



# *Overlay (and P2P) Networks*

Part II

- Complex Networks
- Applications of Overlay networks
- Advanced Topics
- Summary

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# Schedule

- Complex Networks 11.02
- Complex Networks 15.02
- Complex Net & Apps 18.02
- Applications 22.02
- Advanced Topics 25.02
- Conclusion Summary 29.02

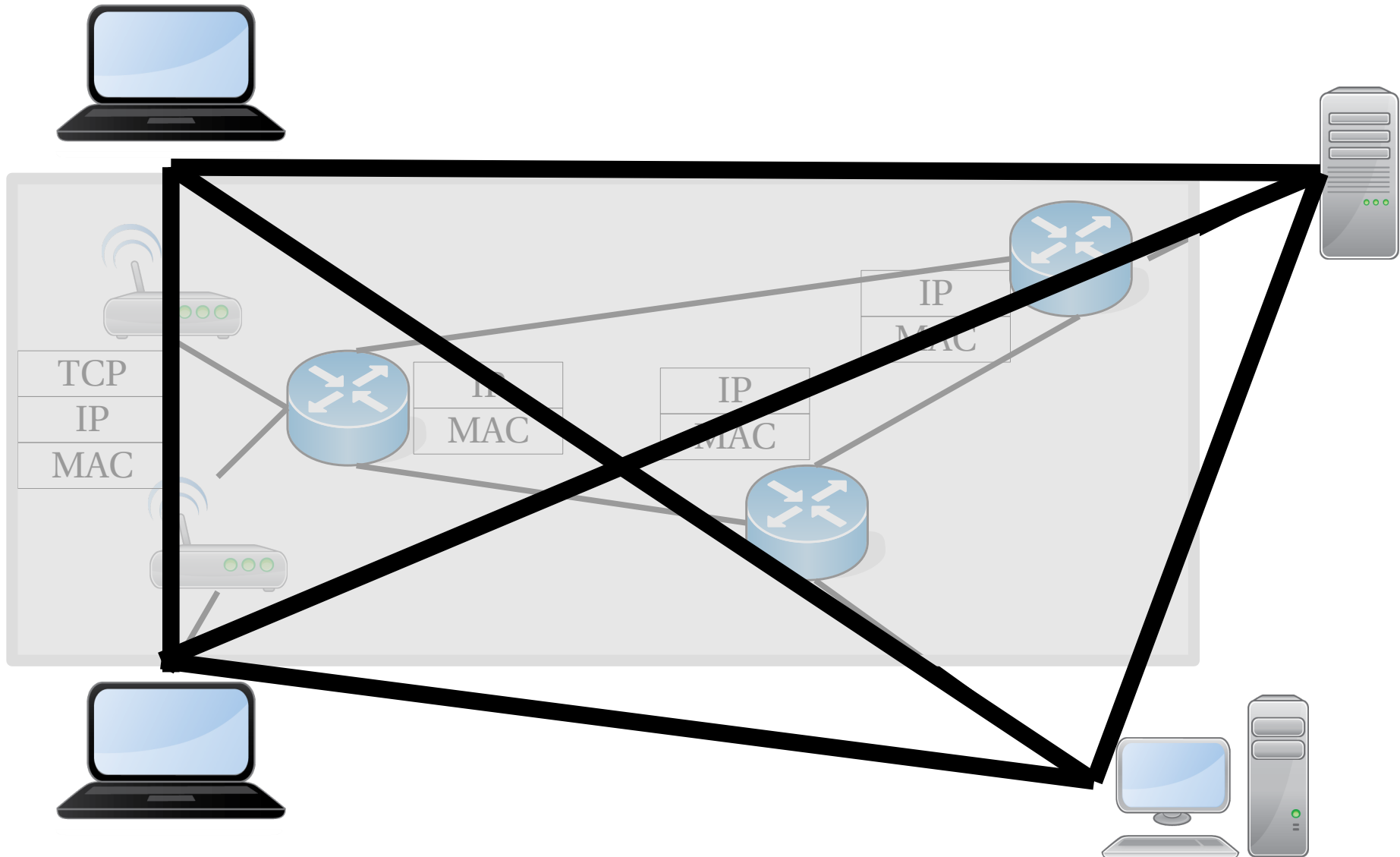
- Why Complex Networks?
- Scale Free & Small World
- Zipf's law
- Power Law
- Search in Small World

- Internet Indirection  
Infrastructure (I3)
- Content Delivery Networks
- Dynamo
- SDN and Clouds

Any suggestions for advanced topics?

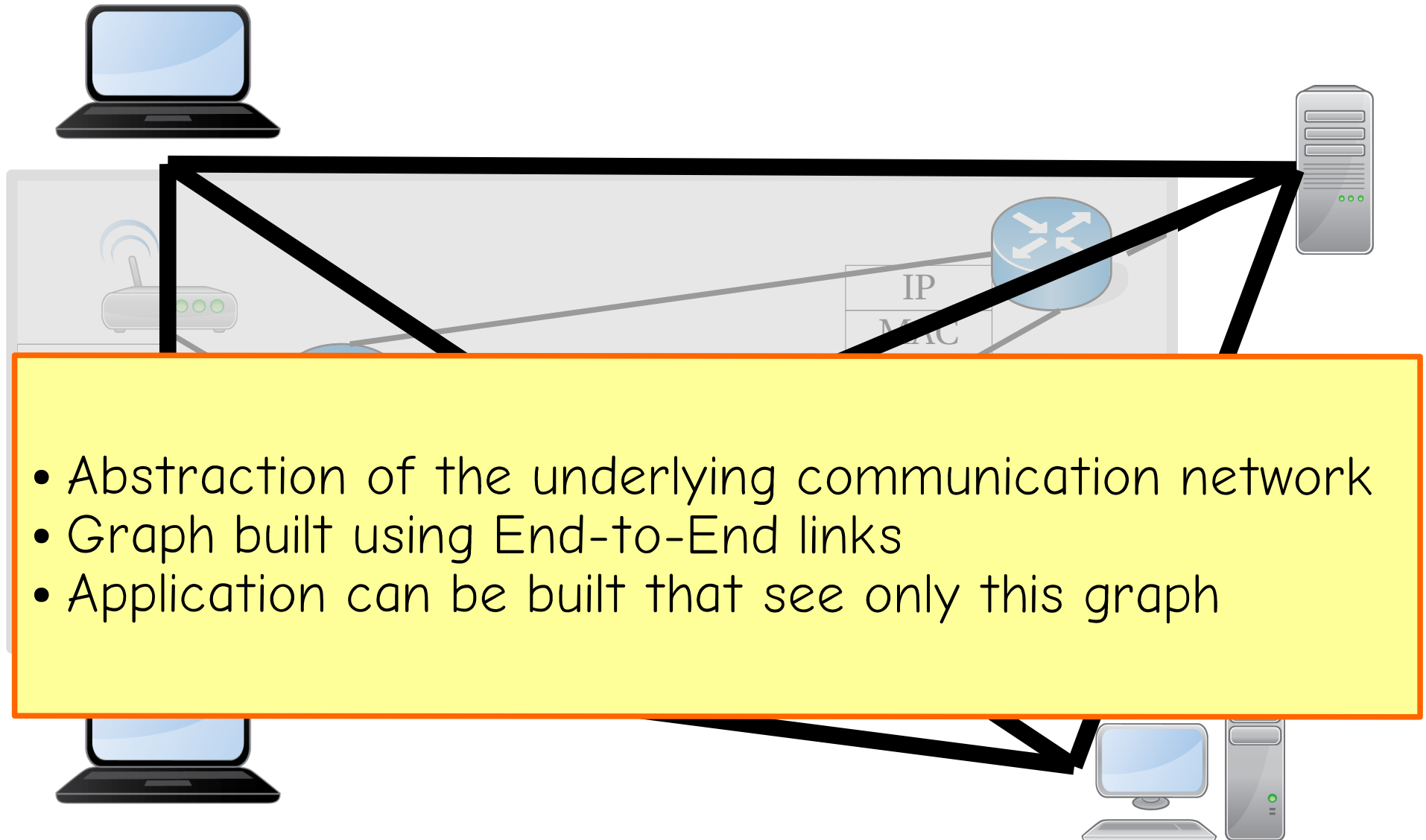


# 1) Hop-by-Hop -> Overlay





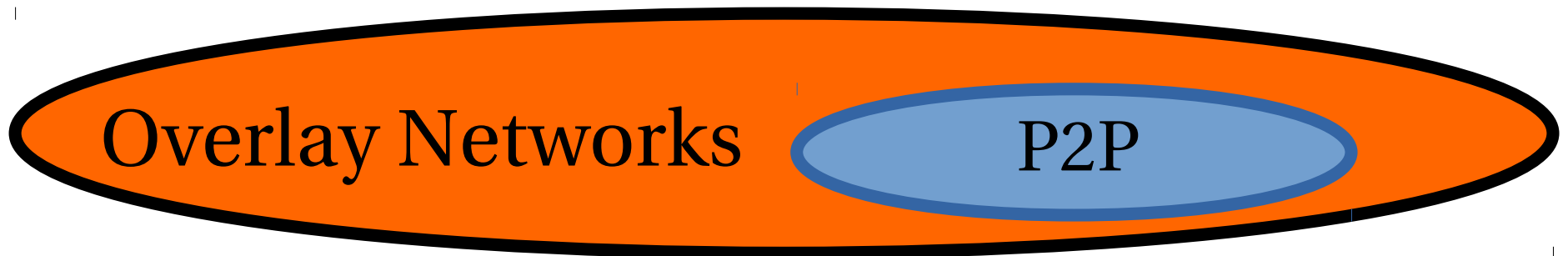
# 1) Hop-by-Hop -> Overlay





## 2) Peer-to-Peer

- Overlays (End-to-End Systems)
- **Peer-to-Peer: example of an overlay system**
- Peer
  - An **End** in an End-to-End system
    - All peers are "end-systems", but all "end-systems" are not peers
  - A computer, an end-user, an application depending on the context



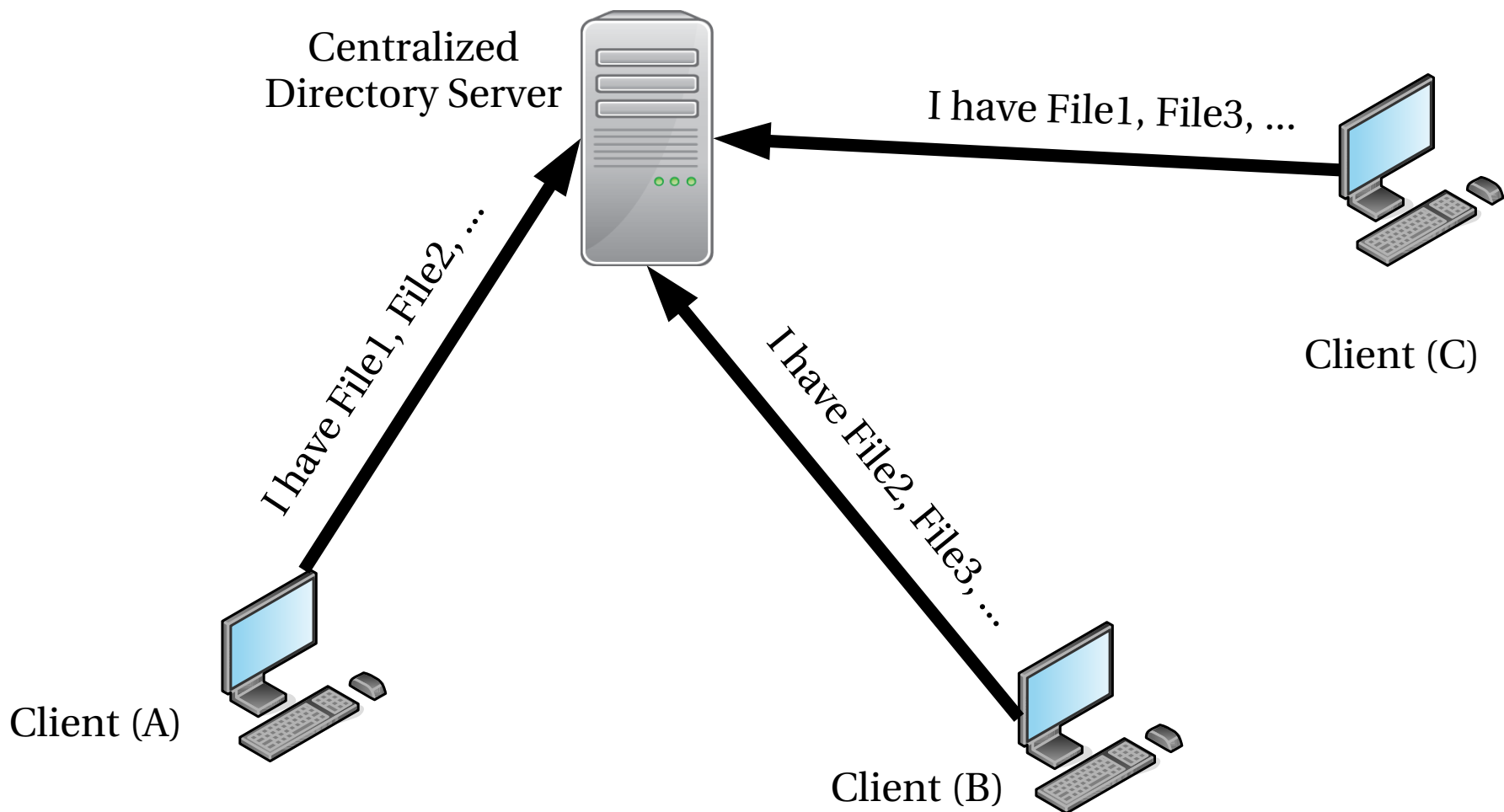


# 3) Unstructured Networks

- Flat or hierarchical organization
  - Napster
  - Gnutella
  - Skype
  - BitTorrent
  - Freenet

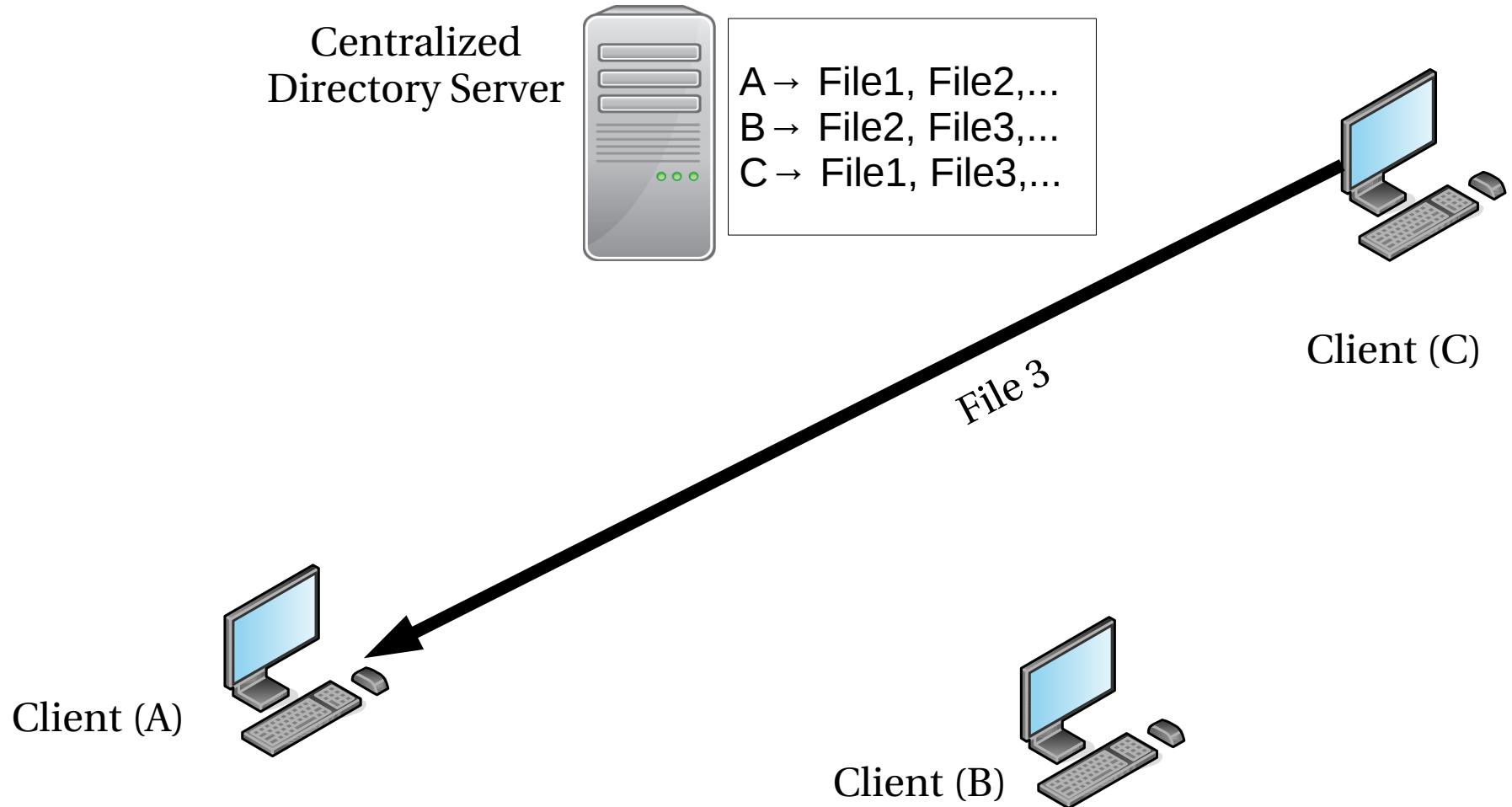


# Napster (simple file sharing)





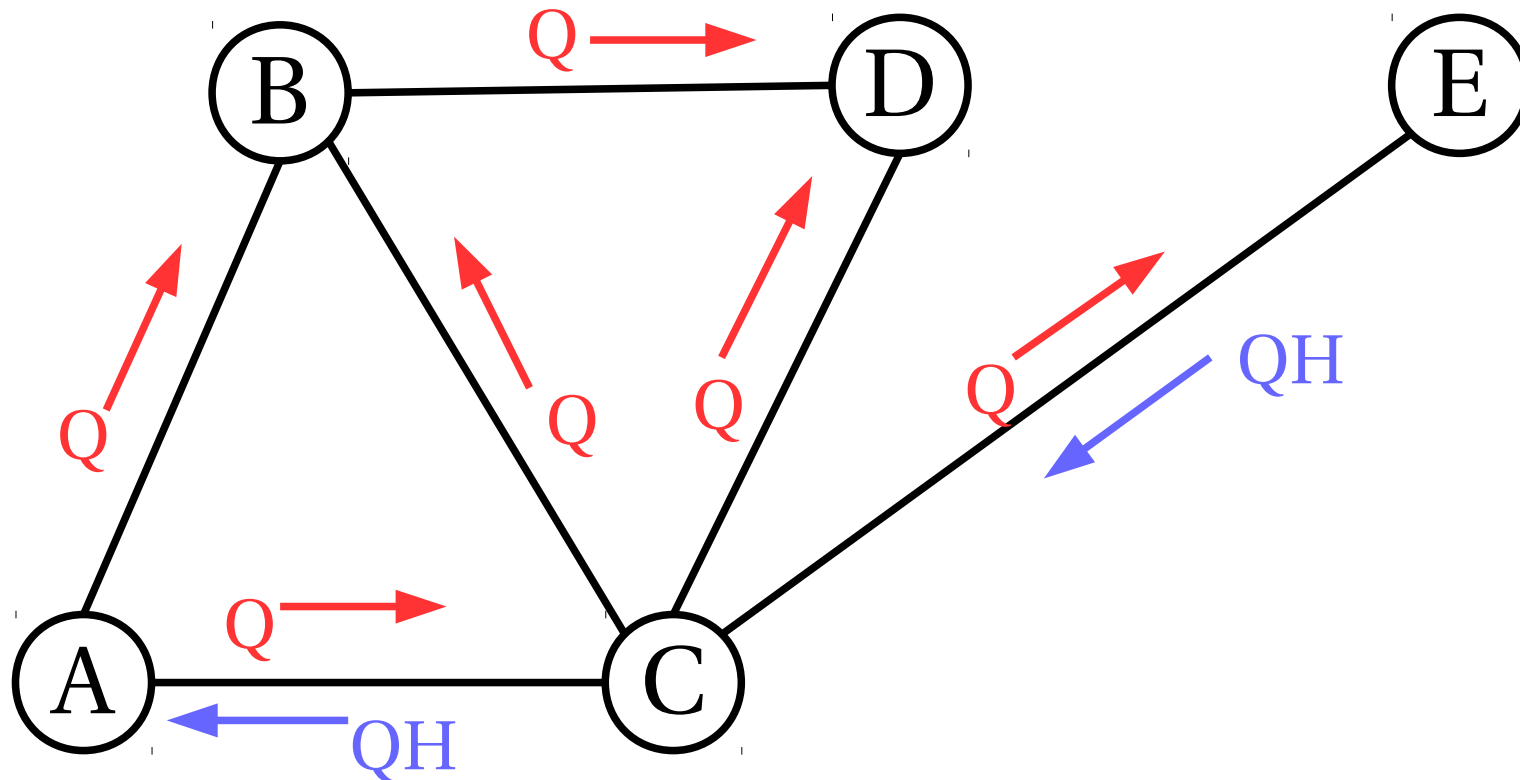
# Napster (simple file sharing)





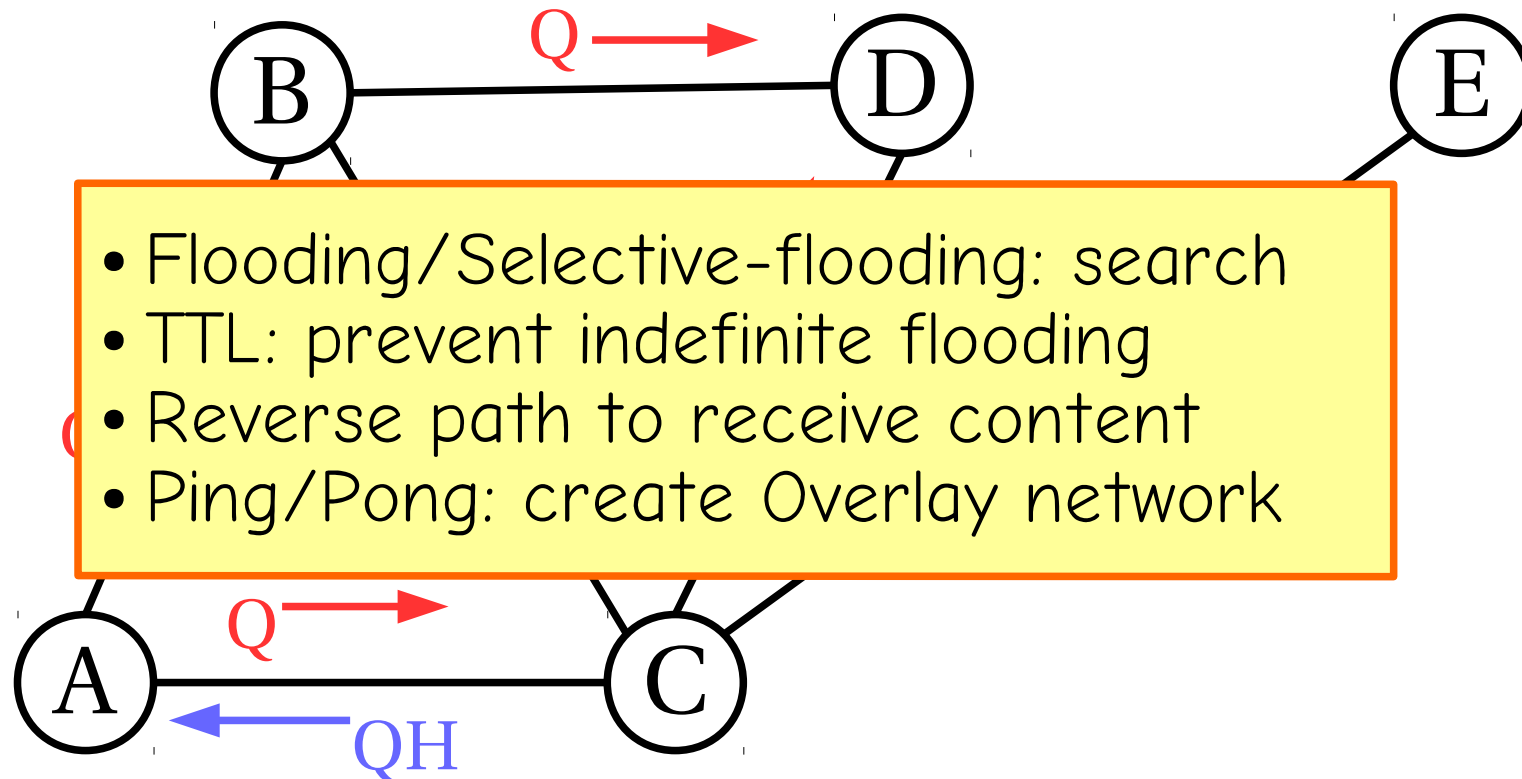


# Gnutella (file sharing-old version)





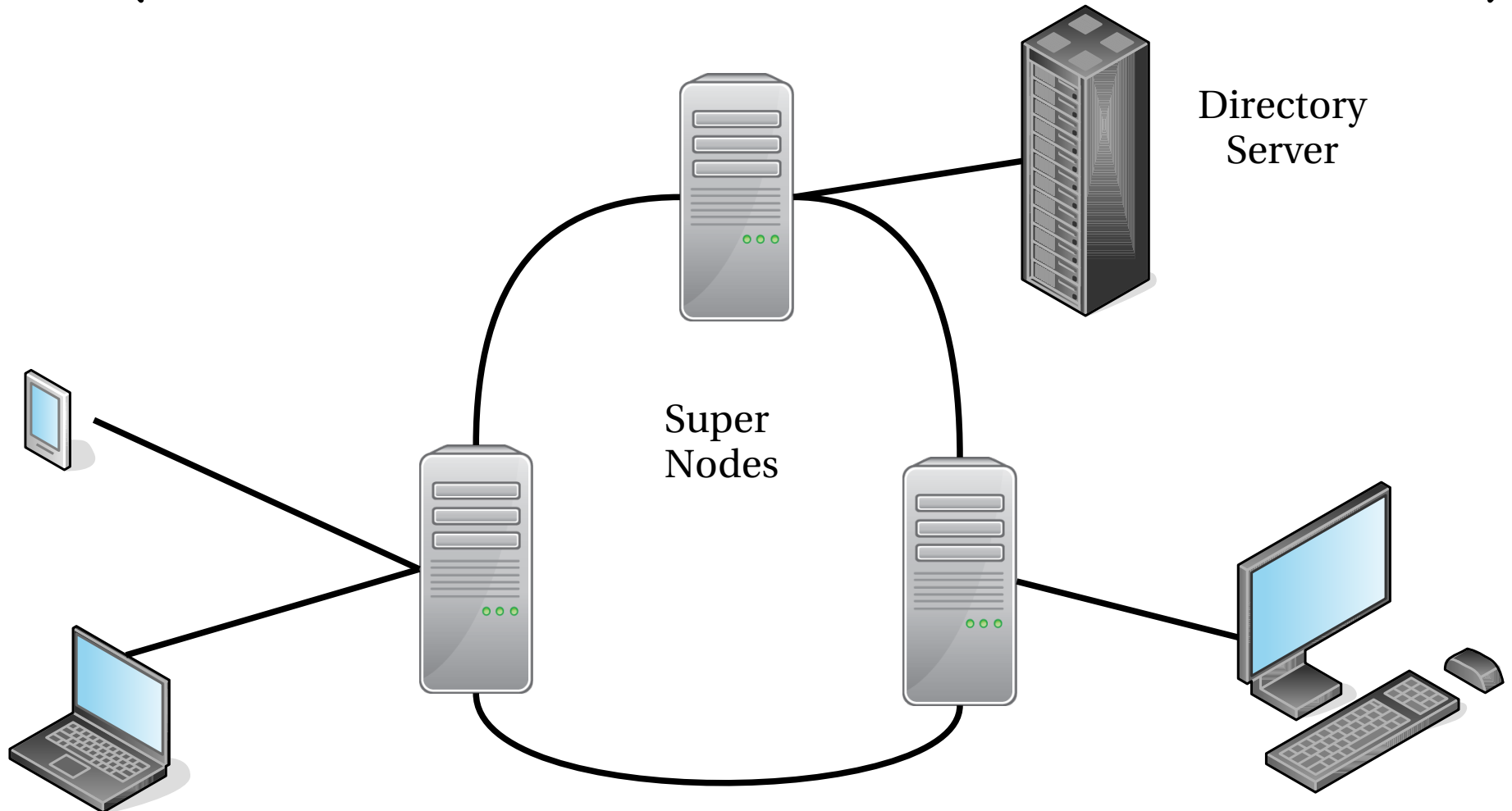
# Gnutella (file sharing-old version)





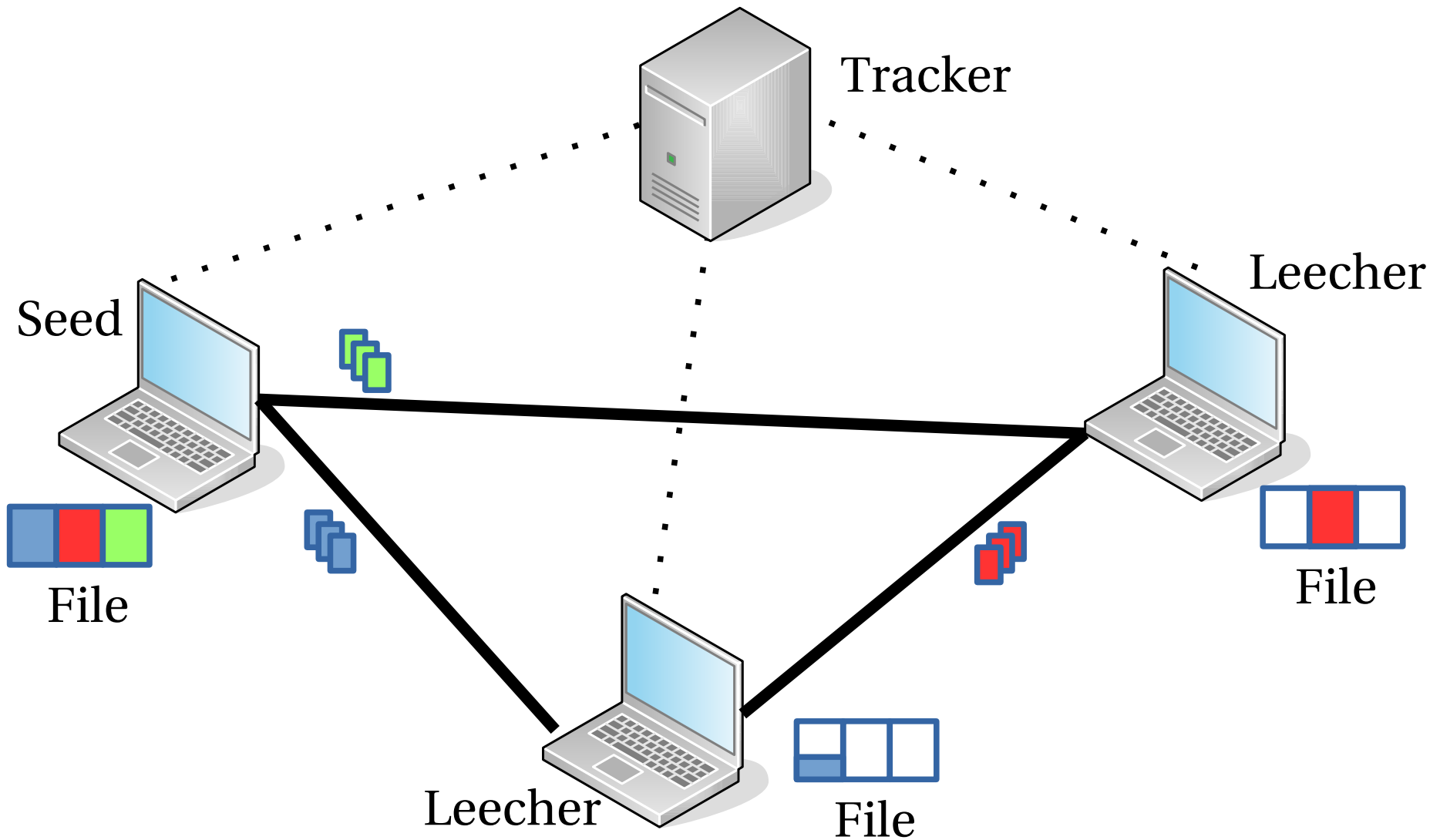
# Skype

(P2P voice/video communication)





# BitTorrent (P2P content dissemination)





# Freenet

- Self-organizing and Self-contained P2P network
- Collaborative (distributed) virtual file system
- Strong anonymity and censorship resistance



# More Resources

- Video: Freenet at C3 Conference:
- B. Cohen.  
Incentives for building robustness in BitTorrent
- Stefan Saroiu, Krishna Gummadi, and Steven Gribble.  
"A Measurement Study of Peer-to-Peer File Sharing Systems."



# Properties of Unstructured Overlay Networks

- Unstructured Link Creation
- Random Arrivals and Churn
- Flat or Hierarchical organization
- and many more ...

Which graph abstracts unstructured  
(and other) overlay networks?



# Why is modeling important?

- What is the expected latency to the peek the content?
  - Average distance between nodes
- What is the impact of a peer leaving the network?
  - Robustness to faults/down-times
- What are the factors that determine the evolution of the graph structure?
  - Impact of proposed optimizations such as localization of content
- ...





# Small World

- Stanley Milgram. "**The small world problem.**" *Psychology today* 2.1 (1967): 60-67
  - "Given any two persons in the world, person X and person Z, how many intermediate acquaintance links are needed before X and Z are connected?"
- Mathematical structure of society



# Milgrams Approach

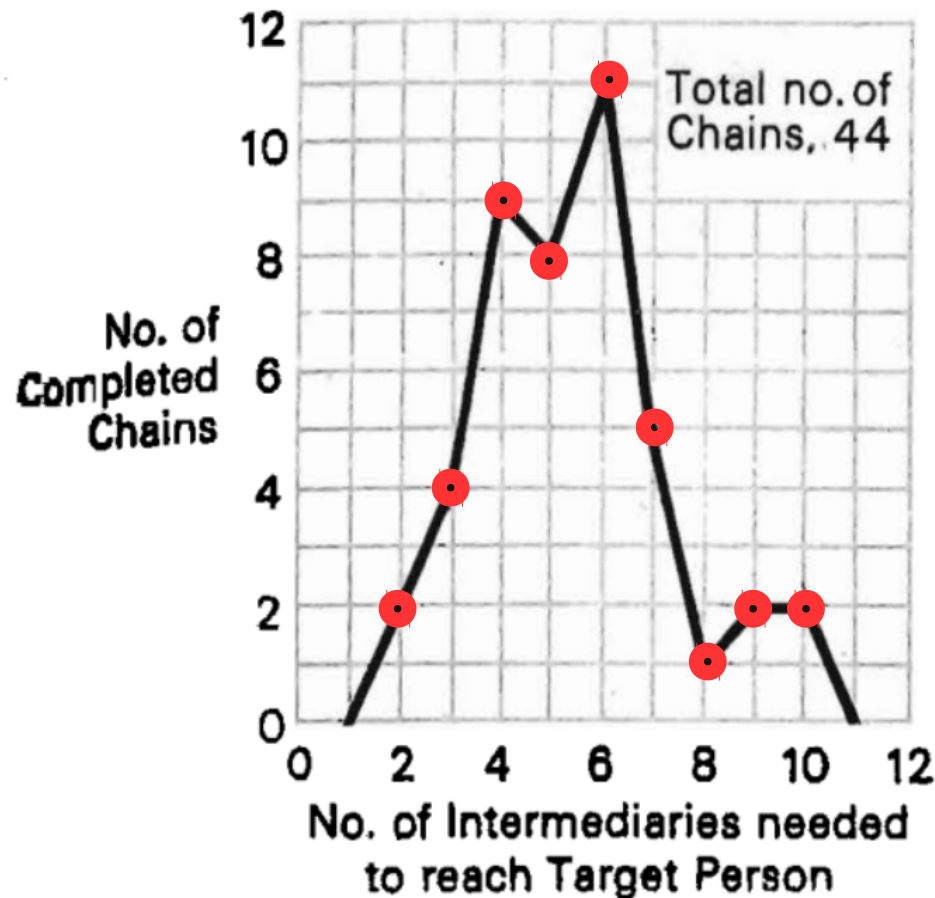
A random person  $X$  was selected and given a document.

The document contained

- (1) The name of person  $Z$  and some information such as profession and city name
- (2) If  $X$  did not know person  $Z$  then  $X$  mails it to a person  $Y$  whom  $X$  knows on a first name basis and who is more likely than  $X$  to know  $Z$ . ( $Y$  is the new  $X$ )
- (3) A roster on which each person to whom document arrives writes his/her name. Roster also prevents endless looping.



# Key Result



Stanley Milgram. "The small world problem." *Psychology today* 2.1 (1967): 60-67

- Median: 5 intermediaries
  - How many degrees of separation?
- Decay in active chains
  - 126 of 160 chains dropped out!
- Common pathway
  - Stock broker, clothing merchant
- Misc
  - Role of gender, ethnicity
- ***When will two sub-populations be isolated from each other?***



# Key Result

Average diameter?

- Median: 5 intermediaries
  - How many degrees of separation?

Churn, failures?

- Decay in active chains
  - 126 of 160 chains dropped out!

Hubs, Super-nodes?

- Common pathway
  - Stock broker, clothing merchant

Device Heterogeneity?

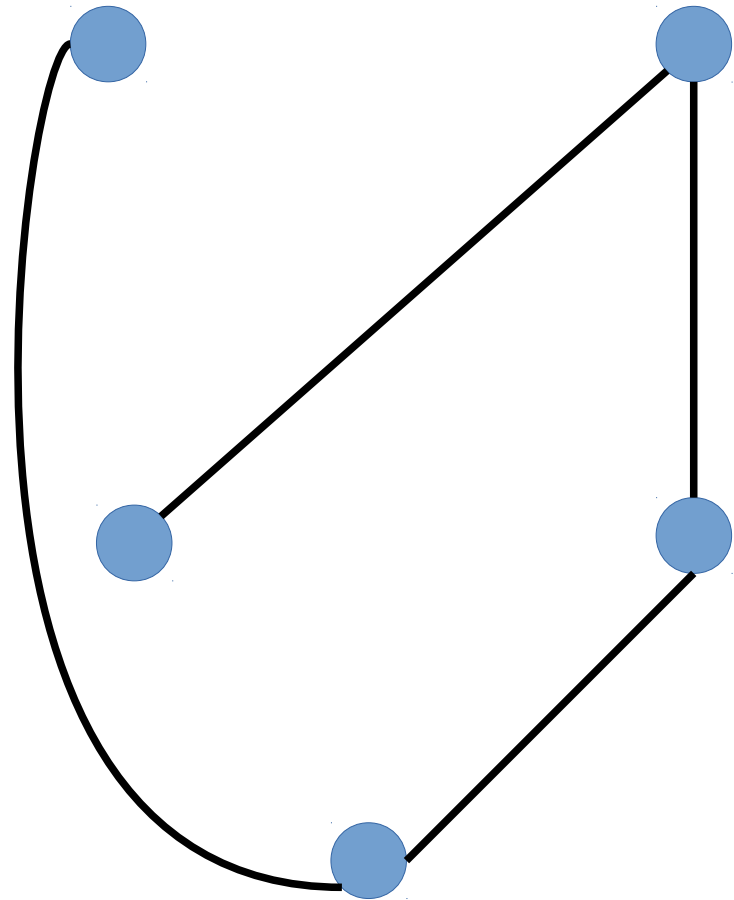
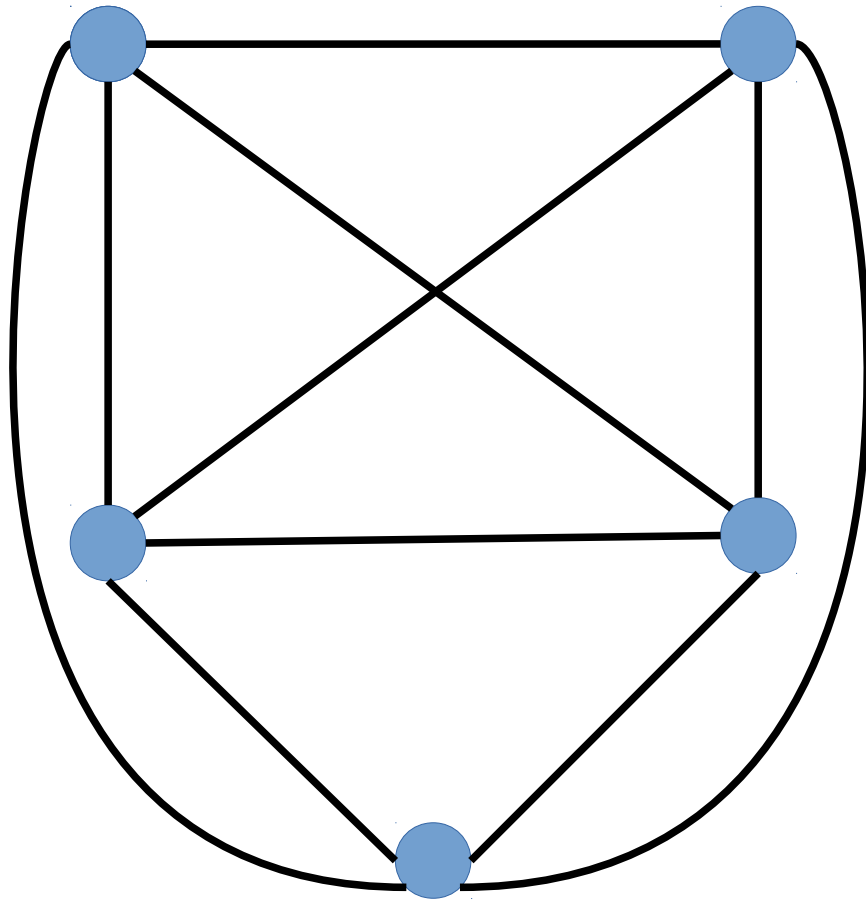
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  - Role of gender, ethnicity

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# Random Graph (Erdős–Rényi) / Gilbert Model

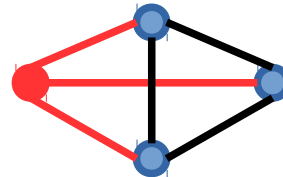


Small diameter but not robust  
to link/node failures?



# Modeling the "Small World"

- Duncan Watts and Steven H. Strogatz. "Collective dynamics of 'small-world' networks." *Nature* 393.6684 (1998): 440-442.
  - Diameter: length of the longest path
  - Clustering Coefficient: how close are the adjacent vertices of a vertex to a complete graph (clique) if the vertex is removed.
  - Desirable properties: Small Diameter and High Clustering Coefficient

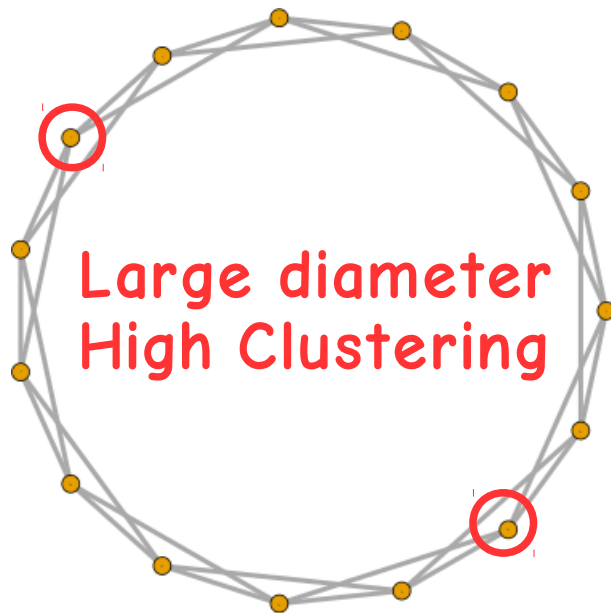




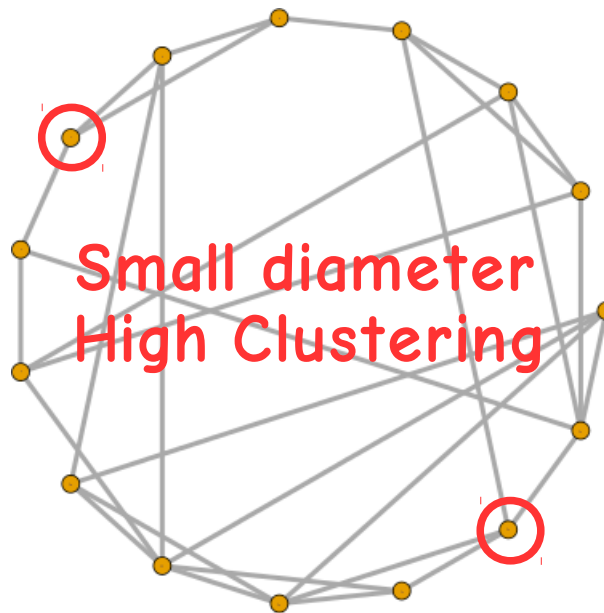
# Random Rewiring Procedure

$n=10, k=4$

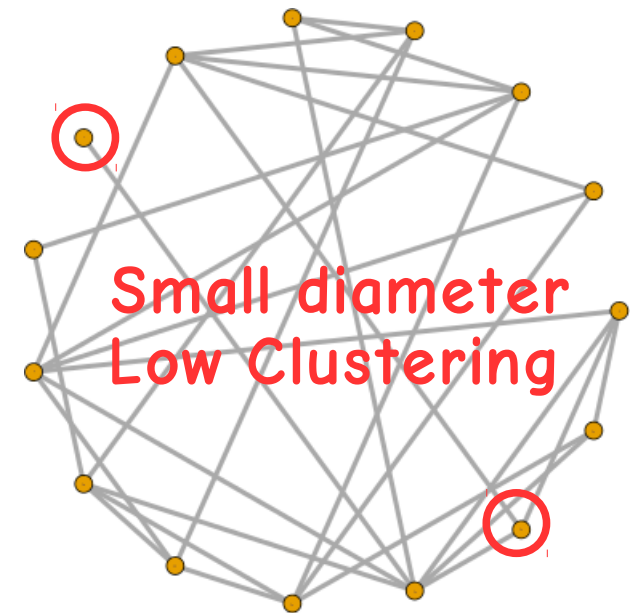
What is the diameter?  
What happens if I remove a neighbour?



$p=0$



$(p=0.15)$



$p=1$

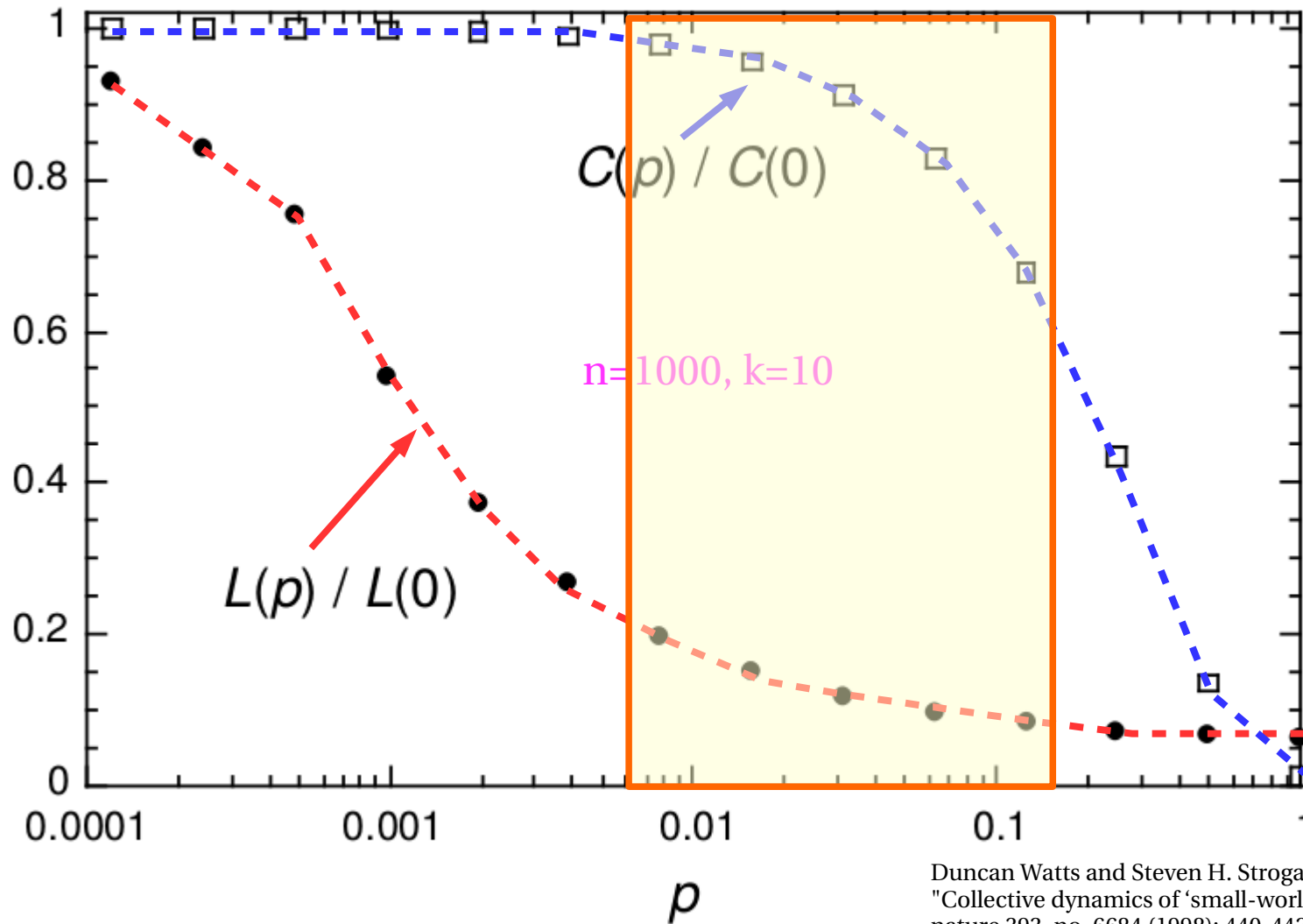
$n$ : number of vertices

$k$ : degree of each node, i.e., neighbours of a vertex ( $n \gg k \gg \ln(n) \gg 1$ )

$p$ : probability of rewiring



# Path Length $L(\cdot)$ and Clustering Coefficient $C(\cdot)$ in Rewired Graphs



Duncan Watts and Steven H. Strogatz.  
"Collective dynamics of 'small-world' networks."  
nature 393, no. 6684 (1998): 440-442.





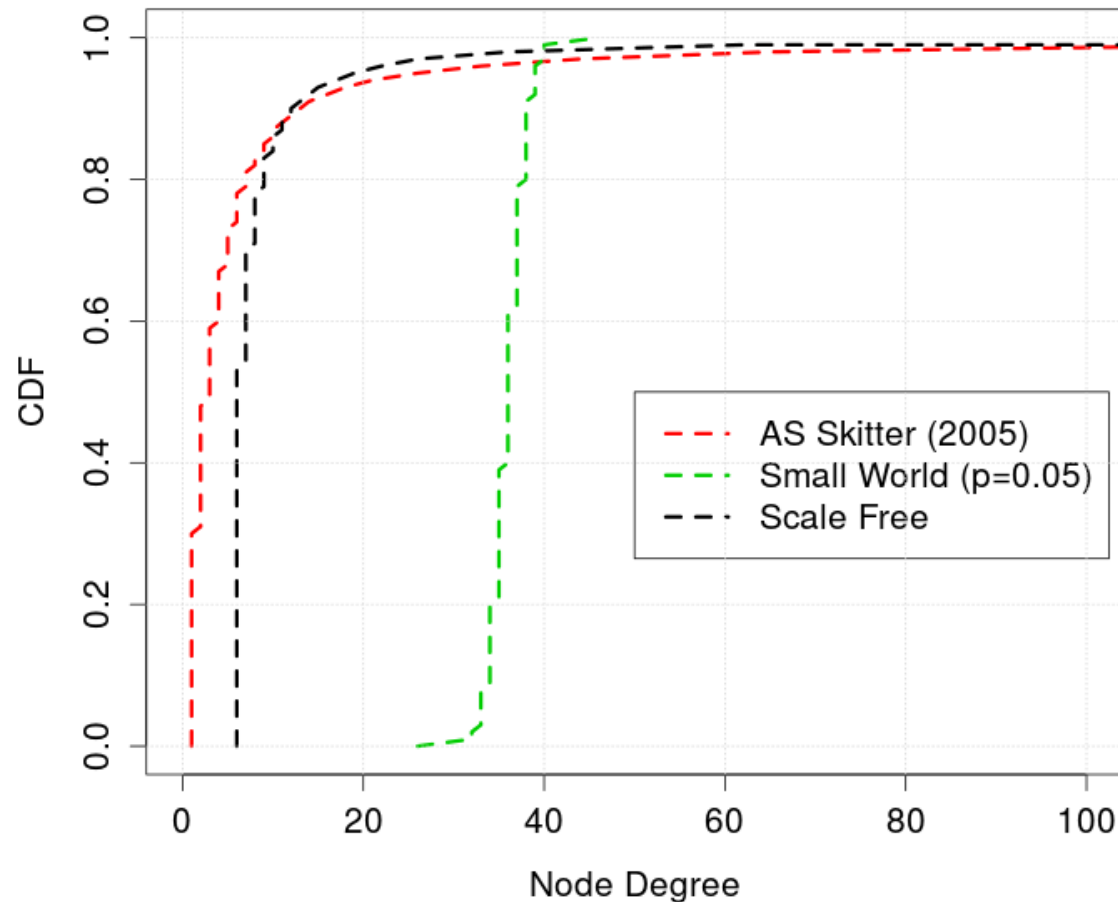
# Is Small-World Networks the right model?

- What happens in dynamic networks whose members/vertices change with time?
- With which vertices of a graph do new arrivals prefer to attach?
- Is the the development of large networks governed by a robust self-organizing phenomena?
- What about heterogeniety in type of elements in and the degree distribution?
- ...



# What about degree distribution?

- Do small-world/random-graph models capture the presence of hubs?





# Assumptions of Random Graphs and Small-World

- Fixed number of nodes that are either randomly connected (Random Graphs) or randomly rewired (Small-World)
- Probability that two vertices are connected is random and uniform

Barabási, Albert-László, and Réka Albert.  
"Emergence of scaling in random networks."  
Science 286, no. 5439 (1999): 509-512.



# Scale Free Networks

- Probability that a node has  $k$  links is  $P(k) \propto k^{-\gamma}$
- $\gamma$  exponent for the degree distribution
- Why the name Scale-Free?

$$P(x) \propto x^{-\gamma}$$

$$P(ax) \propto a^{-\gamma} P(x)$$

- Same functional form across all scales
  - e.g.  $\gamma = 1 \rightarrow P(x) = 1/x$
  - -  $\gamma$  is the slope on log log scale



# Preferential Attachment (Growth in Scale-Free Network)

- Initial number of nodes  $m_0$
- At time 't' add a new vertex  $j$  with degree  $m$  ( $< m_0$ )
- The probability that vertex  $j$  creates a link with vertex  $i$  is the probability  $\pi$  which depends on  $k_i$  (the degree of vertex  $i$ )

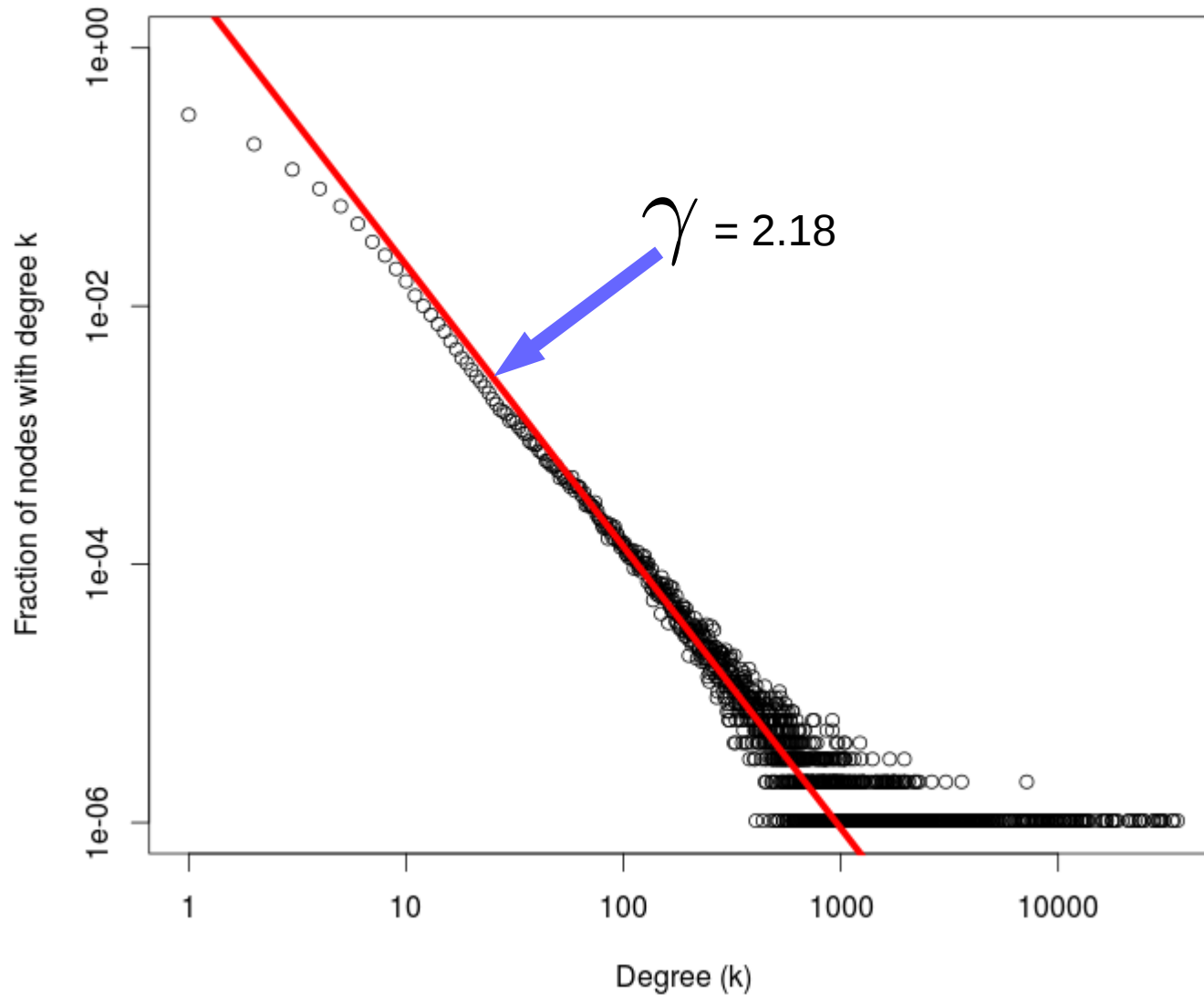
$$\pi(k_i) = \frac{k_i}{\sum_l k_l}$$

- Probability that a node has  $k$  links is  $P(k) \propto k^{-\gamma}$
- $\gamma$  exponent for the degree distribution

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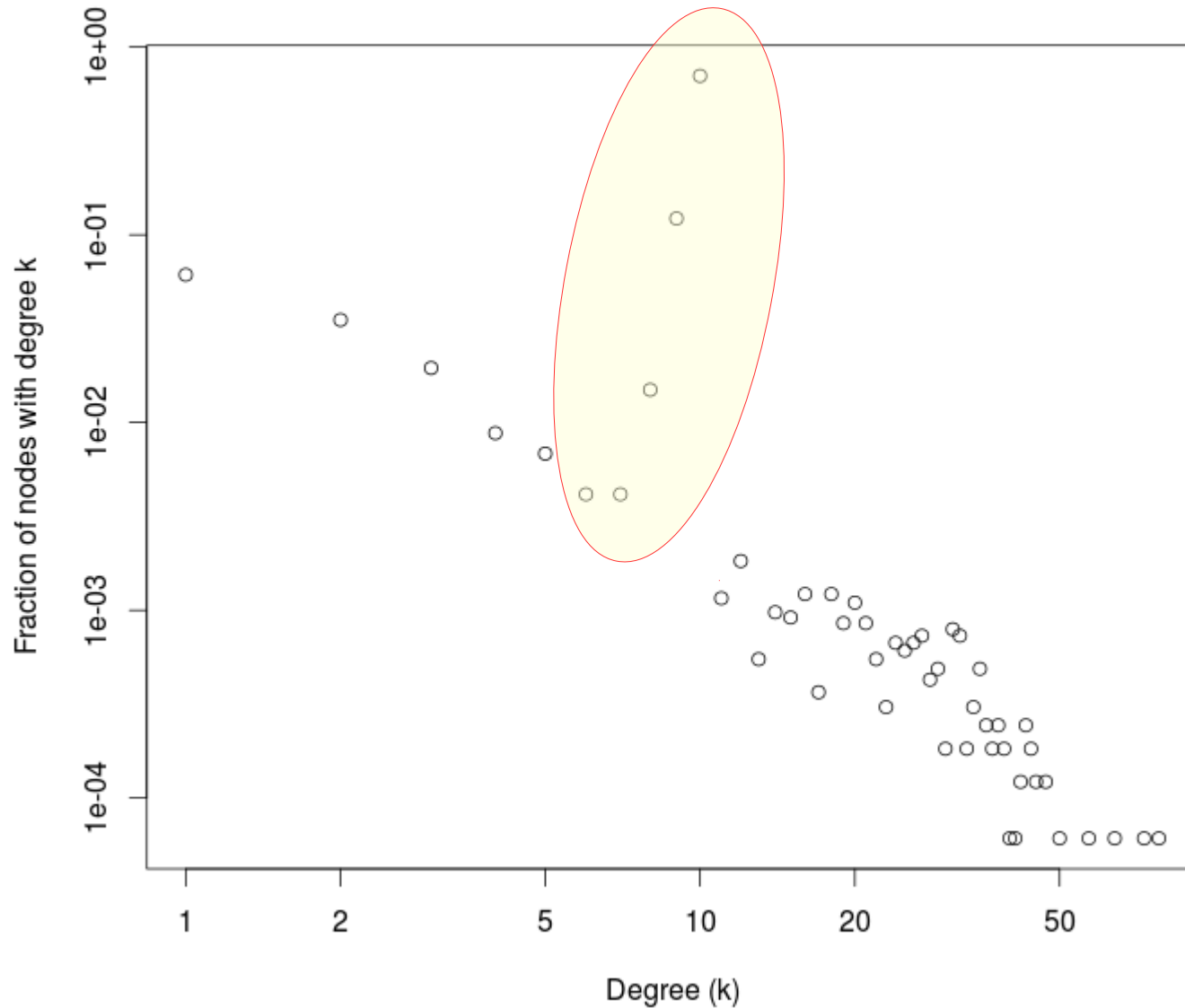


# Scale-Free Model for AS-Graph





# Scale Free for Gnutella?





# Summary

- Large number of interacting elements
- System adapts and evolves
- Although elements follow simple rules, the system behaves in a *complex* manner
- System behavior is an outcome of the interaction between the elements, so studying elements in isolation will not provide detailed insights on system behavior
- Similar processes shape networks therefore many networks share similar characteristics





# Methodology

- 1) Make observations (conduct measurement studies)
- 2) Build model to explain observations
  - Choose the right level of granularity (zoom level)
  - Strip the problem to a simple form
  - Attempt to formulate the problem and model the system
- 3) Validate model
  - Reproduce observations/measurements
  - Explain observations
- 4) Revisit step 2 (and 1) to improve understanding



# Complex Networks

Overlay  
Networks 



# Important Papers

- Stanley Milgram. "**The small world problem.**" *Psychology today* 2.1 (1967): 60-67
- Duncan Watts and Steven H. Strogatz. "**Collective dynamics of 'small-world' networks.**" *Nature* 393.6684 (1998): 440-442.
- Barabási, Albert-László, and Réka Albert. "**Emergence of scaling in random networks.**" *Science* 286, no. 5439 (1999): 509-512.
- Albert, Réka, and Albert-László Barabási. "**Statistical mechanics of complex networks.**" *Reviews of modern physics* 74.1 (2002): 47.
- Mitzenmacher, M. (2004). "**A brief history of generative models for power law and lognormal distributions.**" *Internet mathematics*, 1(2), 226-251.



# Sources for these slides

- Sasu Tarkoma "Overlay and P2P Networks", 2015
- Arnaud Legout. "Peer-to-Peer Applications : From BitTorrent to Privacy", January 2012.
- Jari Saramäki "Introduction to Complex Networks", 2010.
- Datasets from Stanford Network Analysis Project (SNAP)