrm{L}) \% \% \mathrm{~L})+1$ |
| 320 | Randomly initialize a portion of an array: set fraction $p$ of sites in rows iy1 through iy2 and columns ix1 through ix2 equal to 1 (and set the rest of the sites in that block equal to zero). Note: this assume iy1 < iy2 and ix1 < ix2. | $\begin{aligned} & \text { dx=ix2-ix1+1; dy=iy2-iy1+1; } \\ & \text { A(iy1:iy2,ix1:ix2) = } . . \\ & (r a n d(d y, d x)<p 0) * 1 ; \end{aligned}$ | $\begin{aligned} & \text { dx=ix2-ix1+1; dy=iy2-iy1+1; } \\ & \text { A[iy1:iy2,ix1:ix2] = } \\ & \text { (matrix(runif(dy*dx), dy) < } \\ & \text { p0) } * 1 \end{aligned}$ |

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