



Overlay (and P2P) Networks

Part II

- Recap
- Small World
- Random Graphs (Erdős–Rényi model) / Gilbert Model
- Random Rewiring (Duncan Watts Model)

Samu Varjonen

Ashwin Rao



Schedule

- Complex Networks 09.02
- Complex Networks 13.02
- Complex Net & Apps 16.02
- Complex Net & Apps 20.02
- Applications 23.02
- Advanced Topics 27.02
- Conclusion Summary 02.03



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- Why Complex Networks?
- Scale Free & Small World
- Zipf's law
- Power Law
- Search in Small World



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- Internet Indirection
Infrastructure (I3)
- Content Delivery Networks
- Dynamo
- SDN and Clouds



Background/Recap

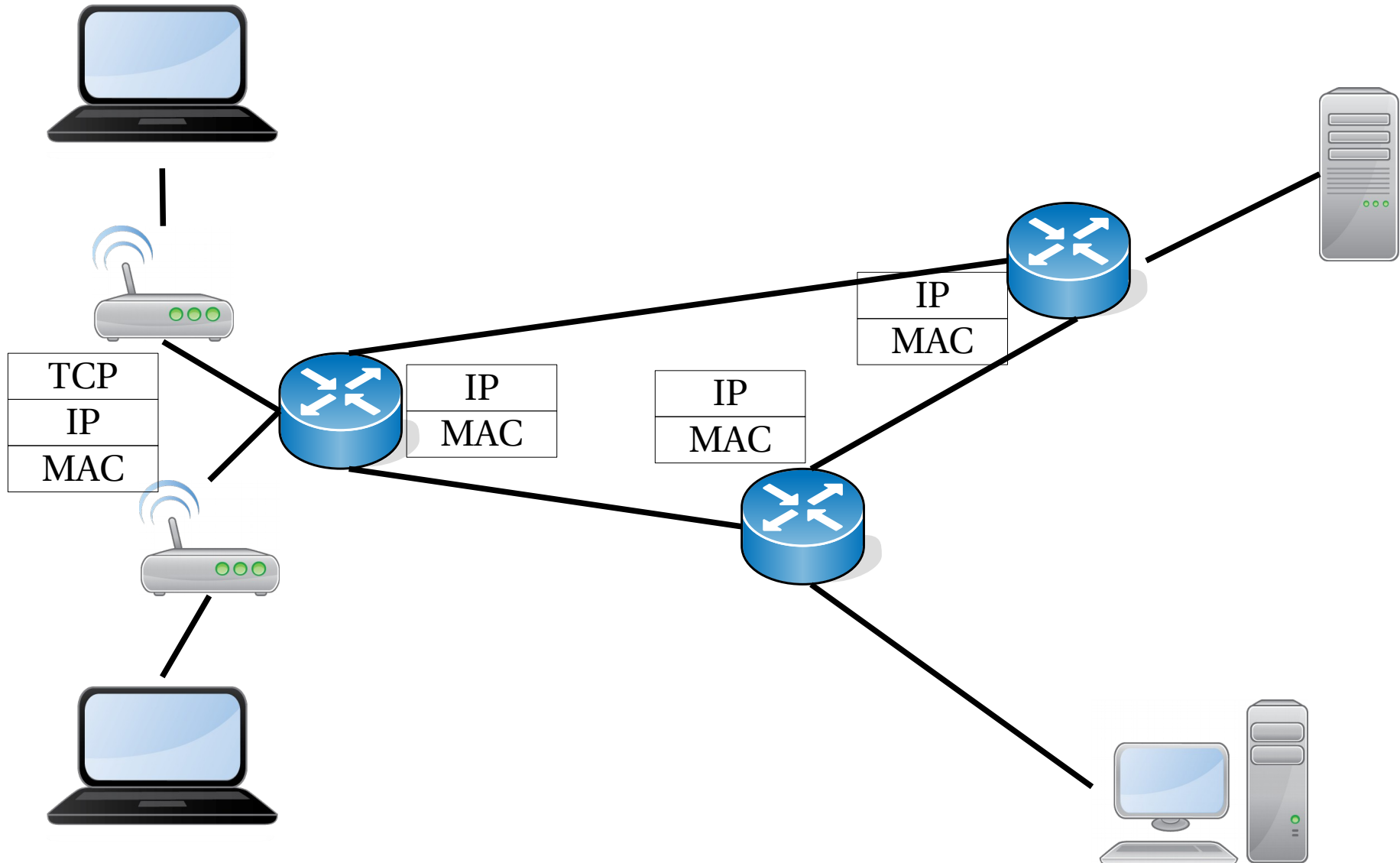


1) Hop-by-Hop -> Overlay



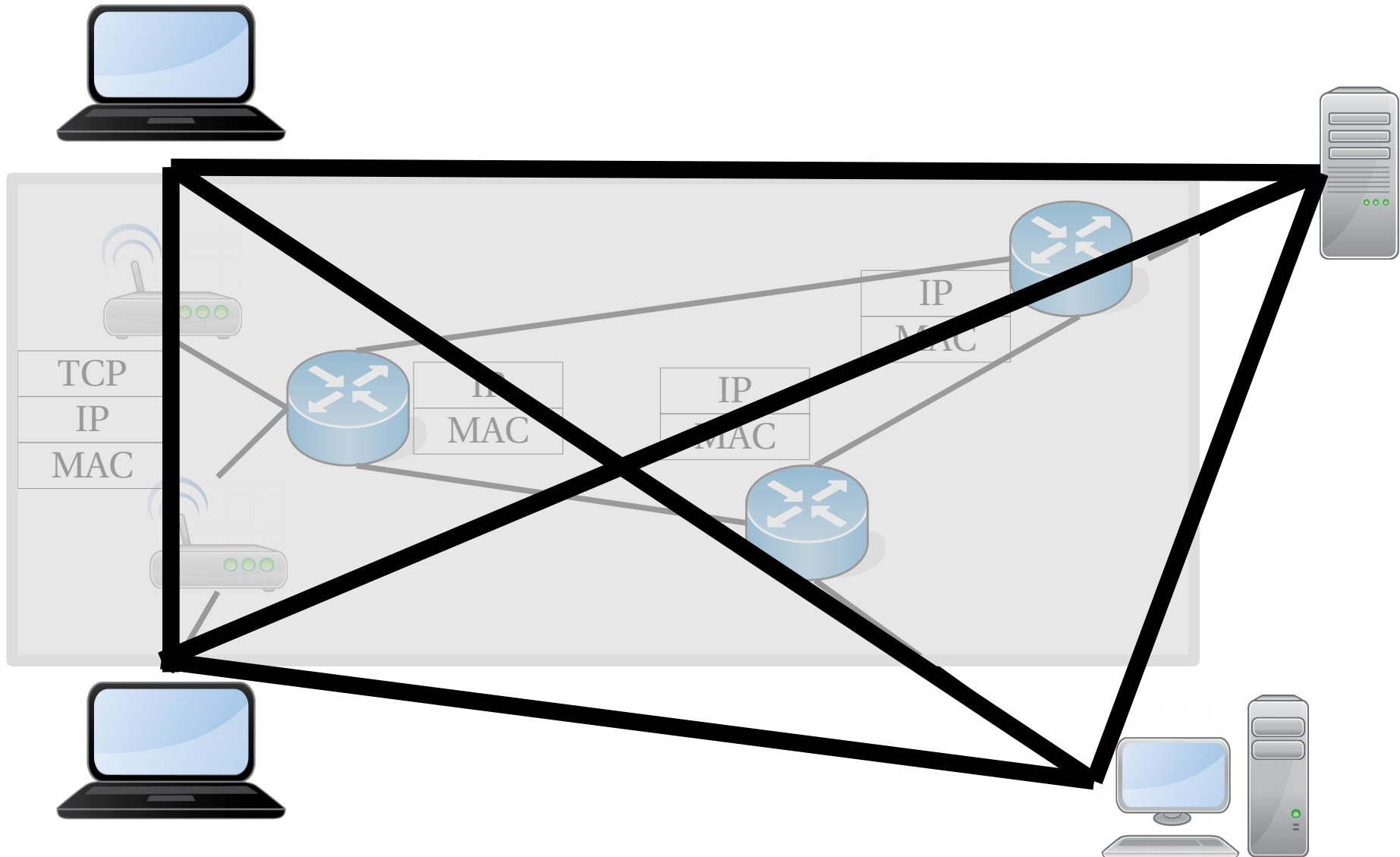


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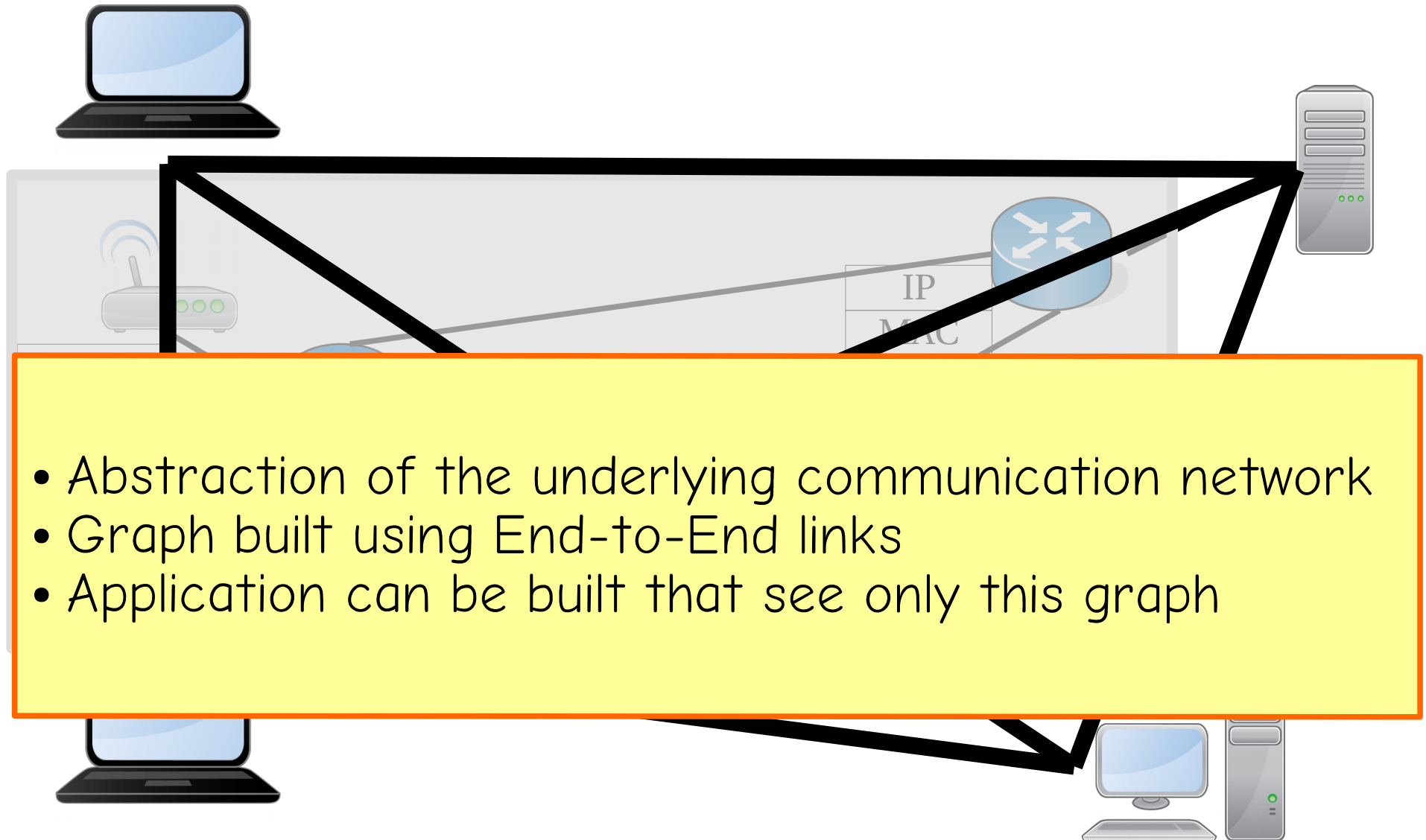


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2) Peer-to-Peer

- Overlays (End-to-End Systems)



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- **Peer-to-Peer: example of an overlay system**



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- Peer



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 - An **End** in an End-to-End system
 - All peers are "end-systems", but all "end-systems" are not peers
 - A computer, an end-user, an application depending on the context



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3) Unstructured Networks

- Flat or hierarchical organization
 - Napster
 - Gnutella
 - BitTorrent
 - Freenet



Napster (simple file sharing)



Napster (simple file sharing)

Centralized
Directory Server



Client (C)



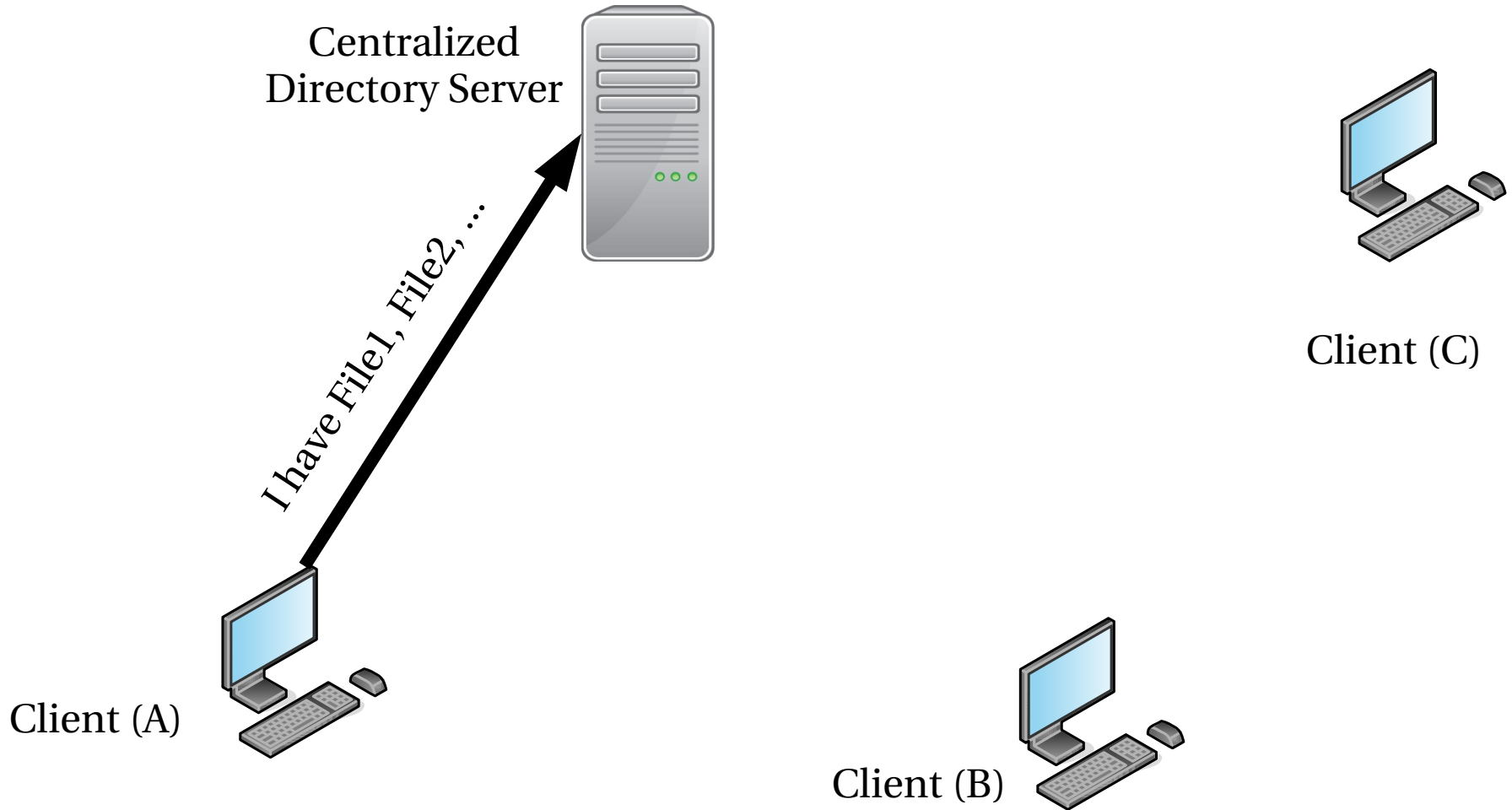
Client (A)



Client (B)

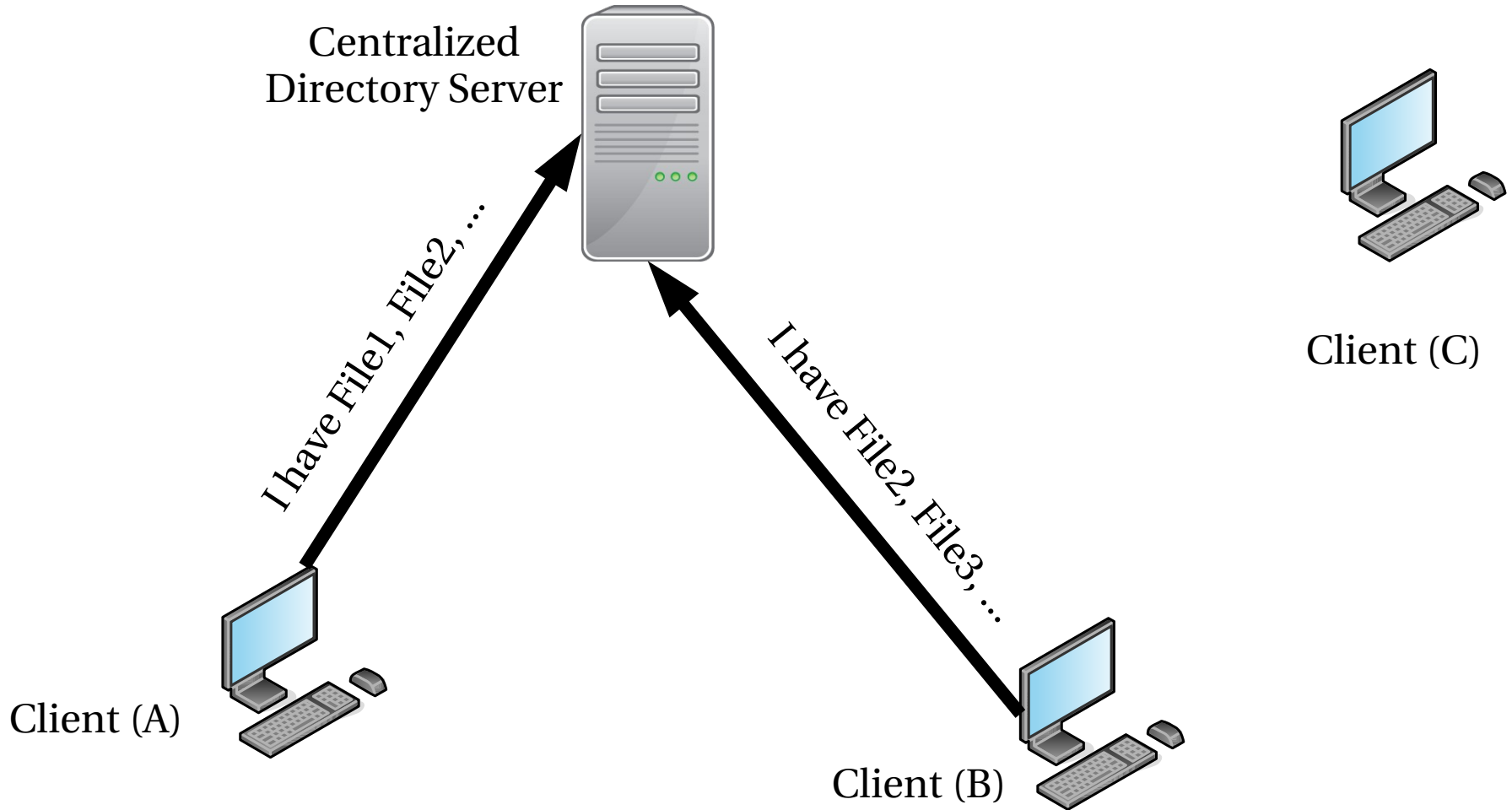


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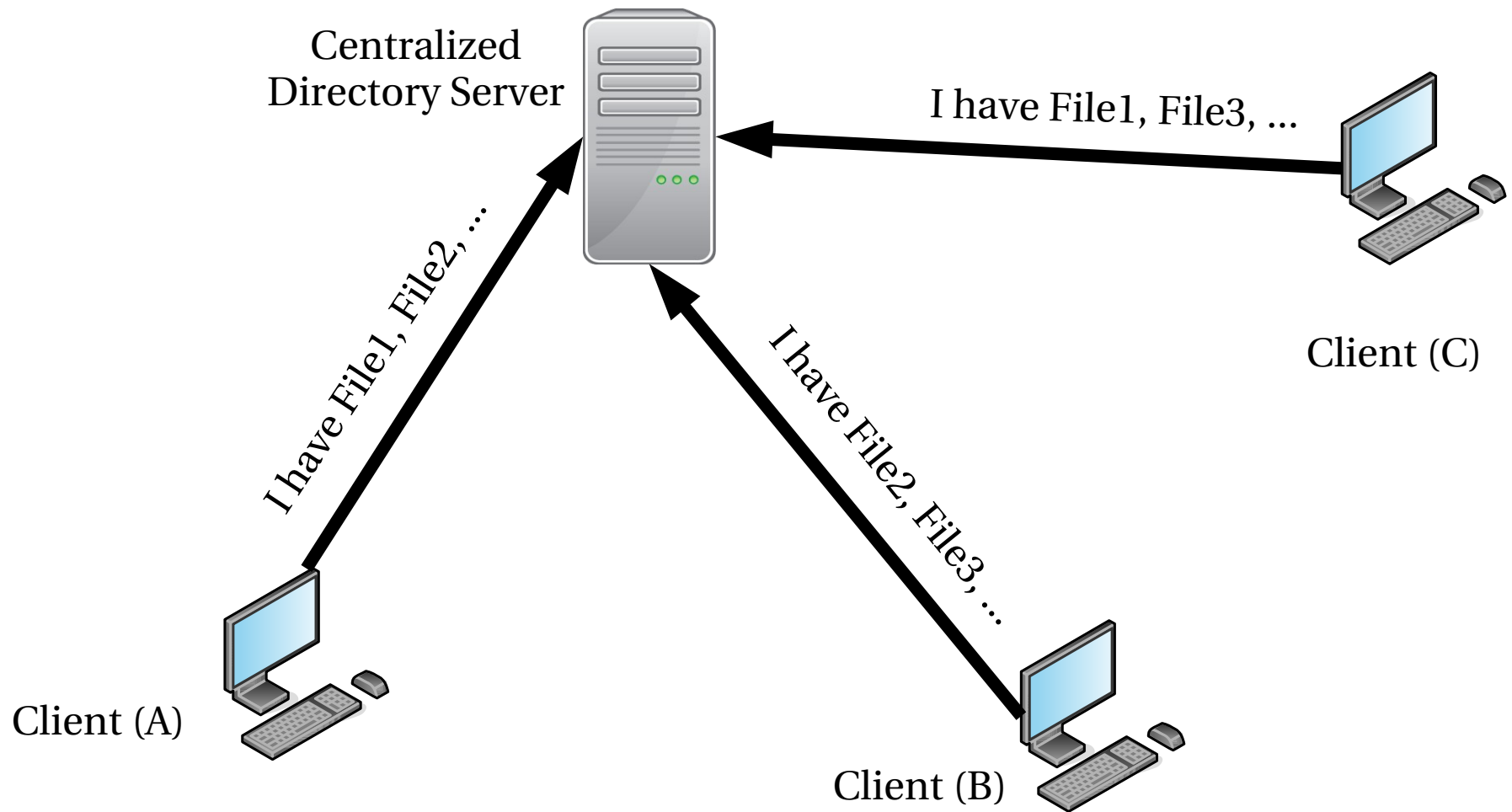


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Centralized
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A → File1, File2, ...
B → File2, File3, ...
C → File1, File3, ...



Client (C)

Client (A)

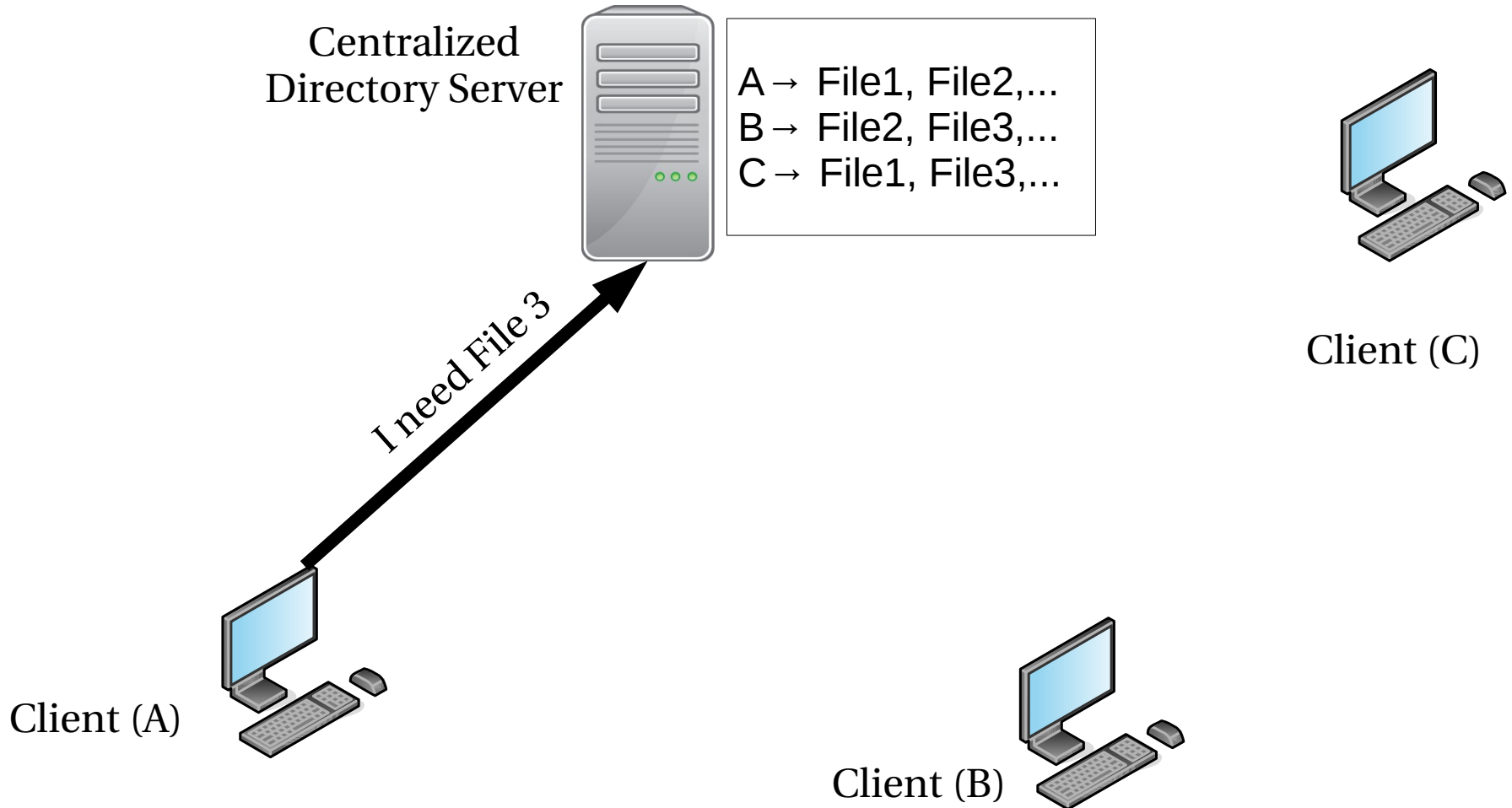


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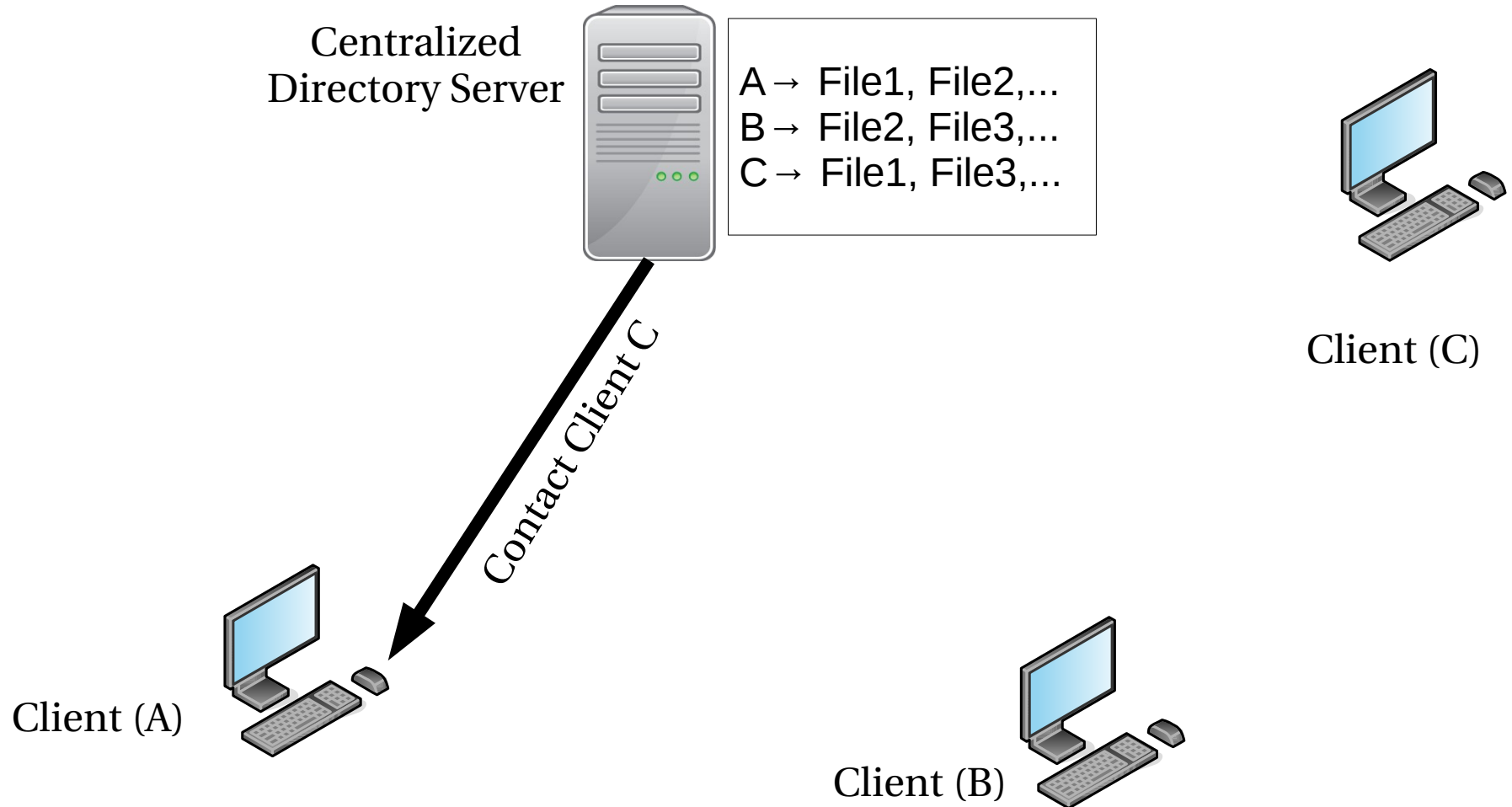


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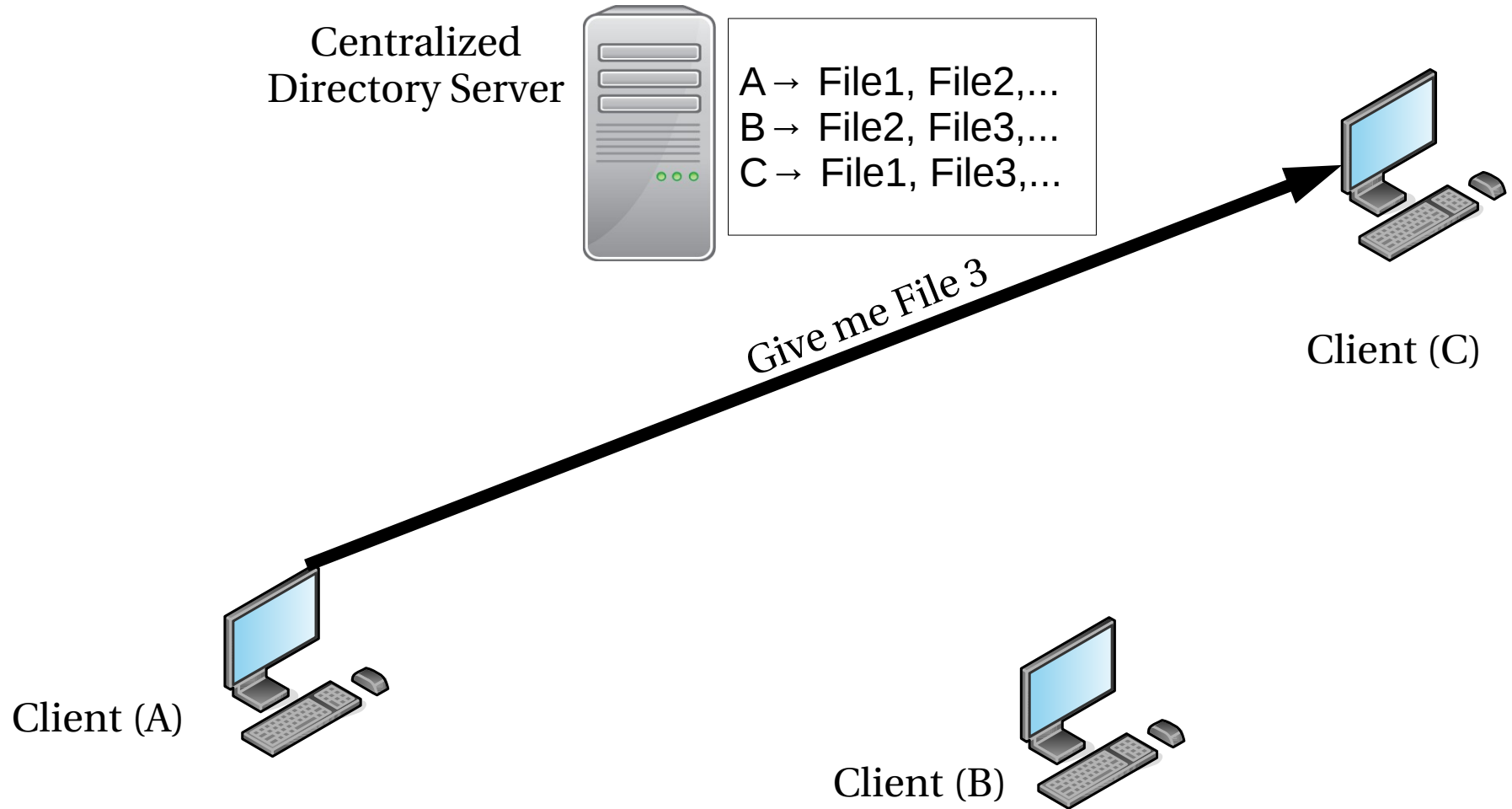


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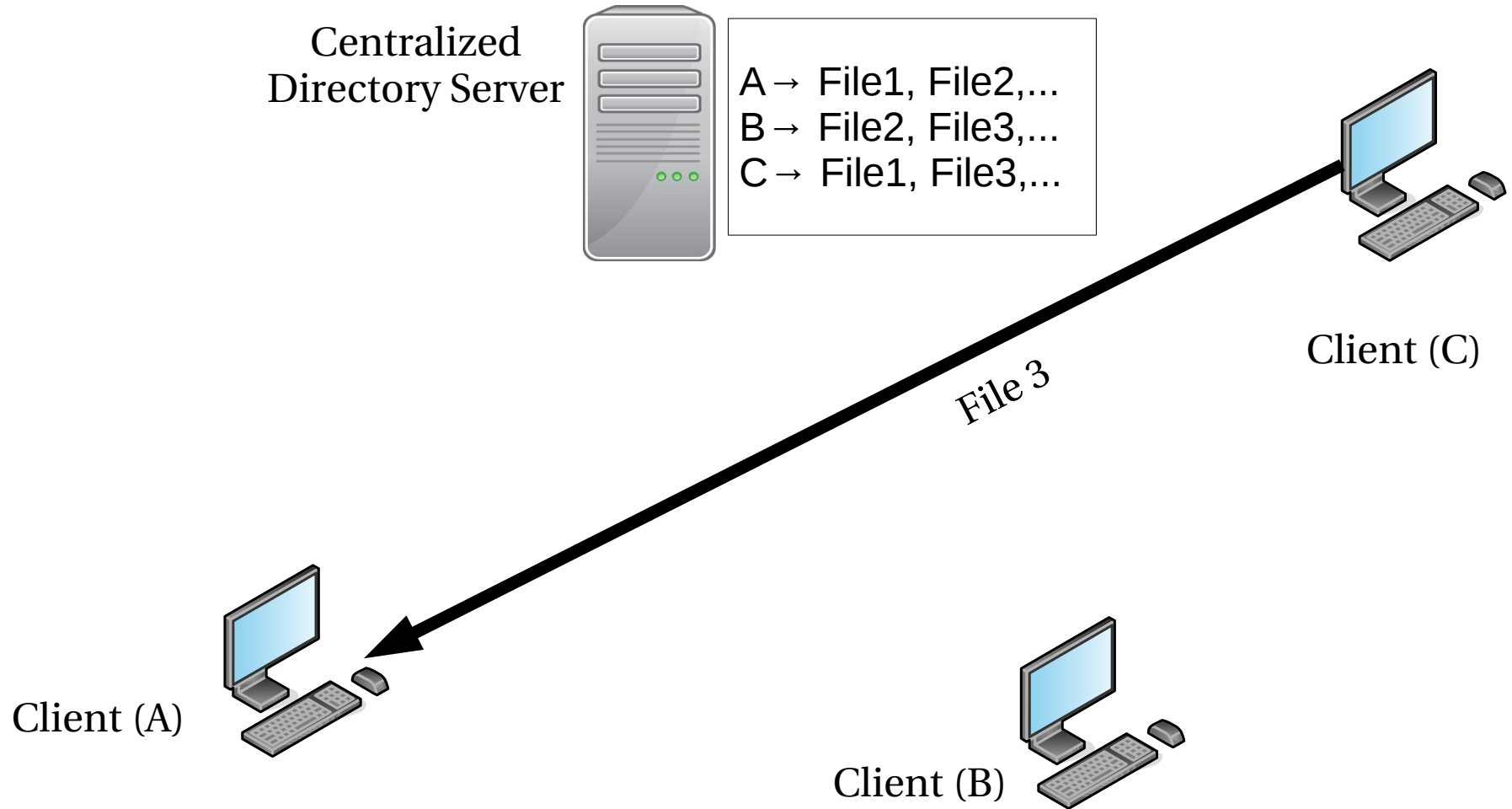


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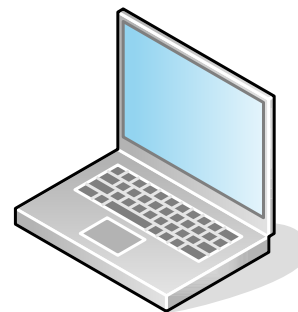
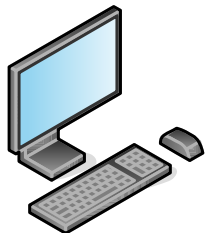
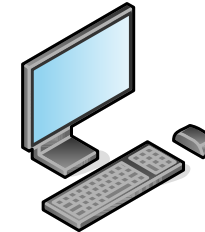


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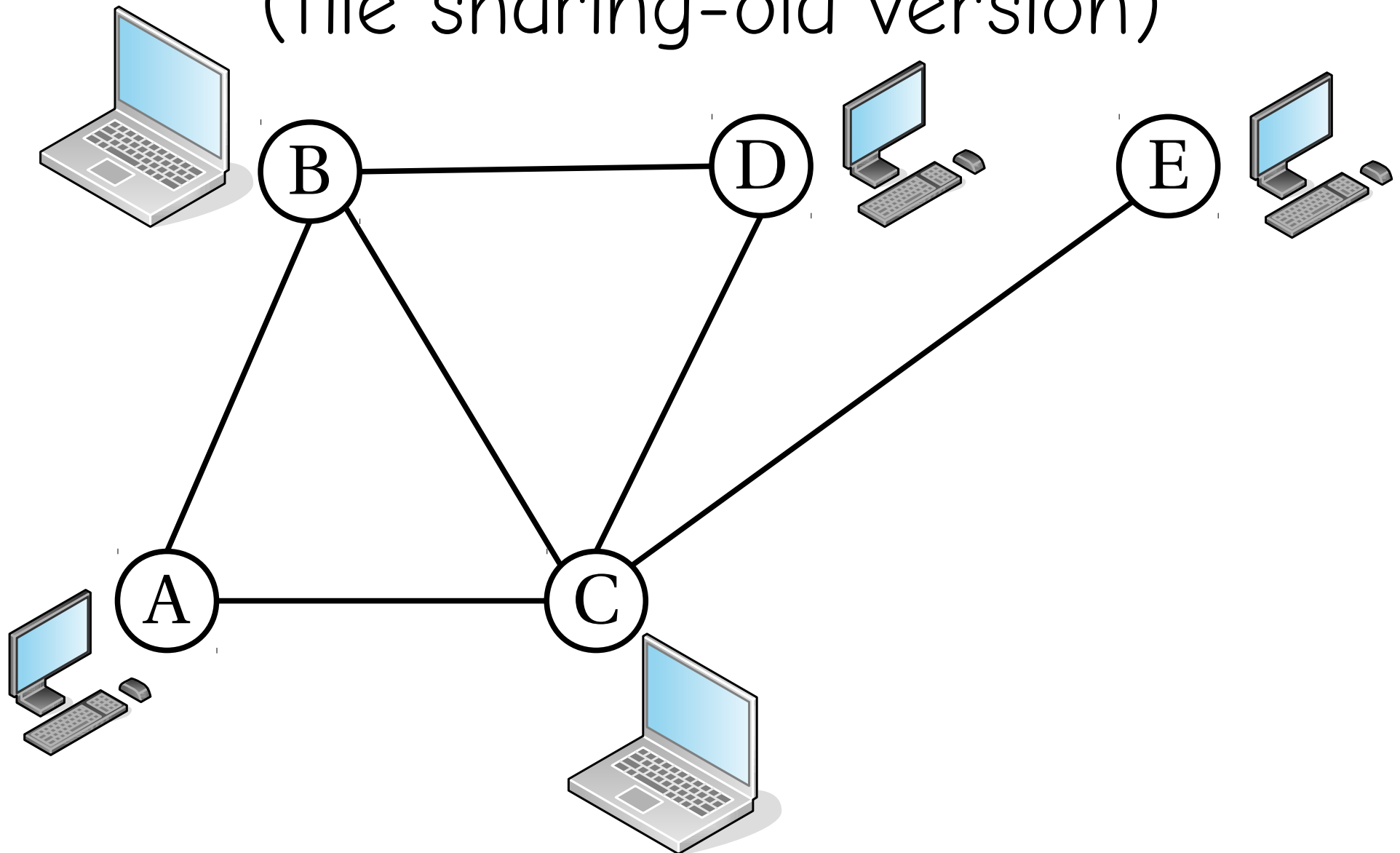


Gnutella (file sharing-old version)



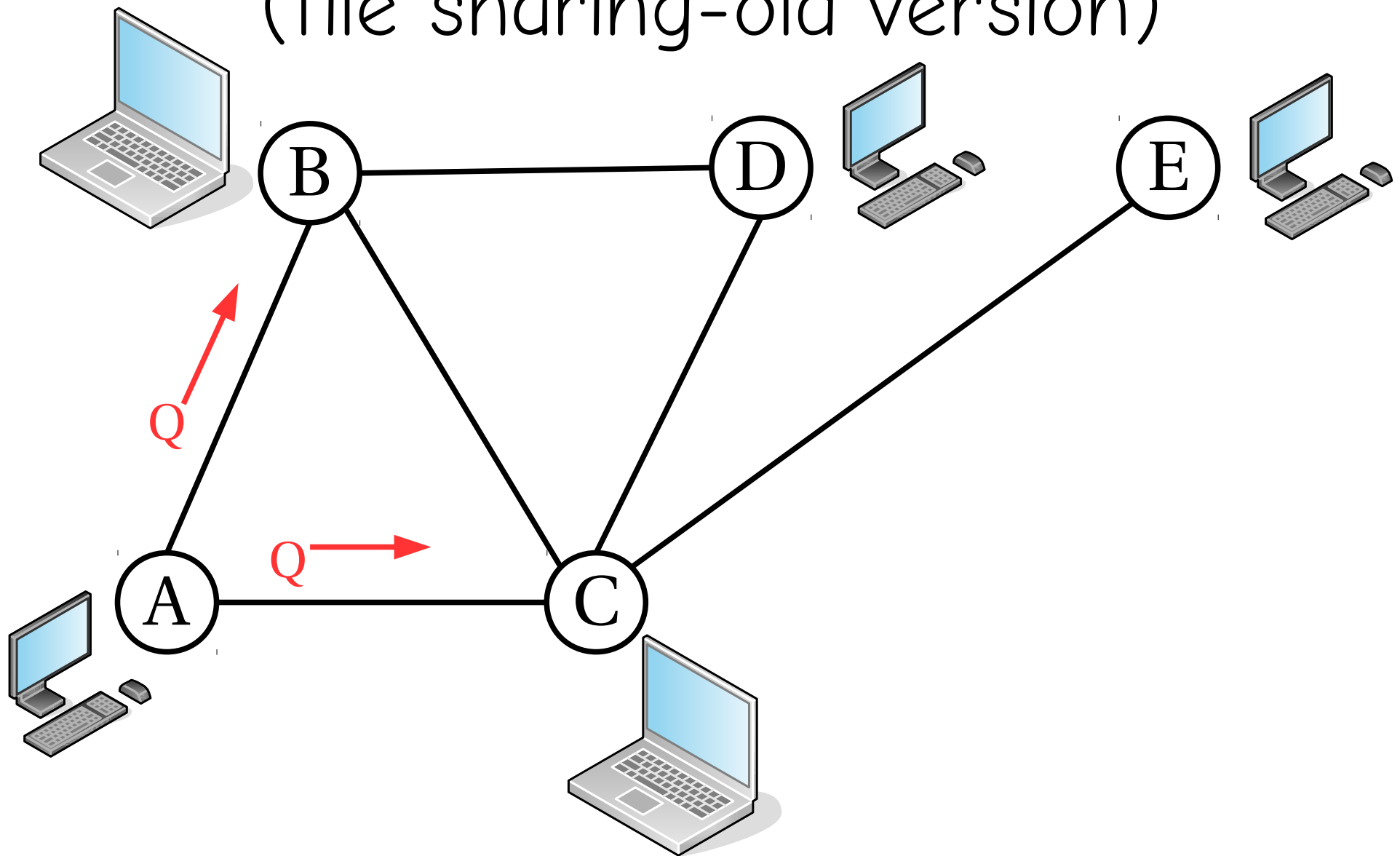


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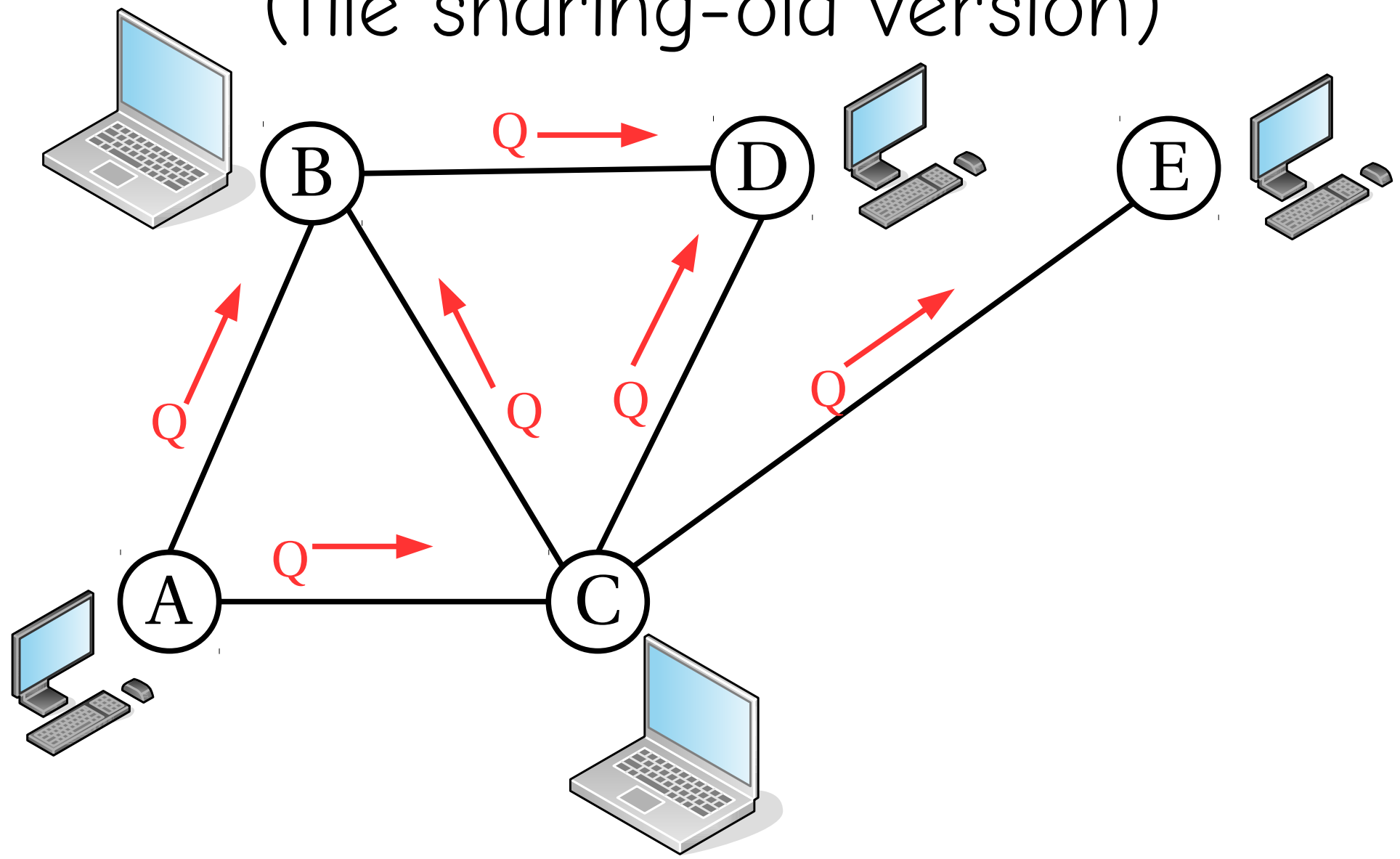


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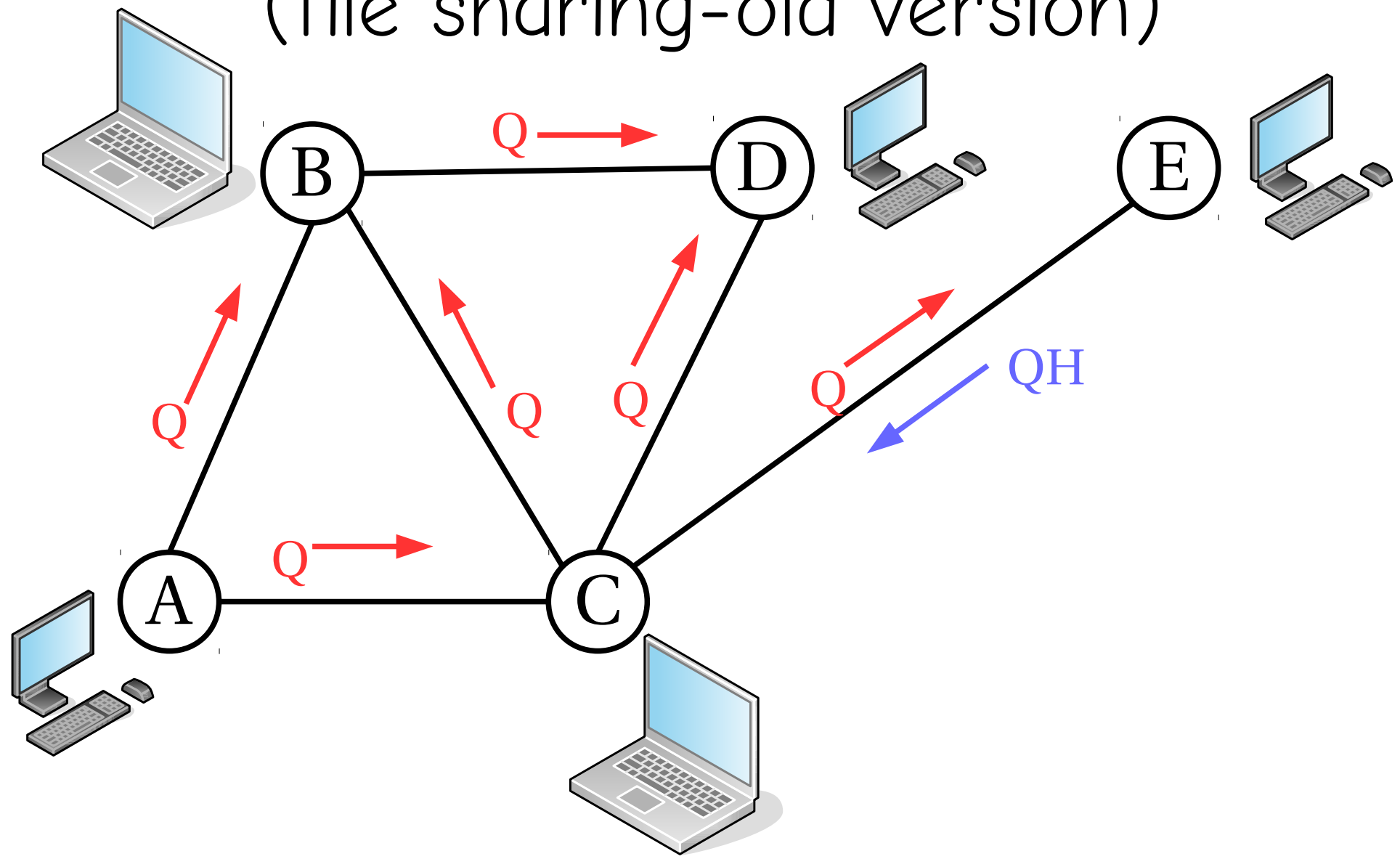


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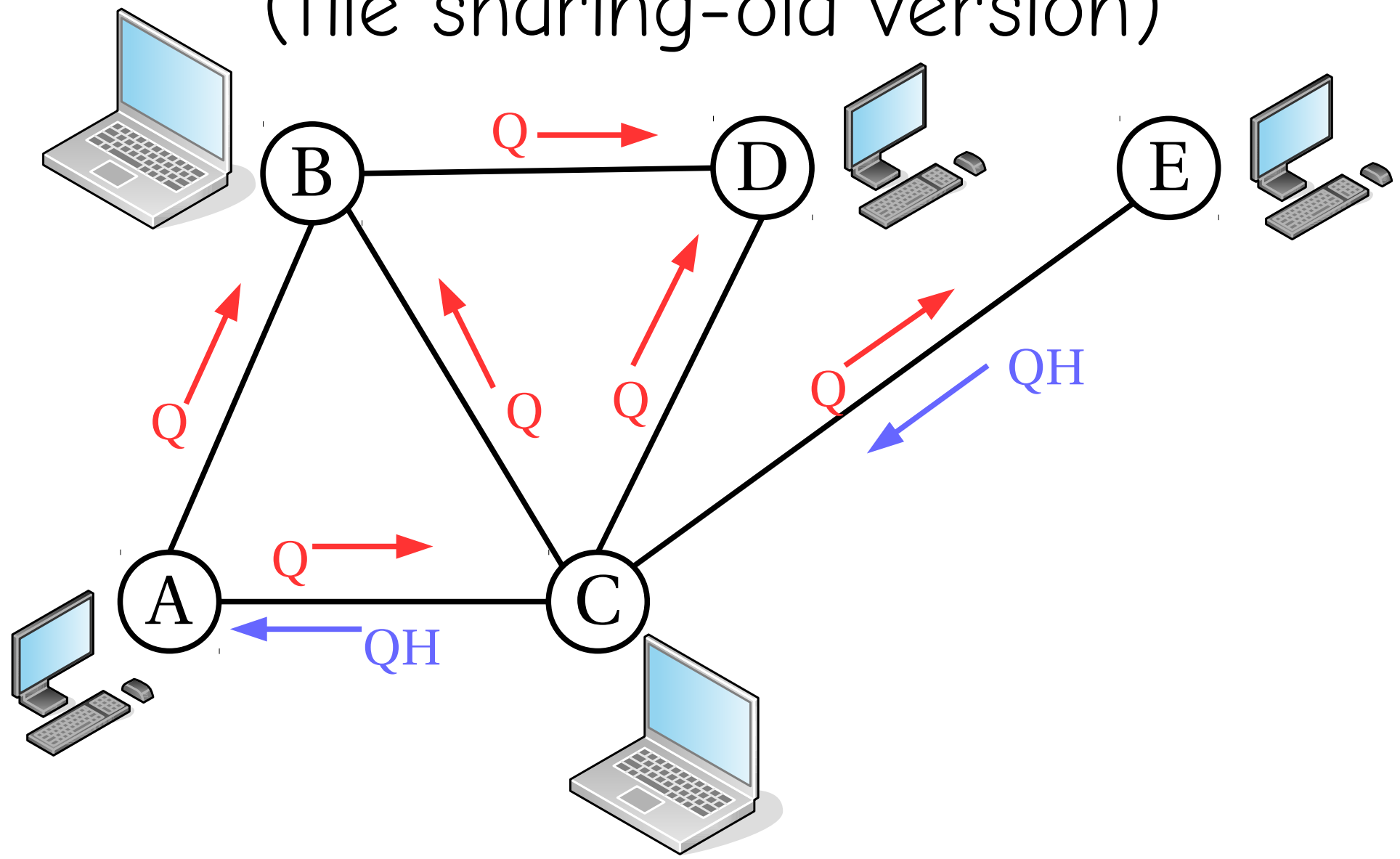


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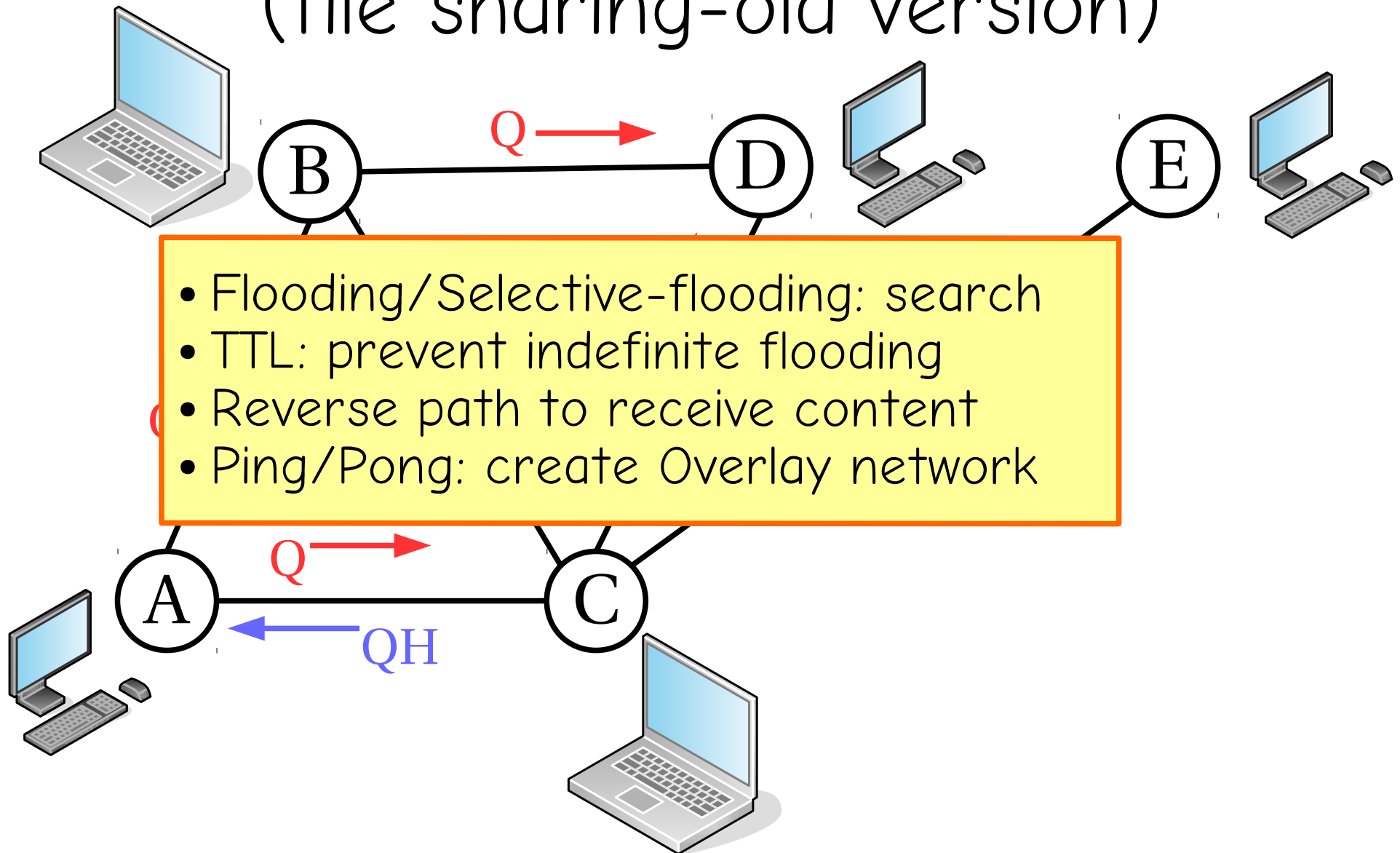


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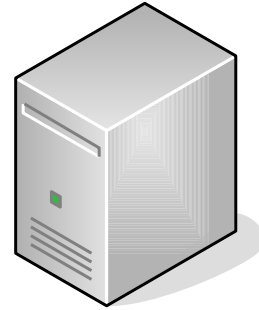
BitTorrent

(P2P content dissemination)



BitTorrent

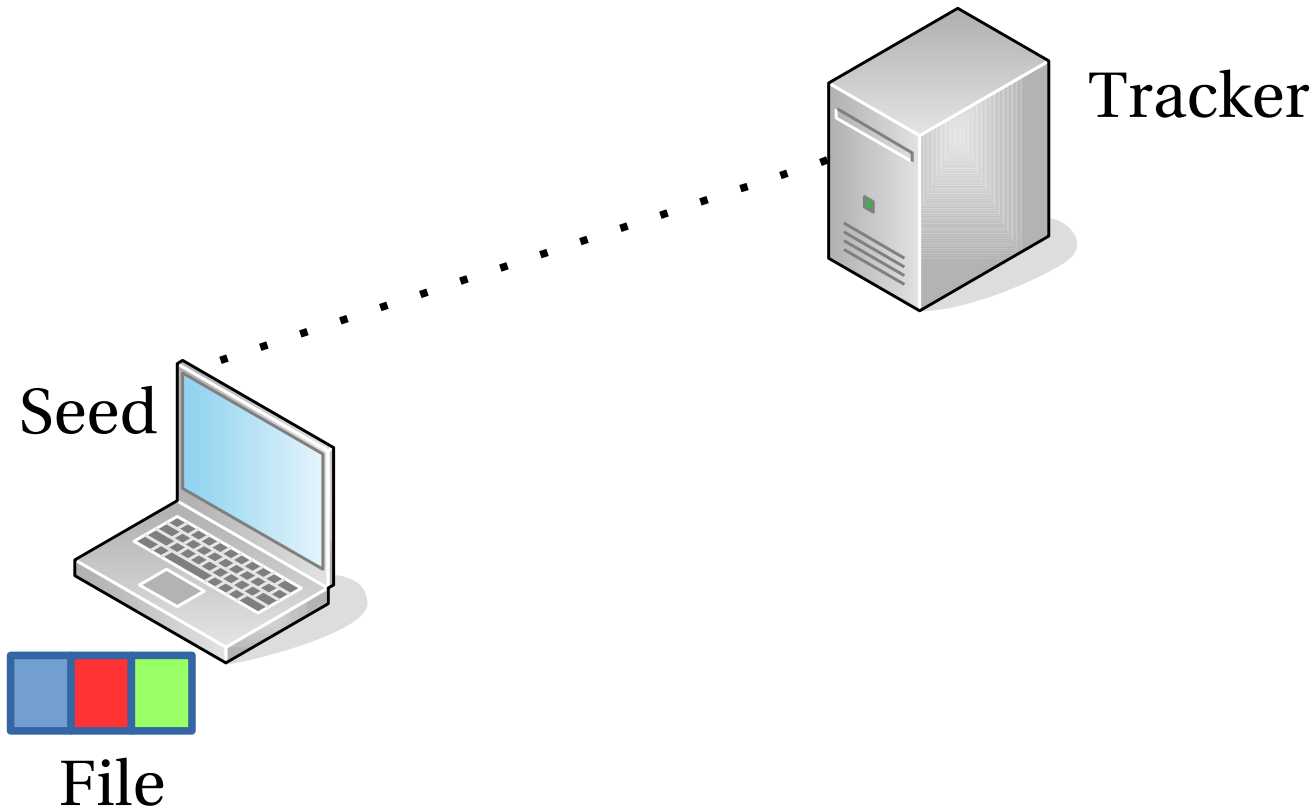
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Tracker

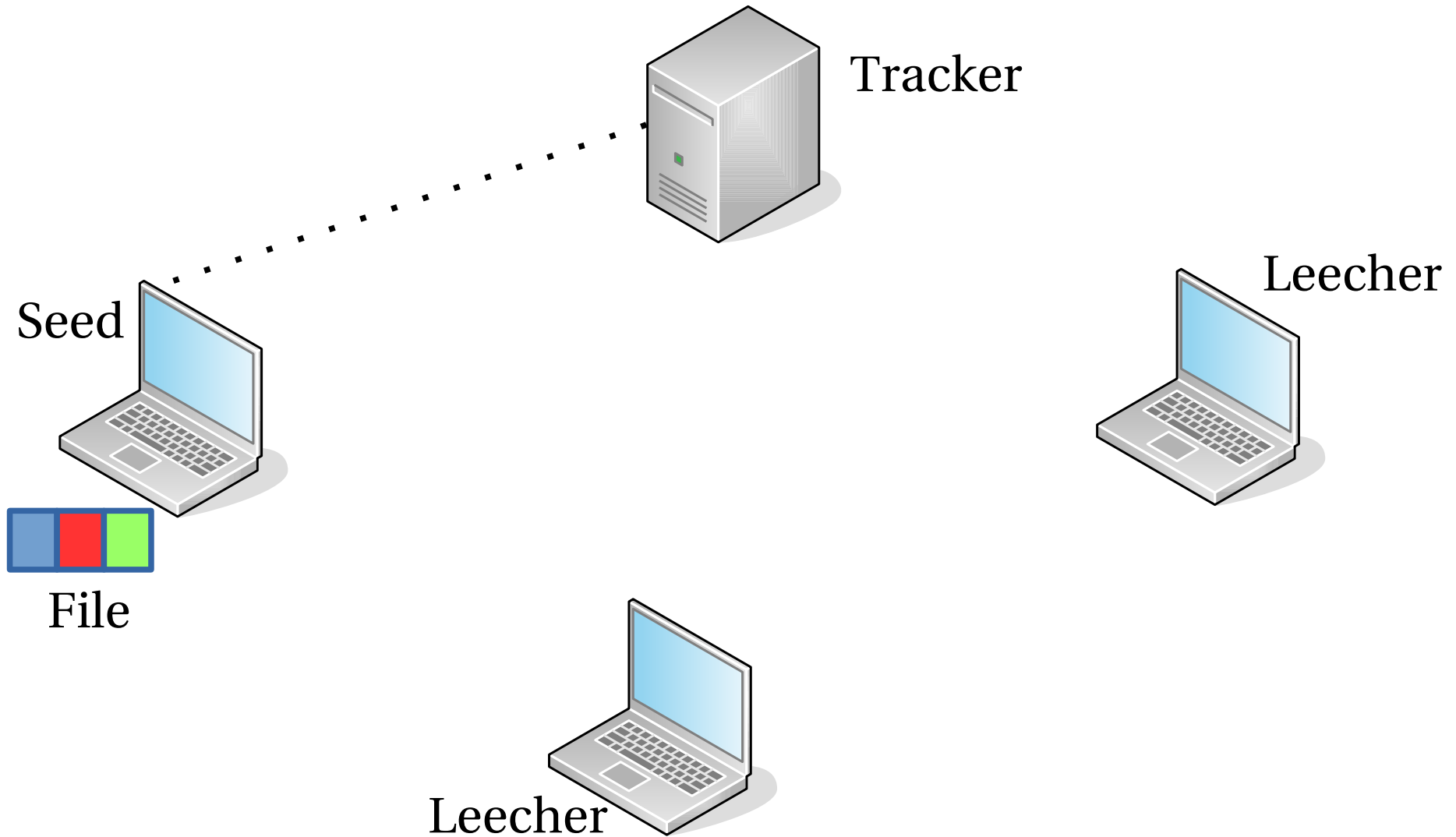


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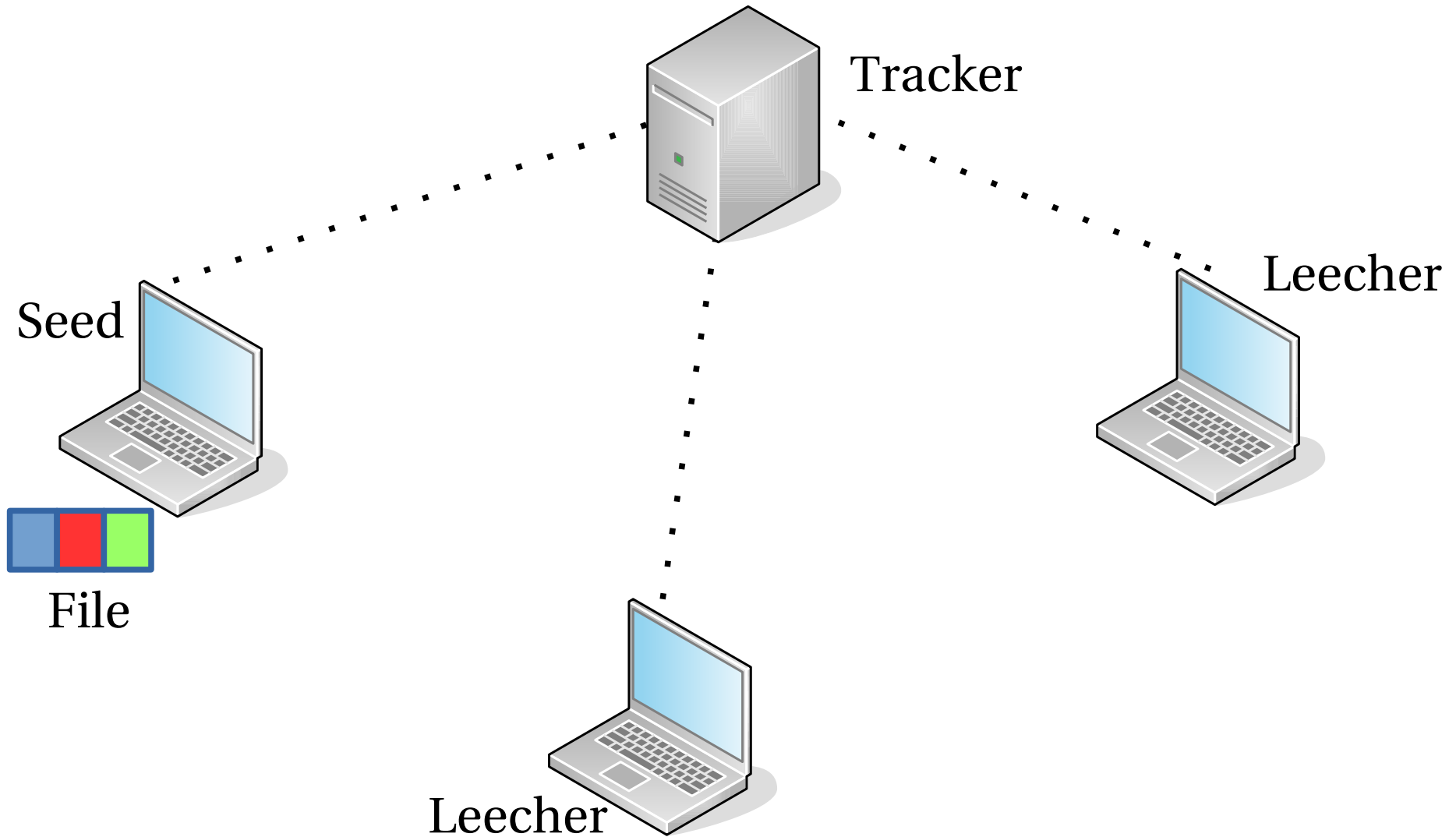


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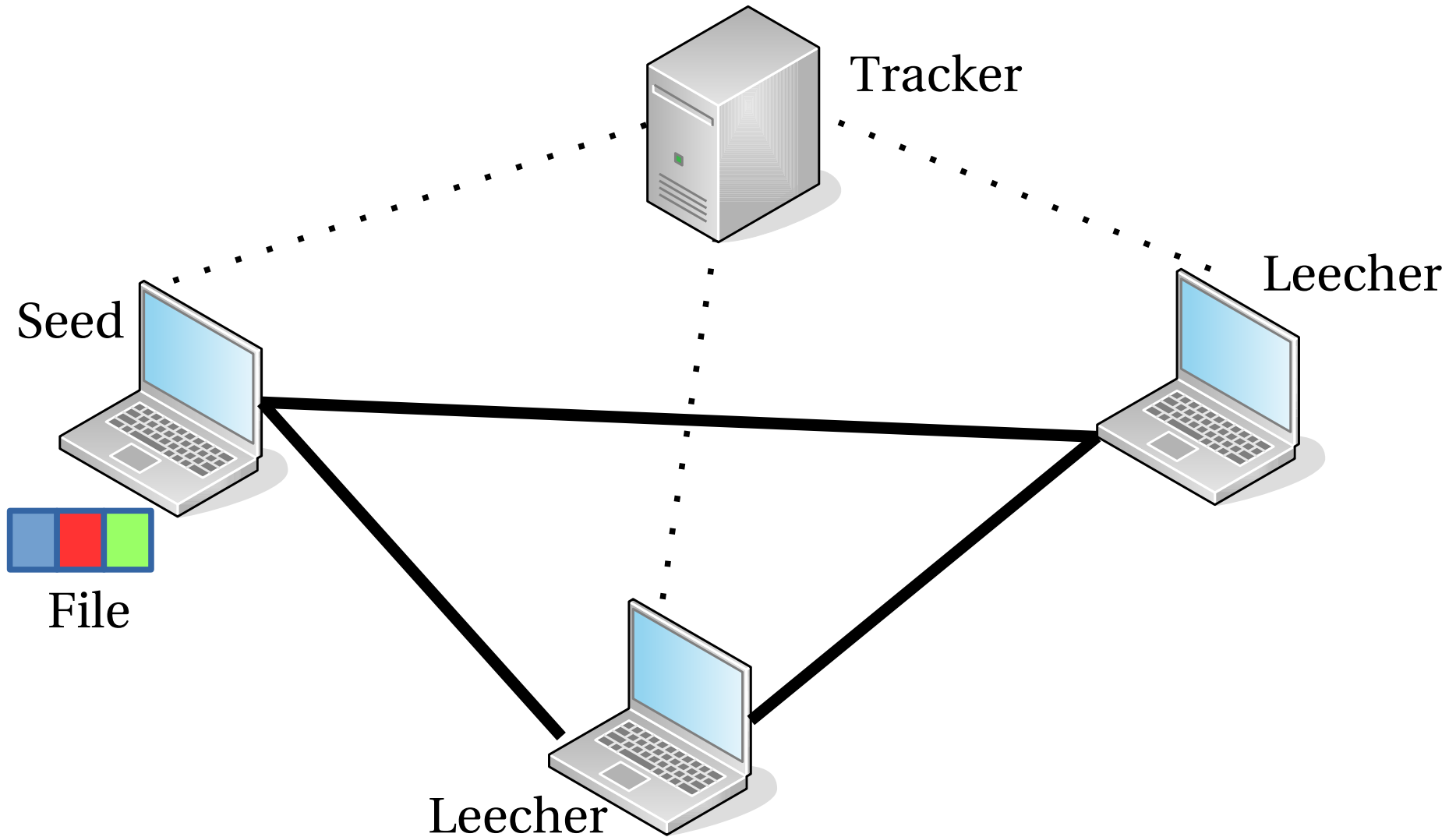


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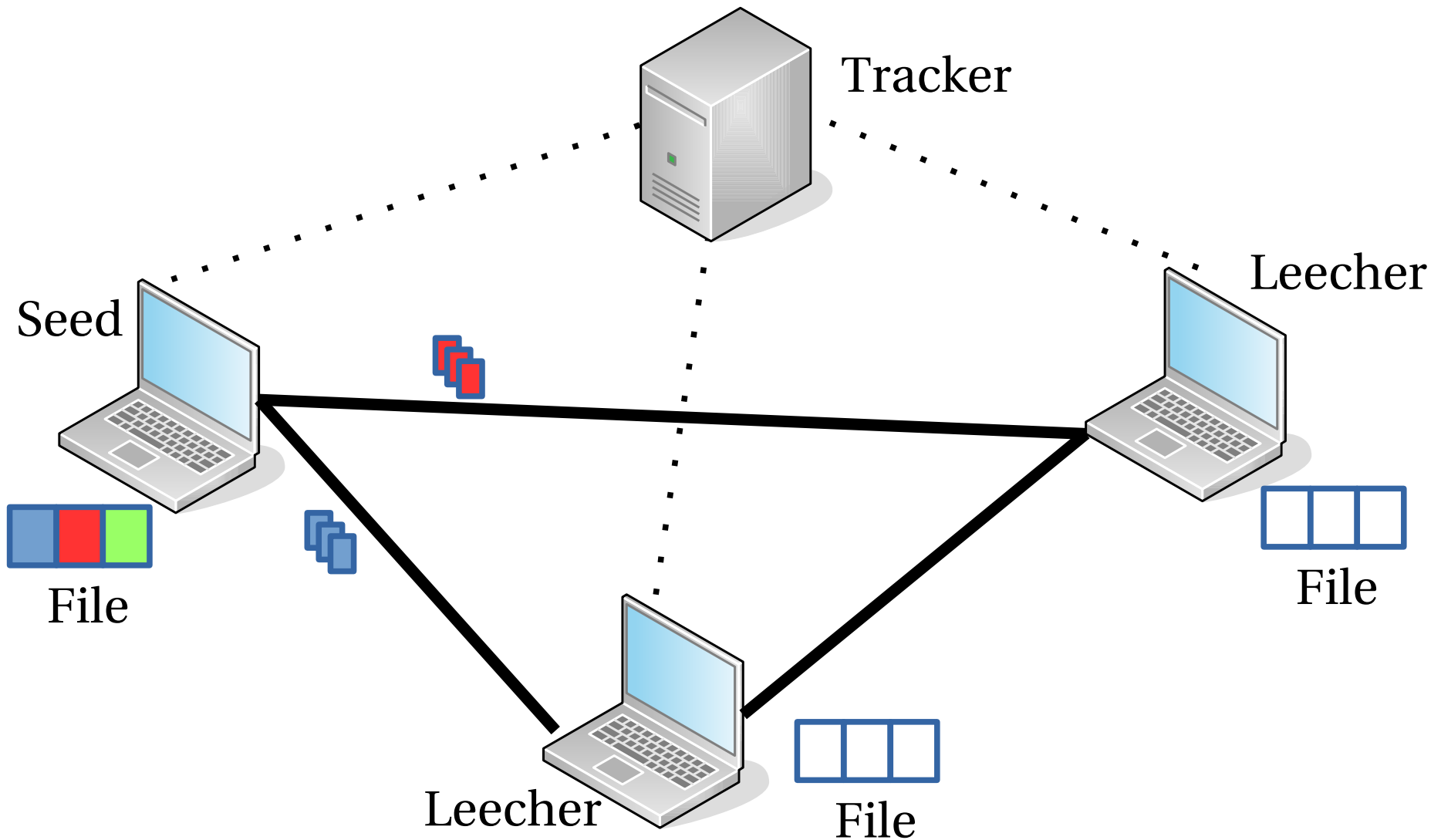


BitTorrent (P2P content dissemination)



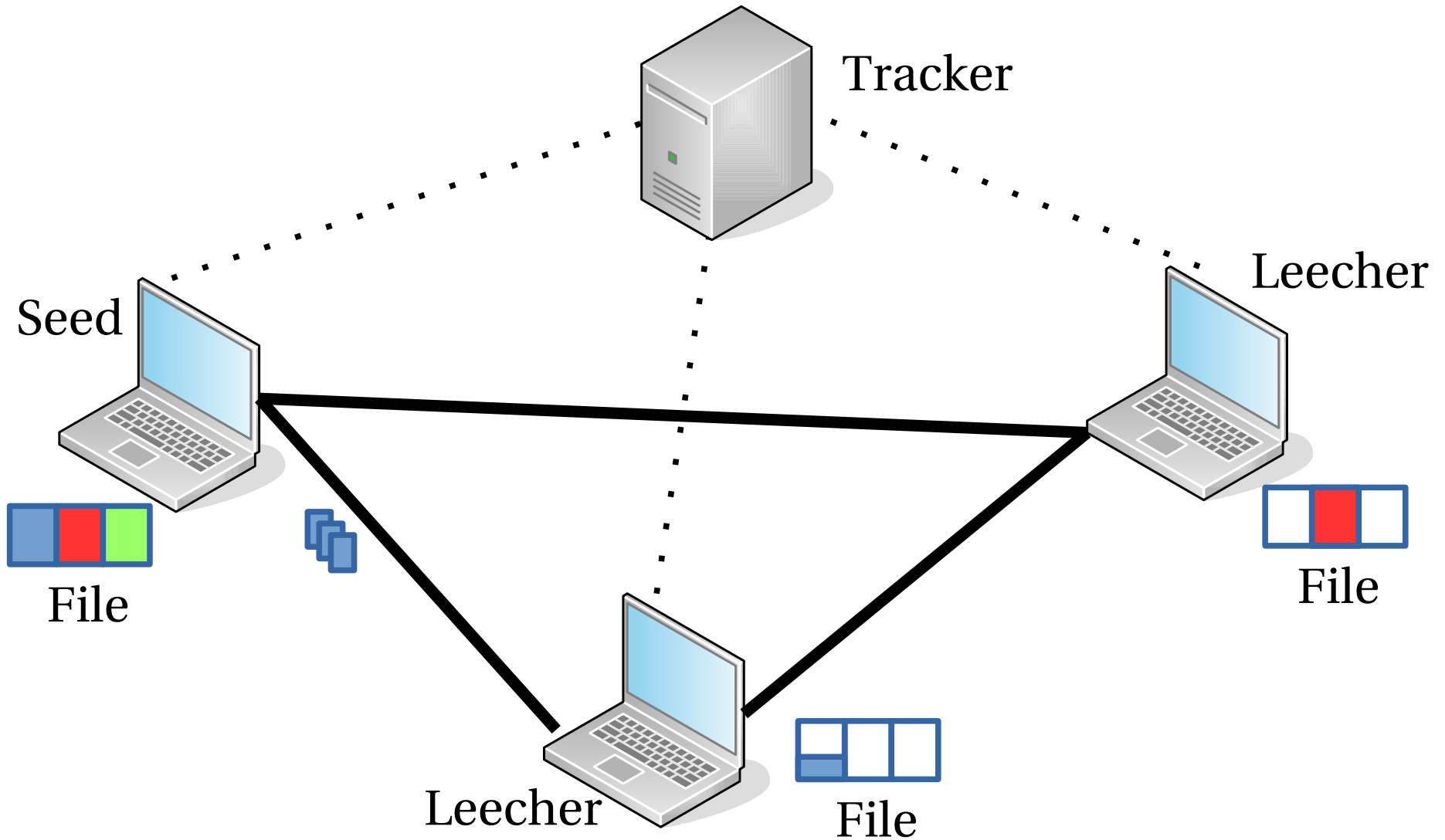


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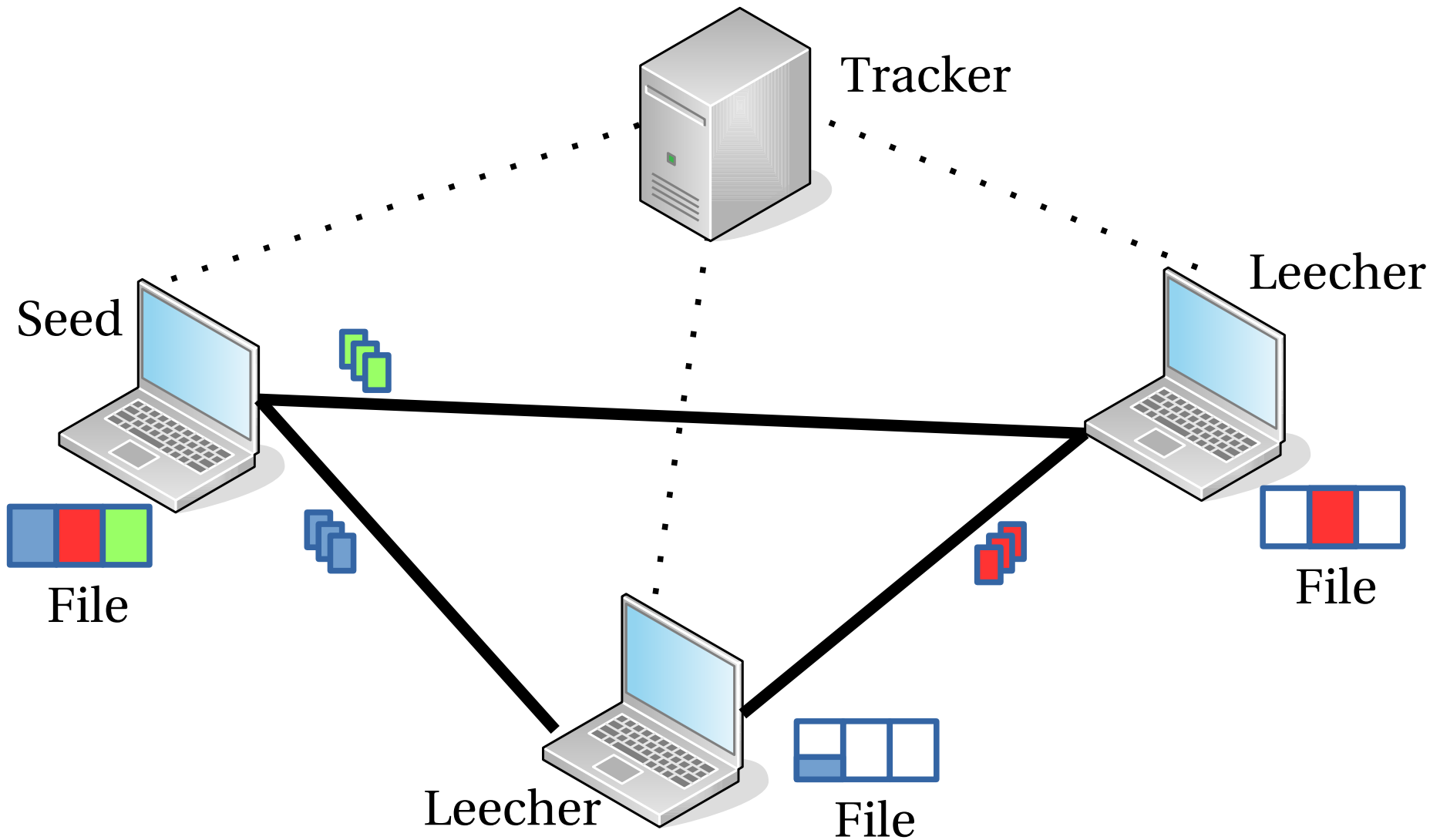


BitTorrent (P2P content dissemination)





BitTorrent (P2P content dissemination)





Freenet

- Self-organizing and Self-contained P2P network
- Collaborative (distributed) virtual file system
- Strong anonymity and censorship resistance



More Resources

- Video: Freenet at C3 Conference:
- B. Cohen.
Incentives for building robustness in BitTorrent
- Stefan Saroiu, Krishna Gummadi, and Steven Gribble.
"A Measurement Study of Peer-to-Peer File Sharing Systems."



Properties of Unstructured Overlay Networks



Properties of Unstructured Overlay Networks

- Unstructured Link Creation
- Random Arrivals and Churn
- Flat or Hierarchical organization
- and many more ...



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- Unstructured Link Creation
- Random Arrivals and Churn
- Flat or Hierarchical organization
- and many more ...

Which graph abstracts unstructured
(and other) overlay networks?



Why is modeling important?

- What is the expected latency to the peek the content?
 - Average distance between nodes
- What is the impact of a peer leaving the network?
 - Robustness to faults/down-times
- What are the factors that determine the evolution of the graph structure?
 - Impact of proposed optimizations such as localization of content
- ...



Birds Eye View of Complex Networks



Small World

- Stanley Milgram. "**The small world problem.**" *Psychology today* 2.1 (1967): 60-67
 - "Given any two persons in the world, person X and person Z, how many intermediate acquaintance links are needed before X and Z are connected?"
- Mathematical structure of society



Milgrams Approach

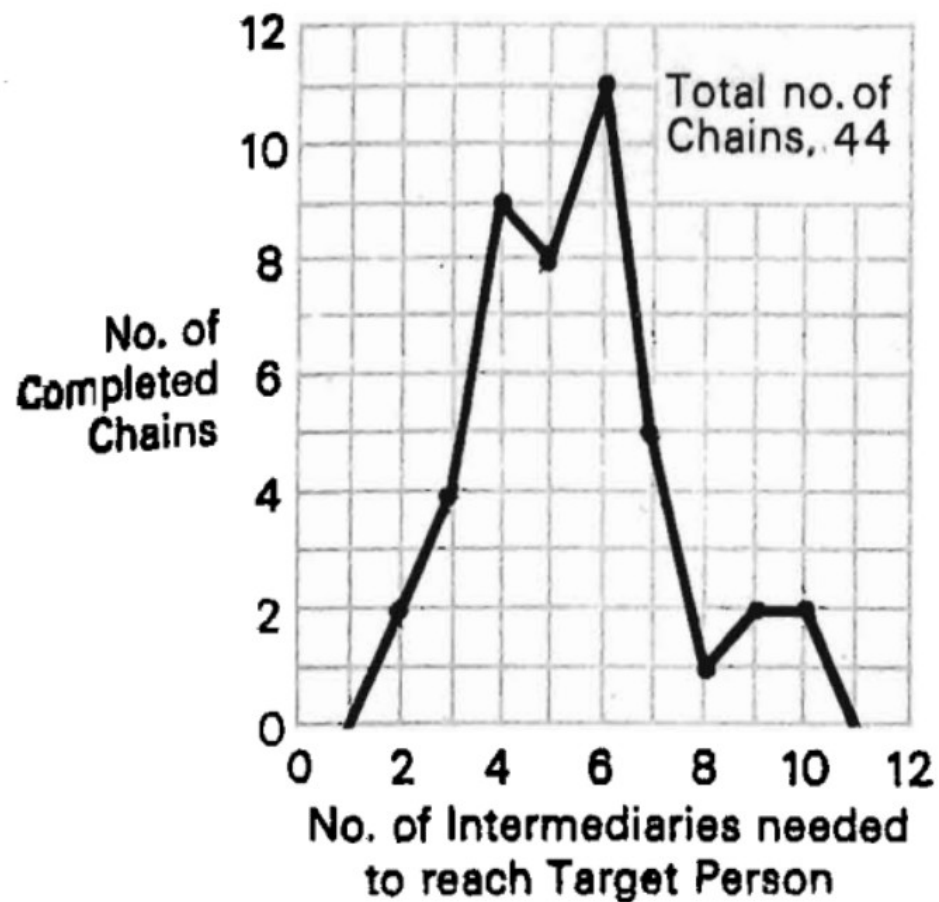
A random person X was selected and given a document.

The document contained

- (1) The name of person Z and some information such as profession and city name
- (2) If X did not know person Z then X mails it to a person Y whom X knows on a first name basis and who is more likely than X to know Z . (Y is the new X)
- (3) A roster on which each person to whom document arrives writes his/her name. Roster also prevents endless looping.



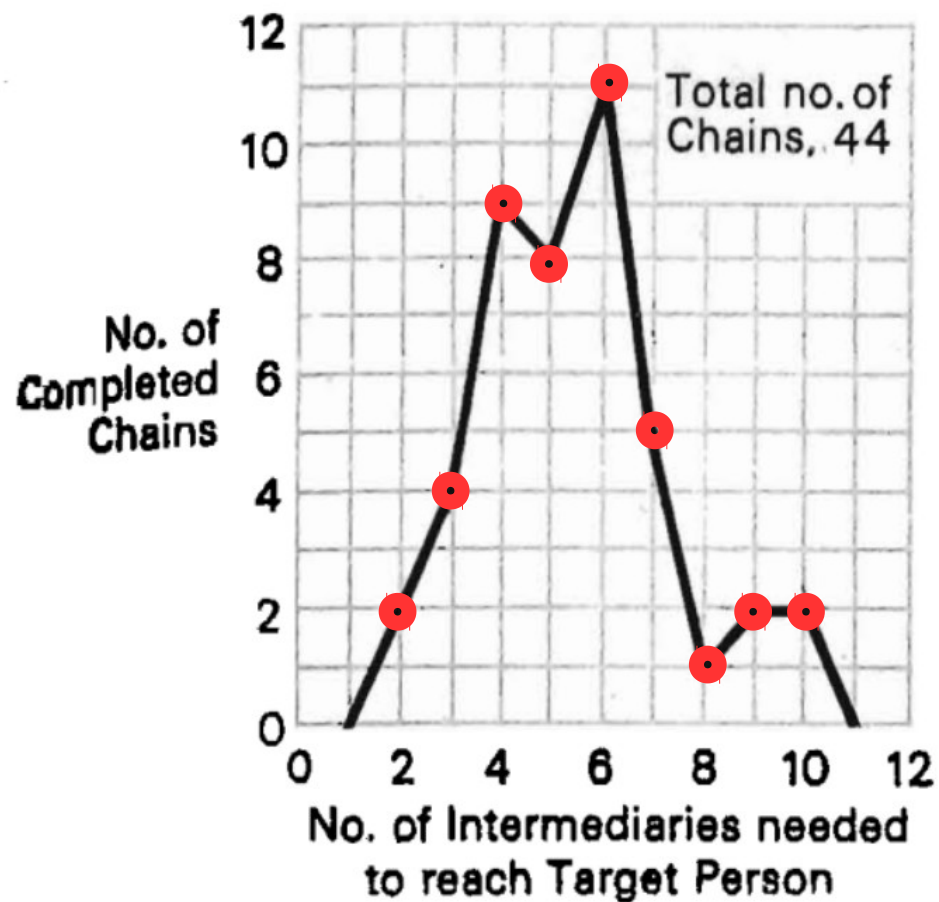
Key Result



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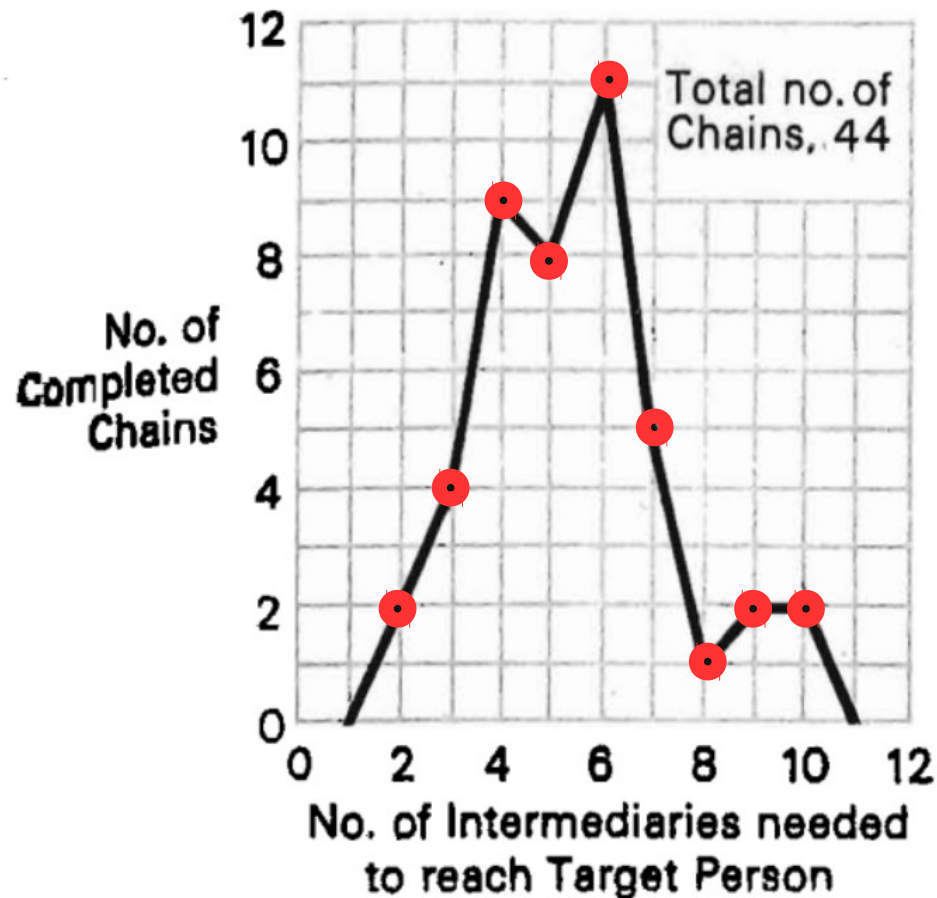


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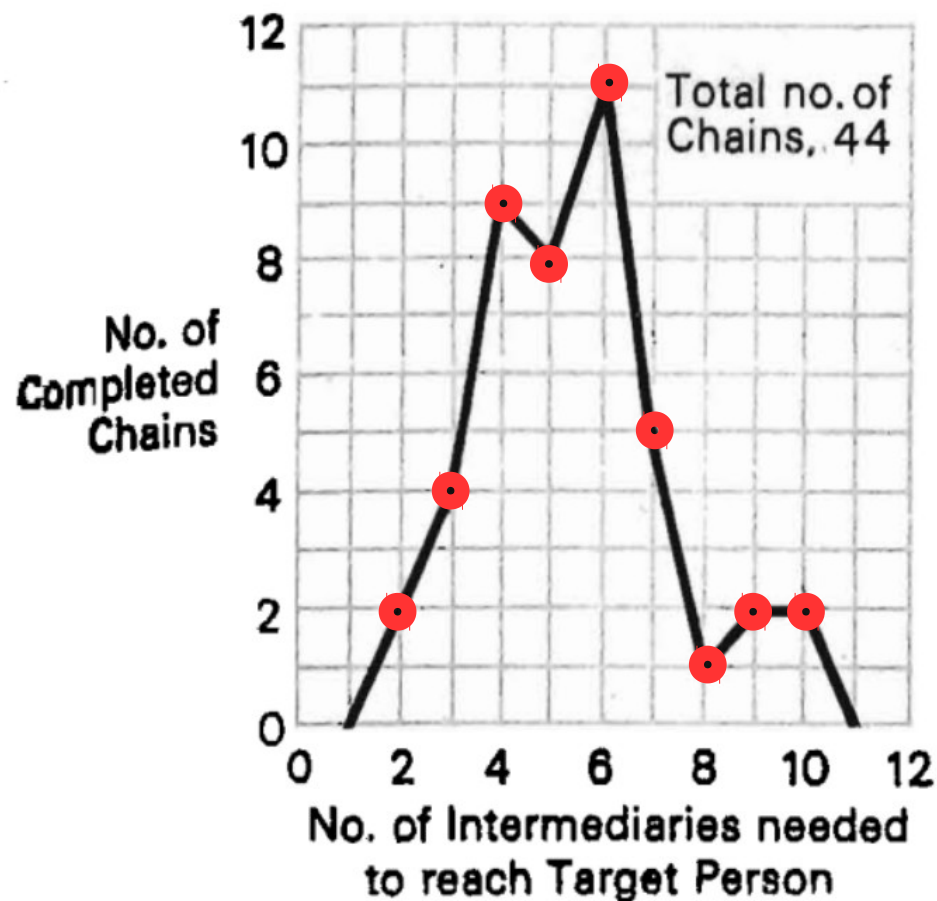
- Median: 5 intermediaries
- How many degrees of separation?



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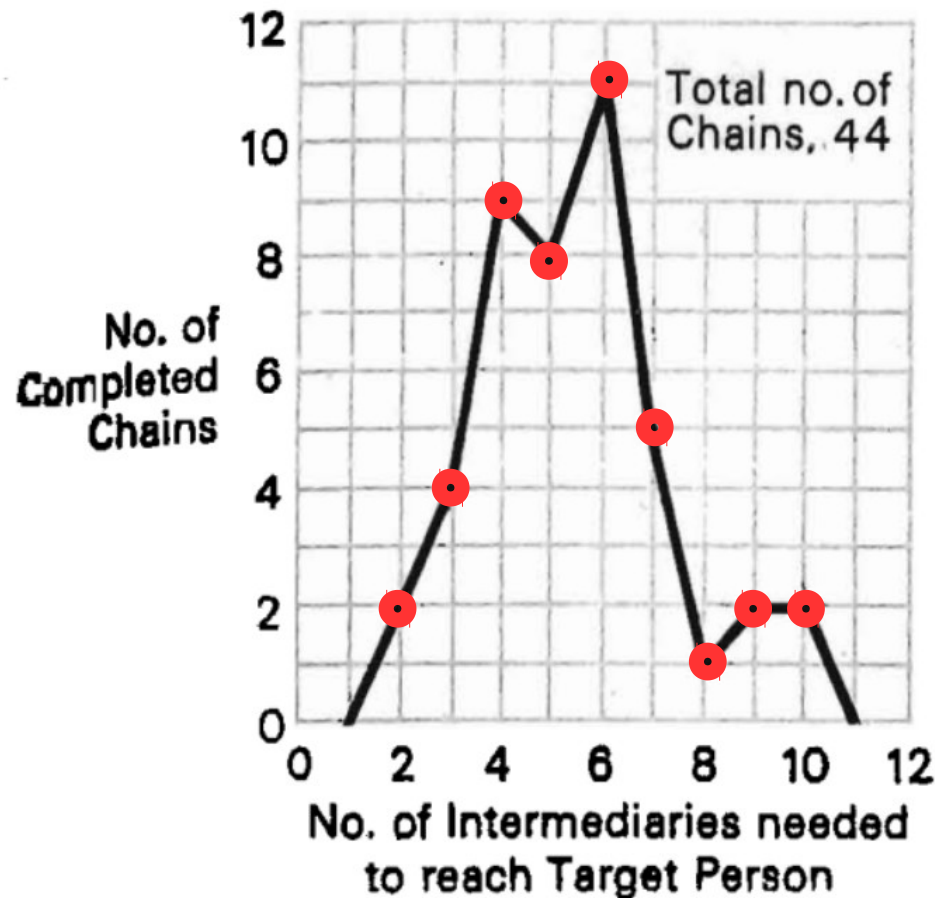


- Median: 5 intermediaries
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- Decay in active chains
 - 126 of 160 chains dropped out!

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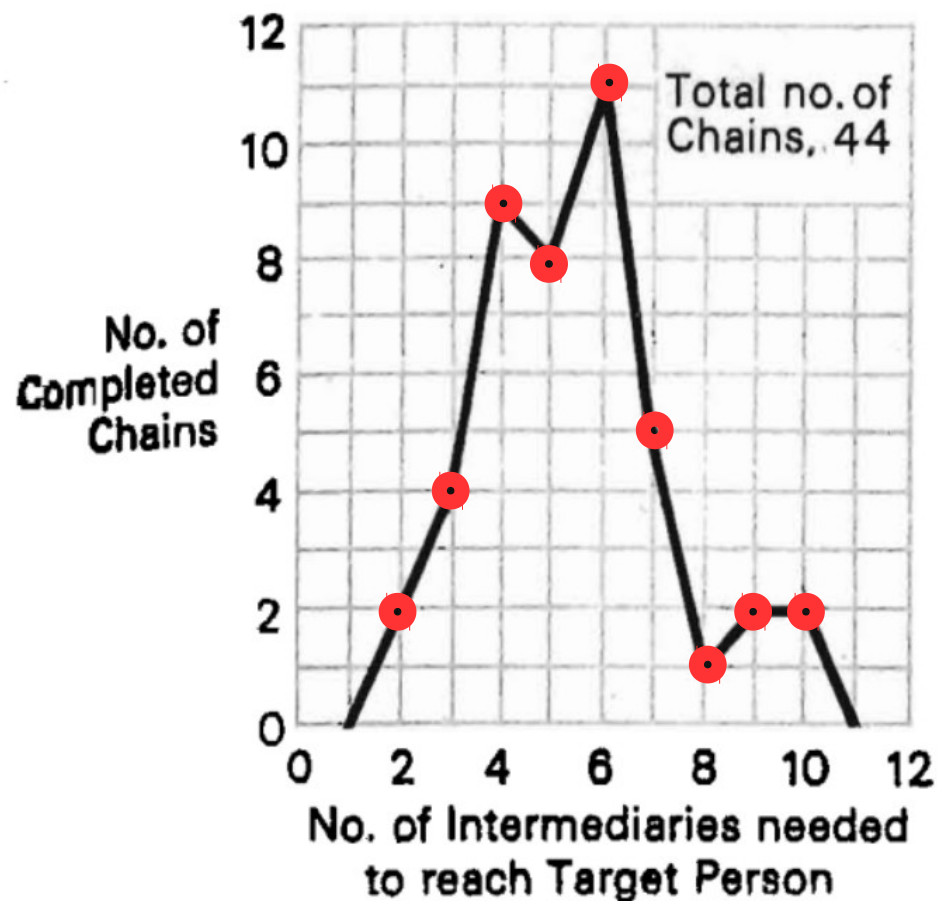


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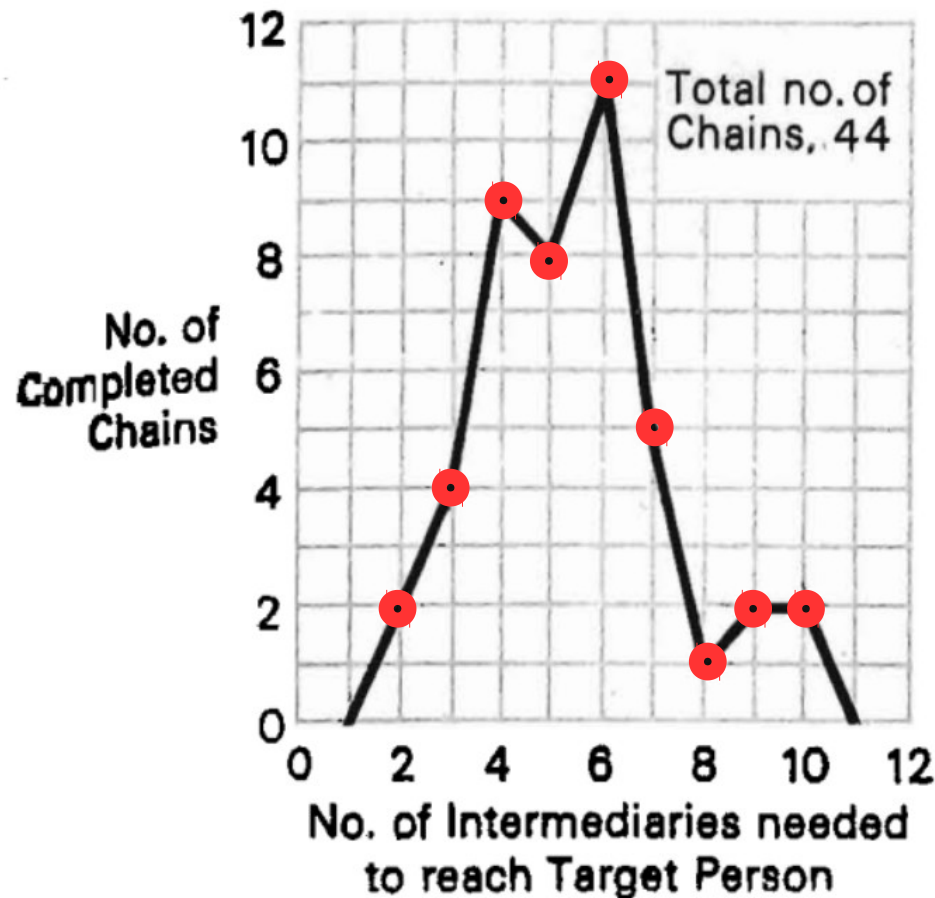


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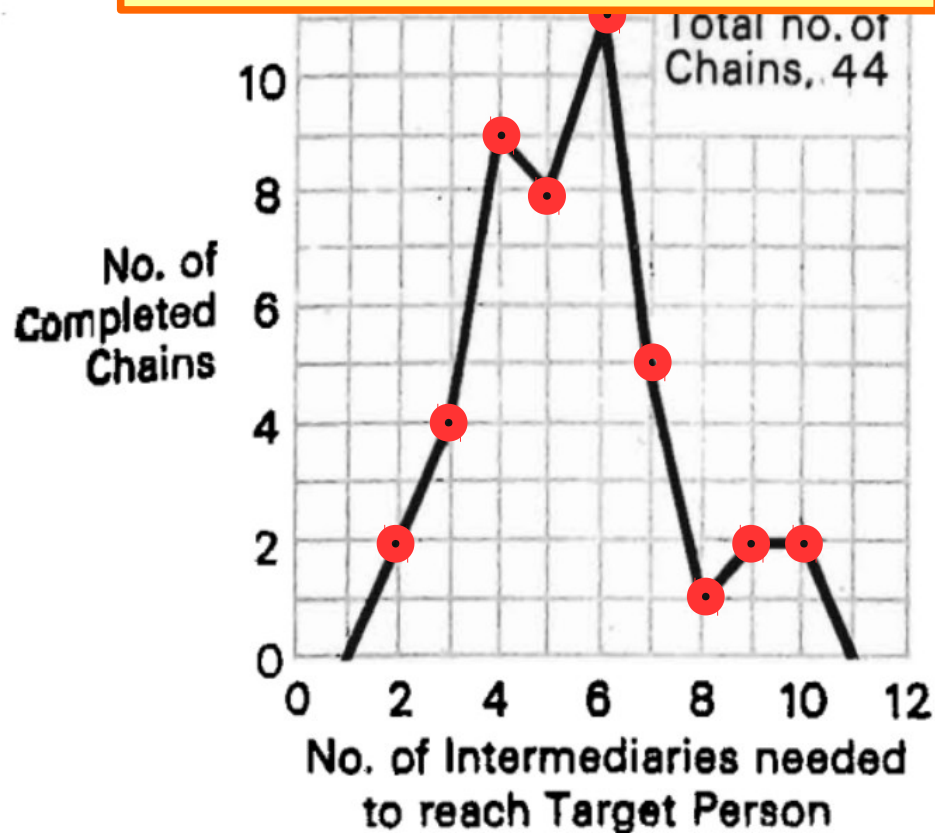
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Key Result

Average diameter?



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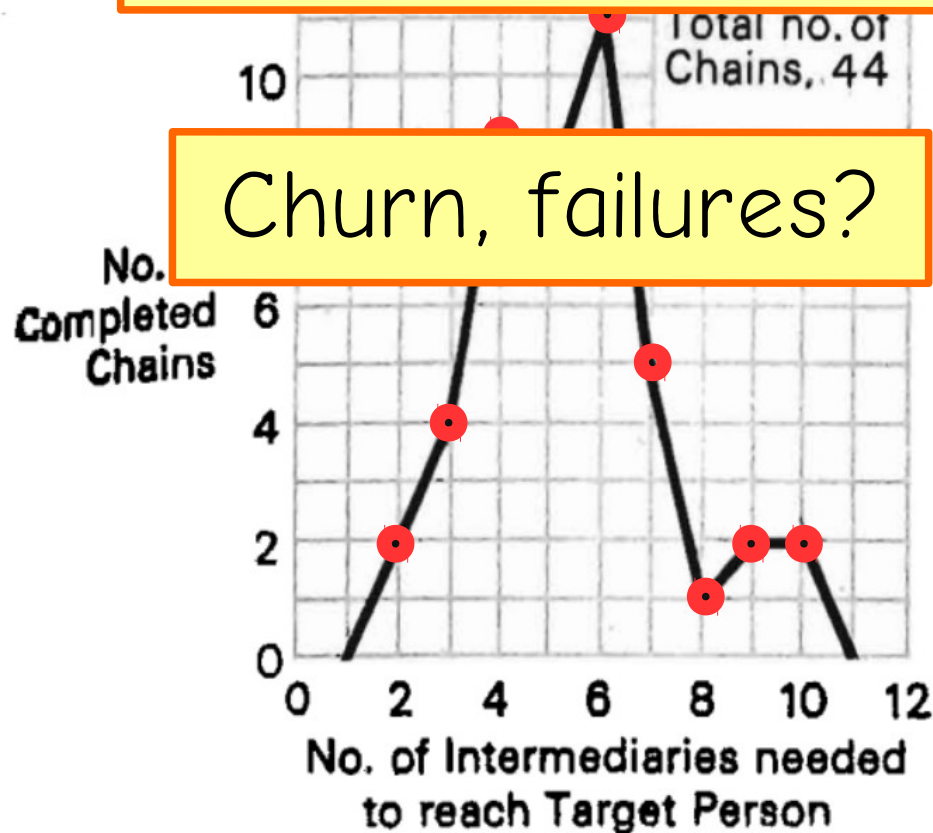
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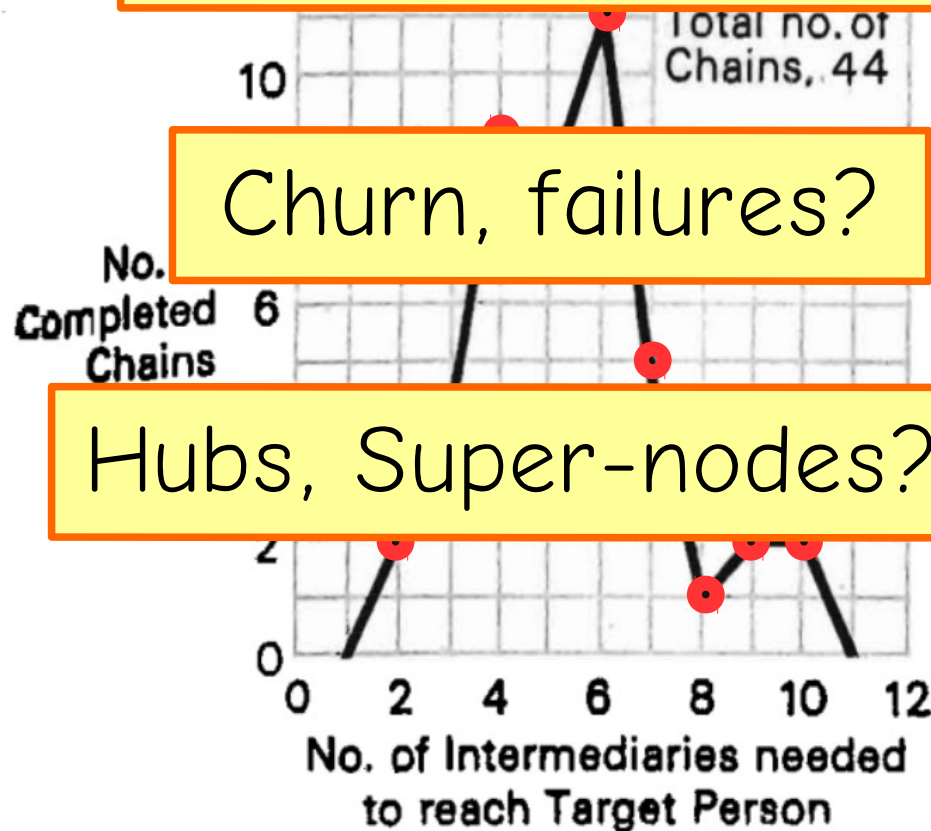


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Device Heterogeneity?

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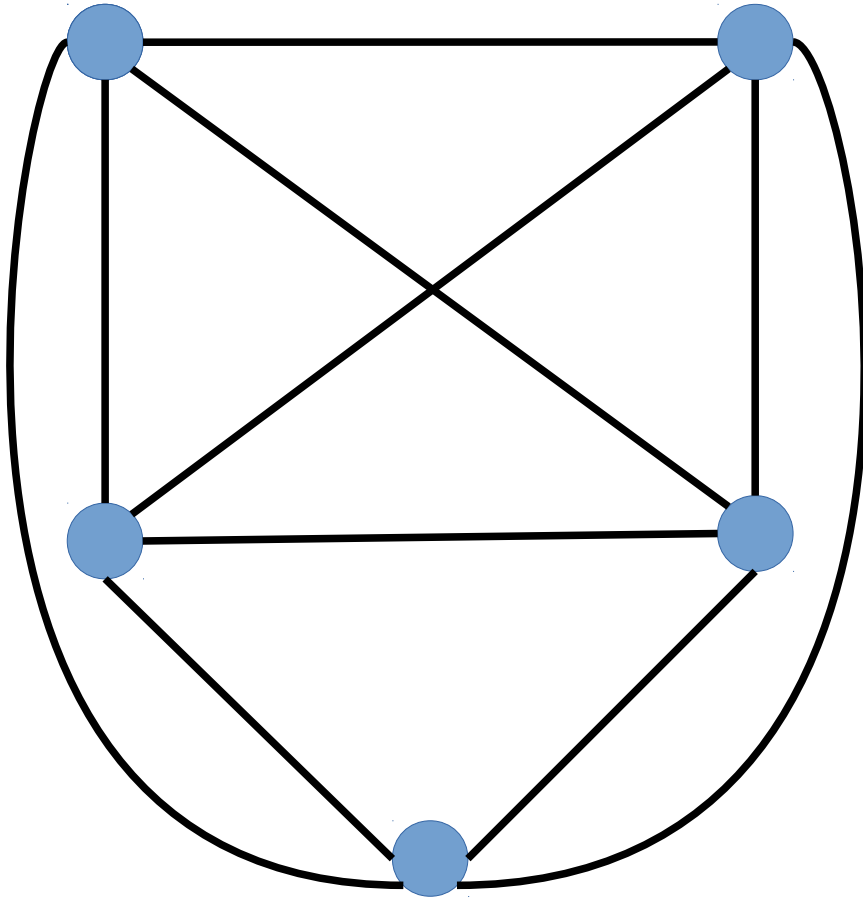


Random Graph

(Erdős–Rényi model) / Gilbert Model

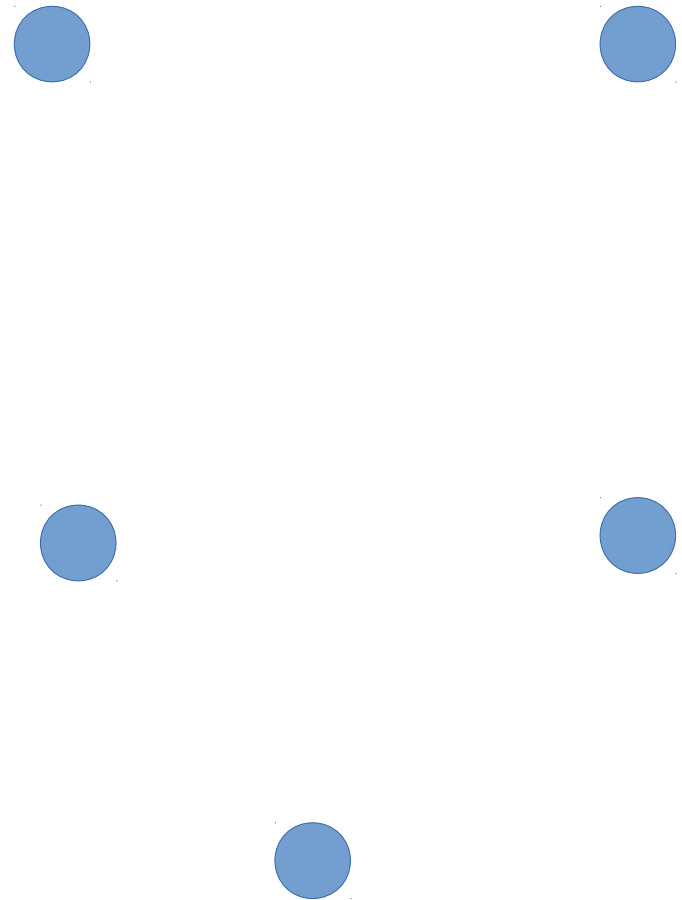
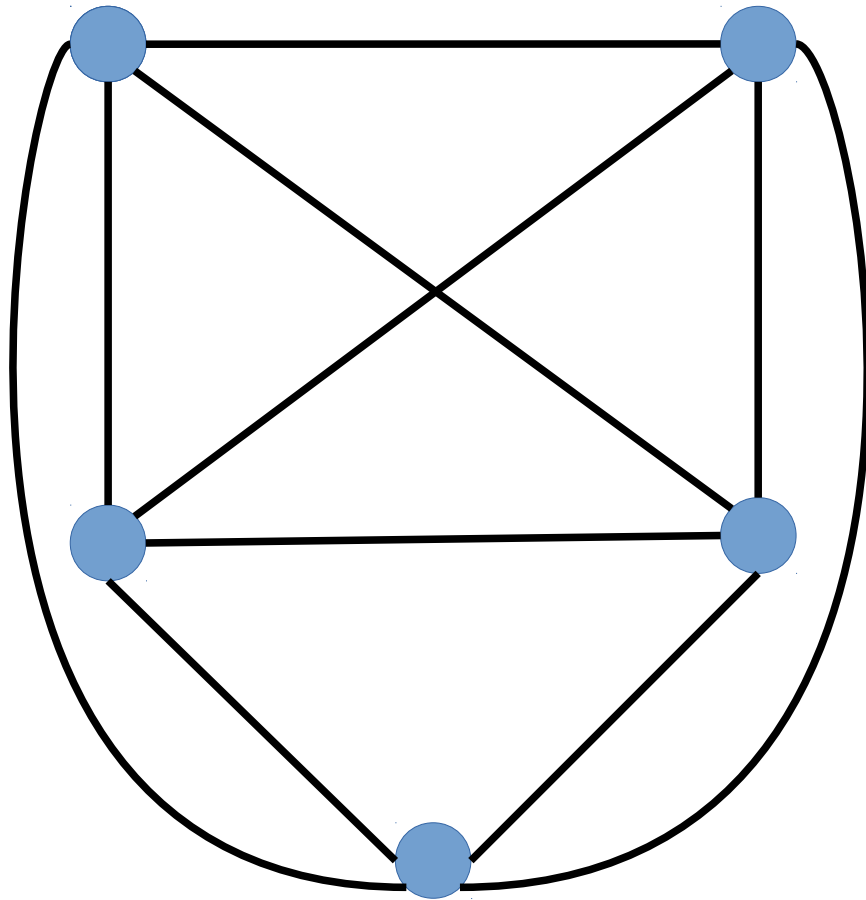


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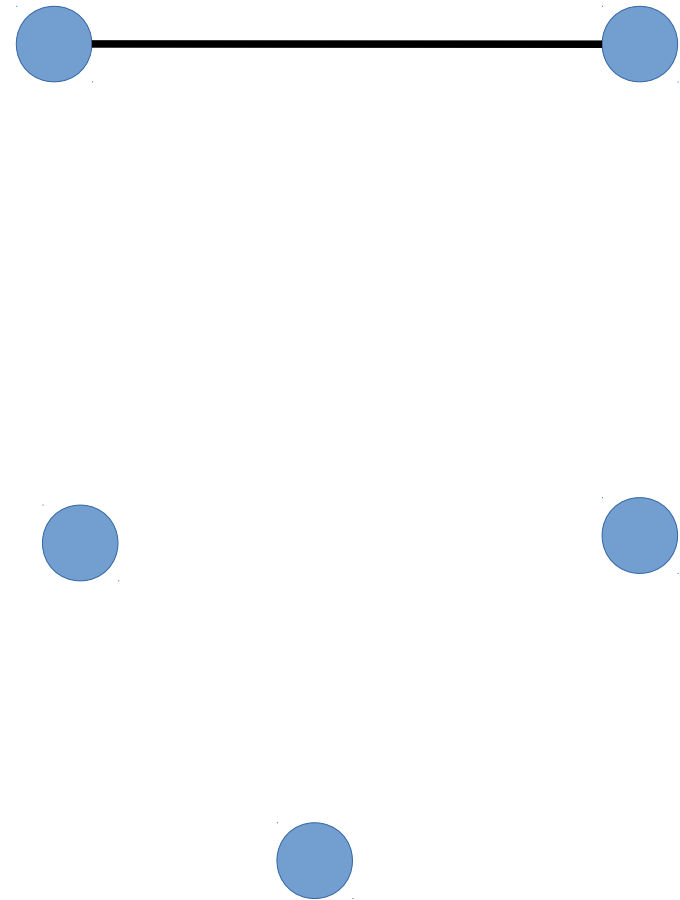
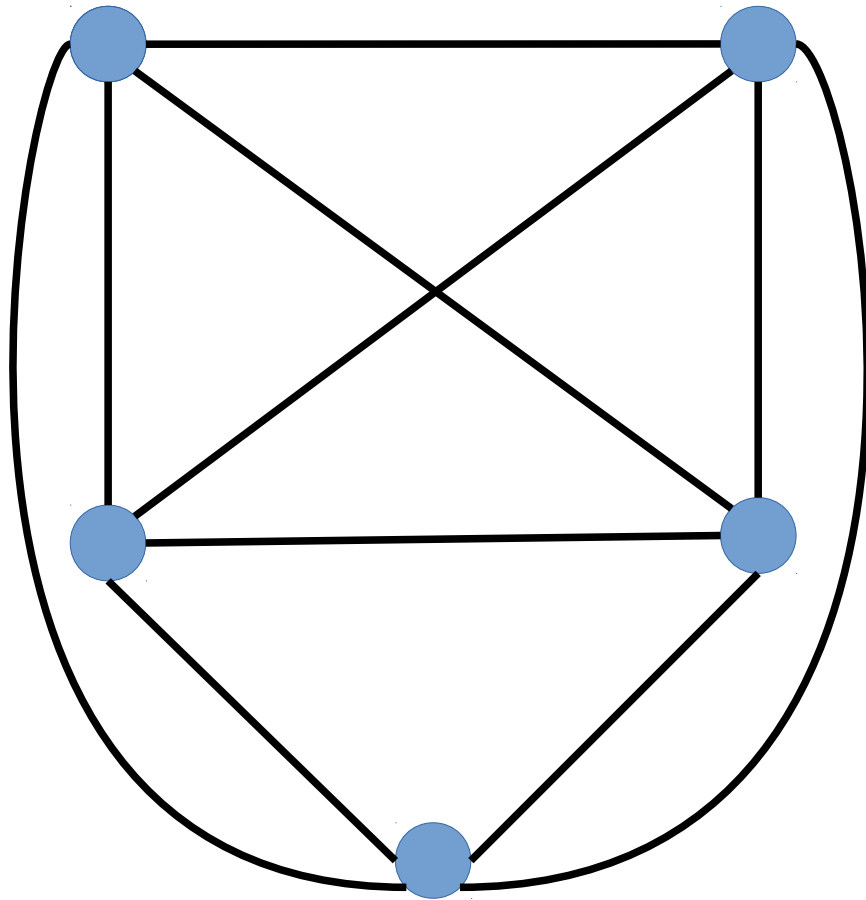


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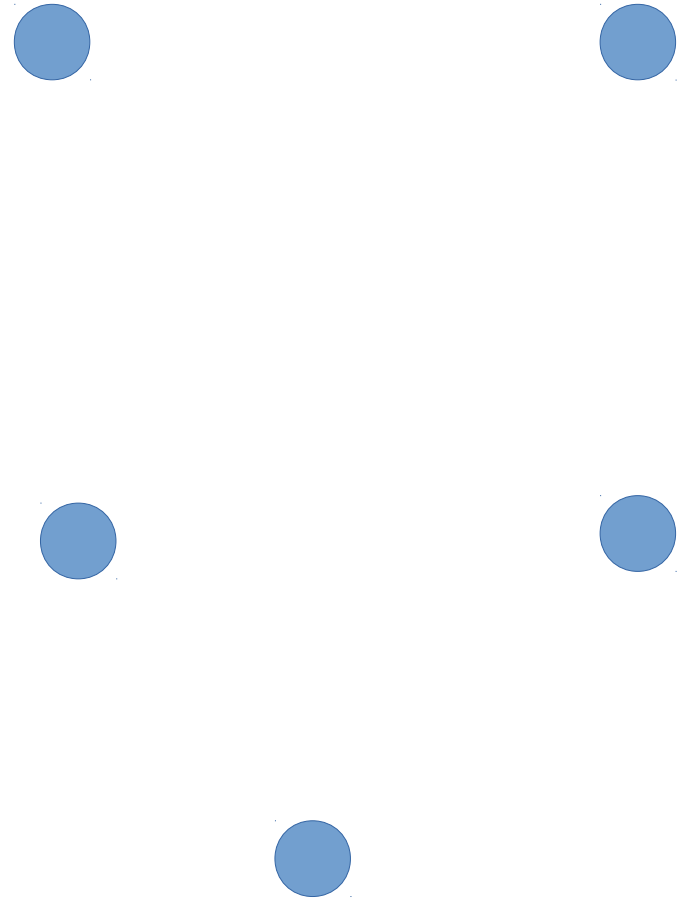
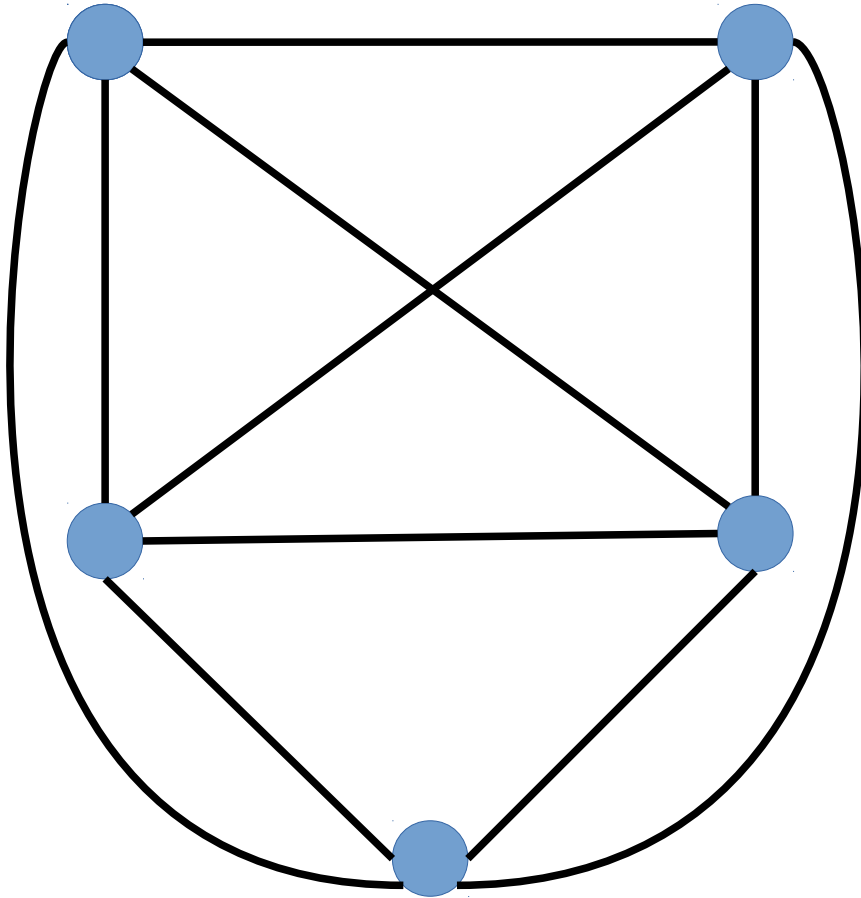


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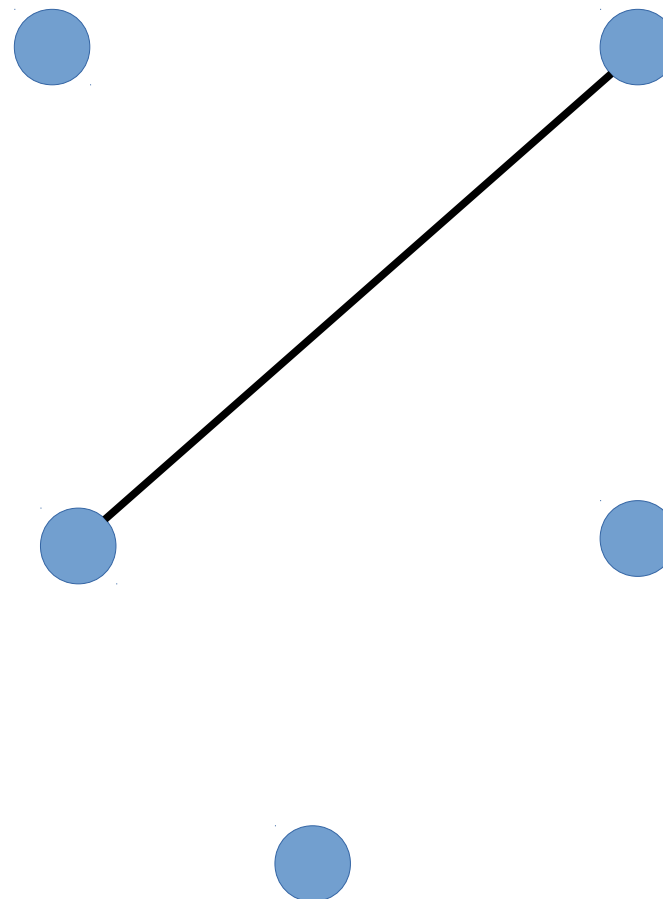
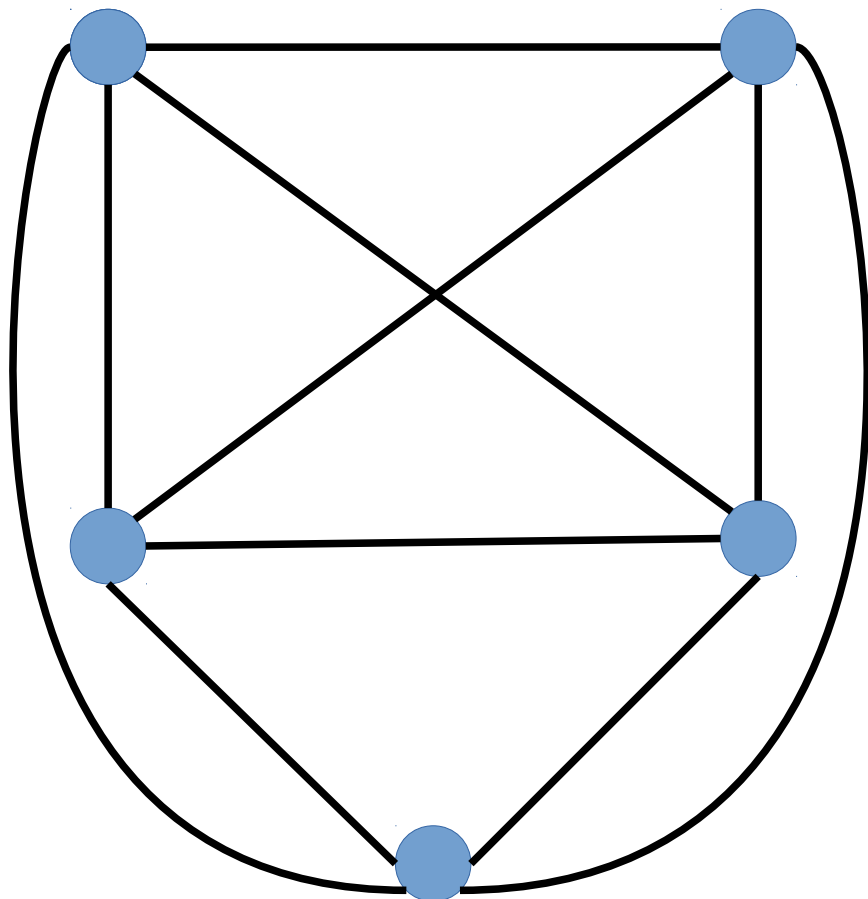


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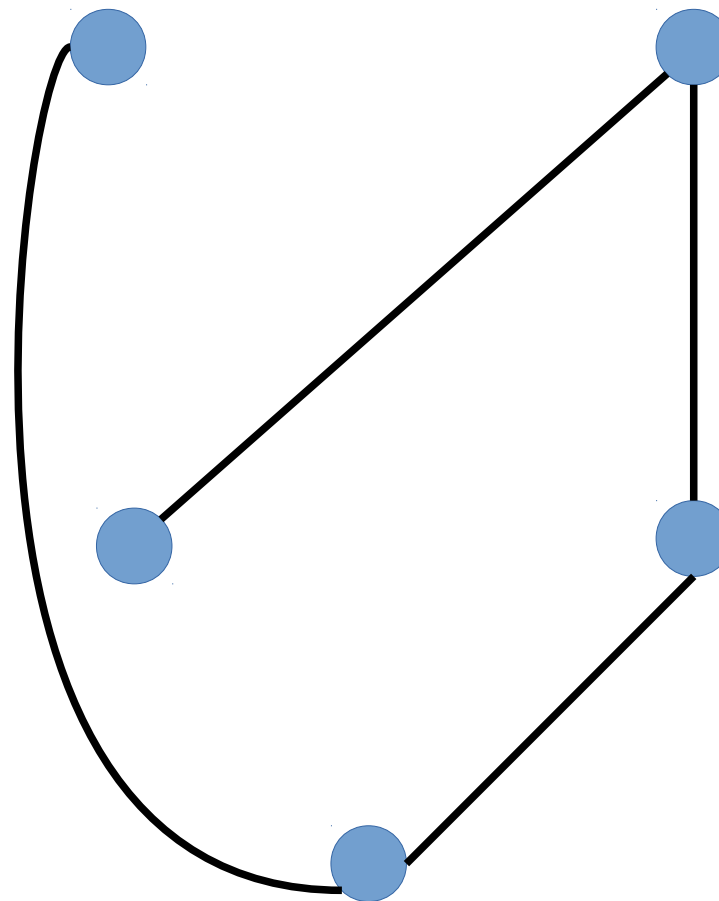
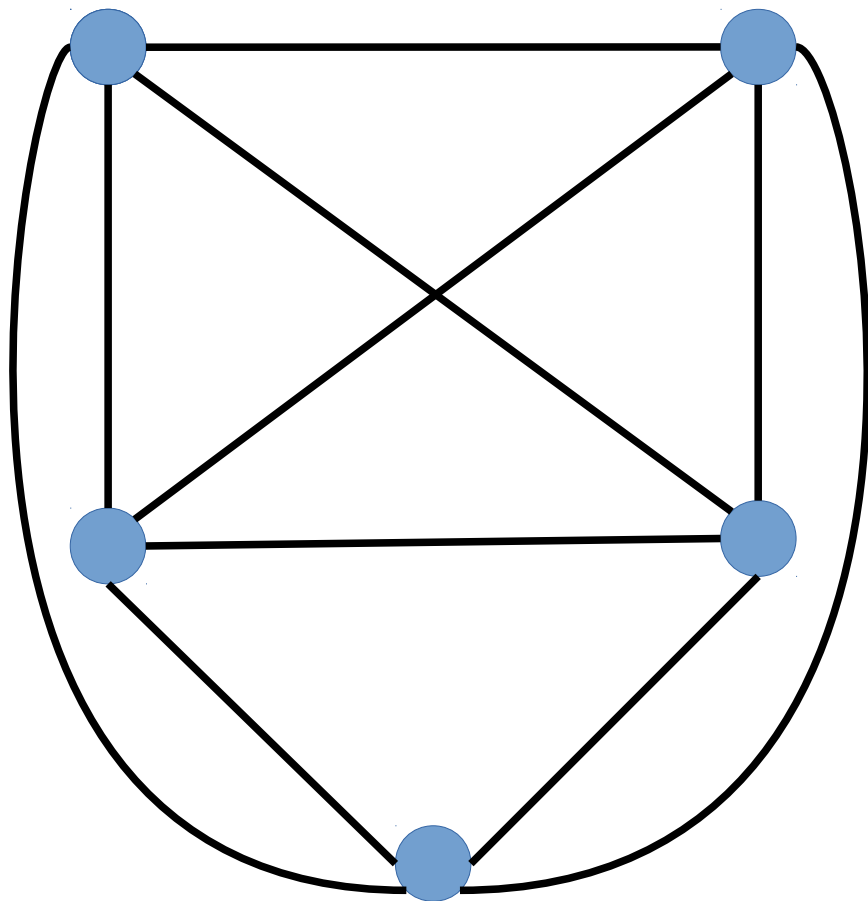


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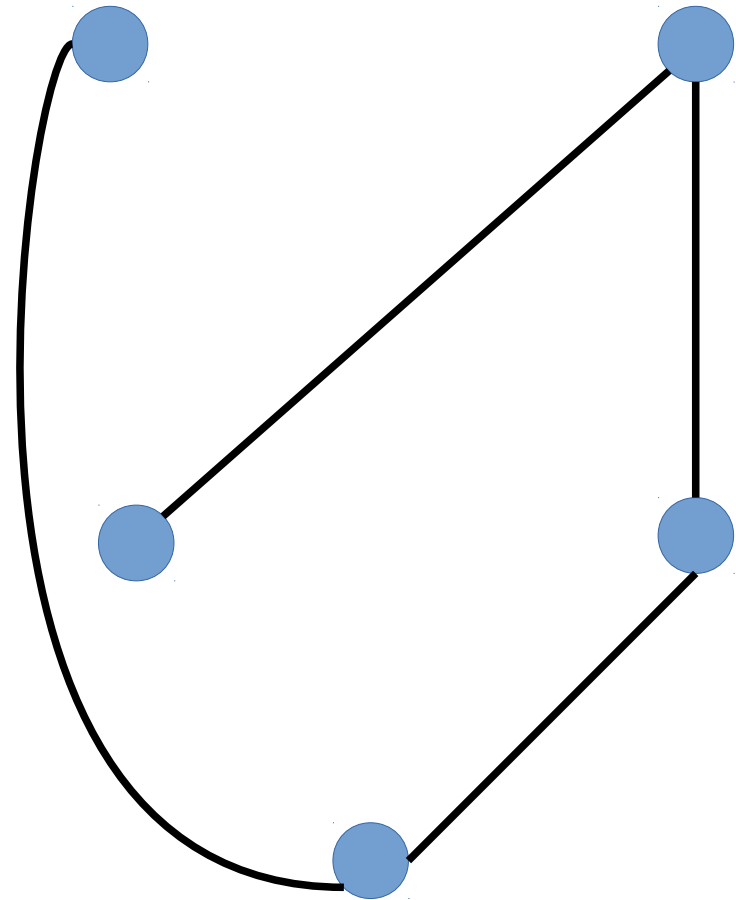
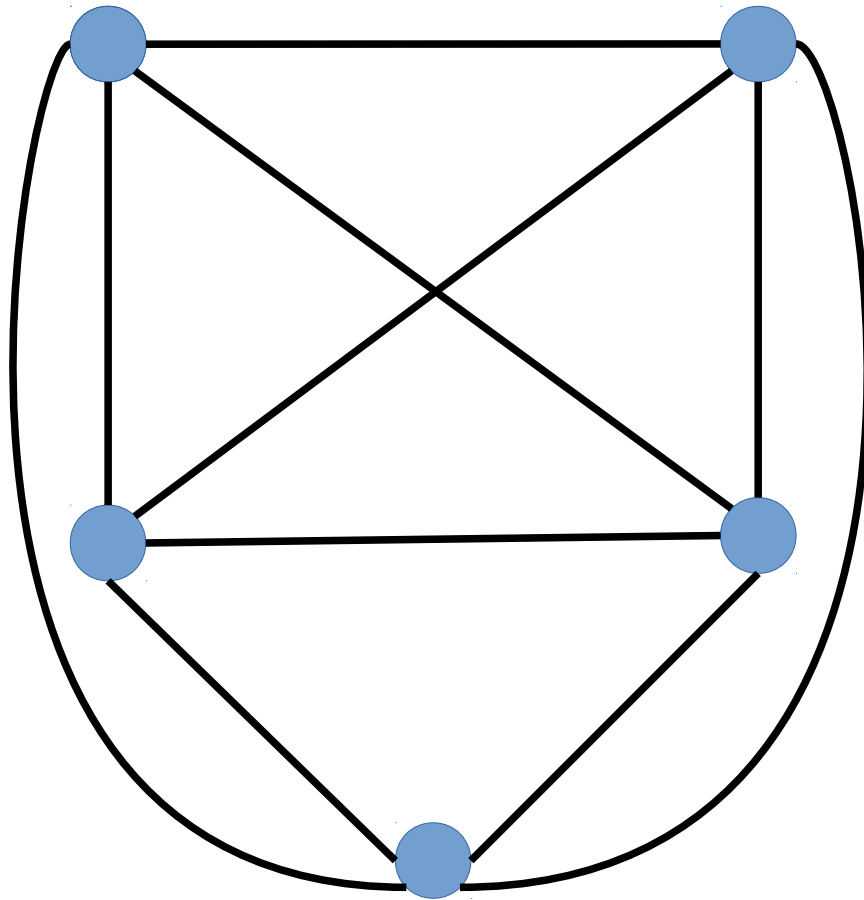


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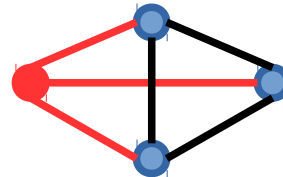


Small diameter but not robust
to link/node failures?



Modeling the "Small World"

- Duncan Watts and Steven H. Strogatz. "Collective dynamics of 'small-world' networks." *Nature* 393.6684 (1998): 440-442.
 - Diameter: length of the longest path
 - Clustering Coefficient: how close are the adjacent vertices of a vertex to a complete graph (clique) if the vertex is removed.
 - Desirable properties: Small Diameter and High Clustering Coefficient





Random Rewiring Procedure

$p=0$

$p=1$

n : number of vertices

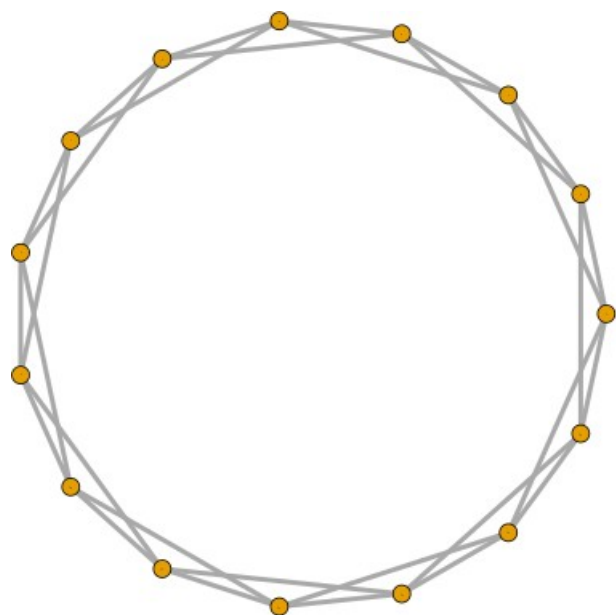
k : degree of each node, i.e., neighbours of a vertex ($n \gg k \gg \ln(n) \gg 1$)

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Random Rewiring Procedure

$n=10, k=4$



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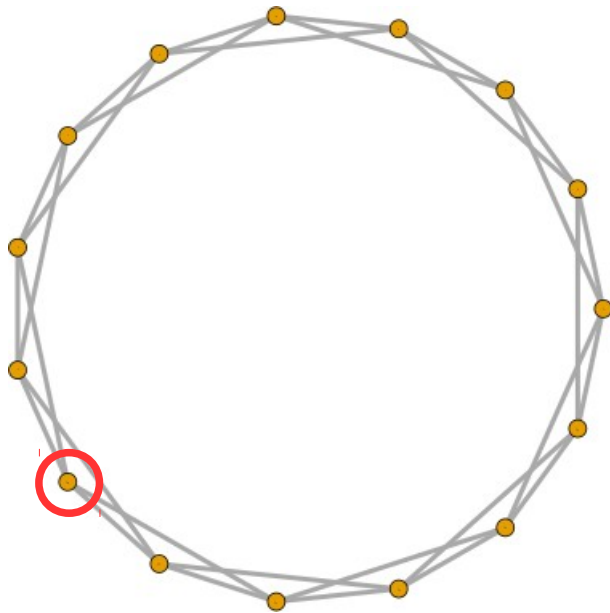
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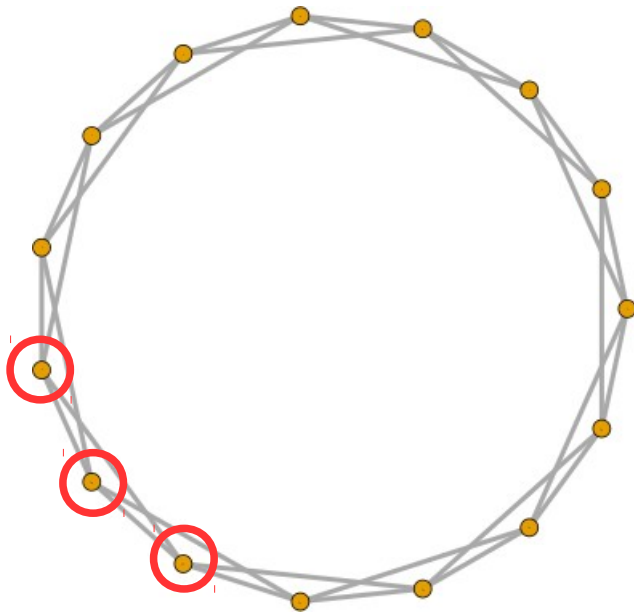
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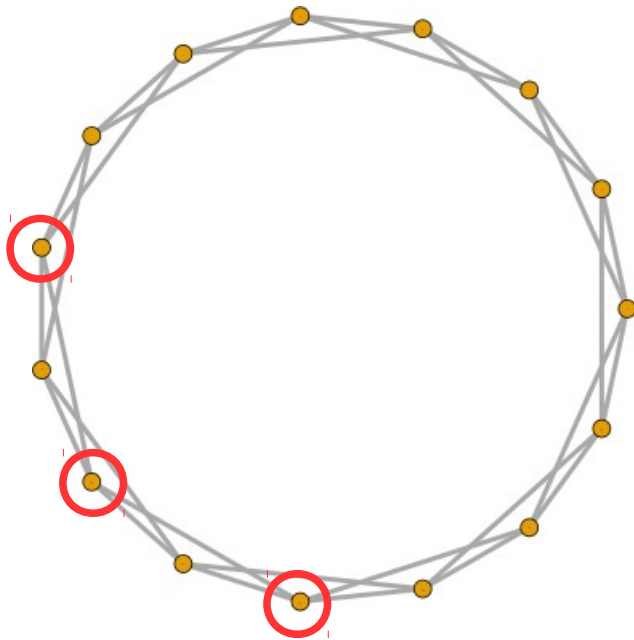
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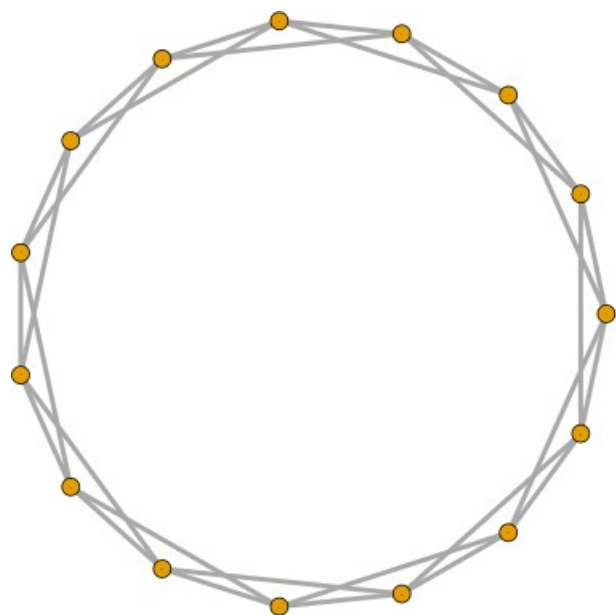
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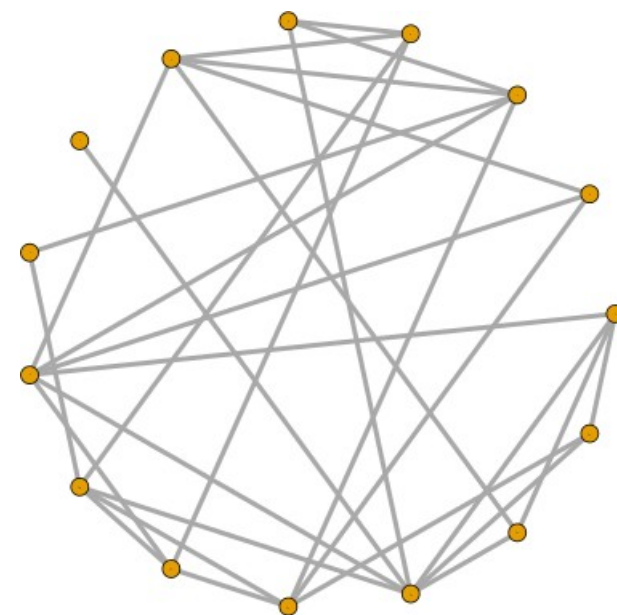


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$p=0$



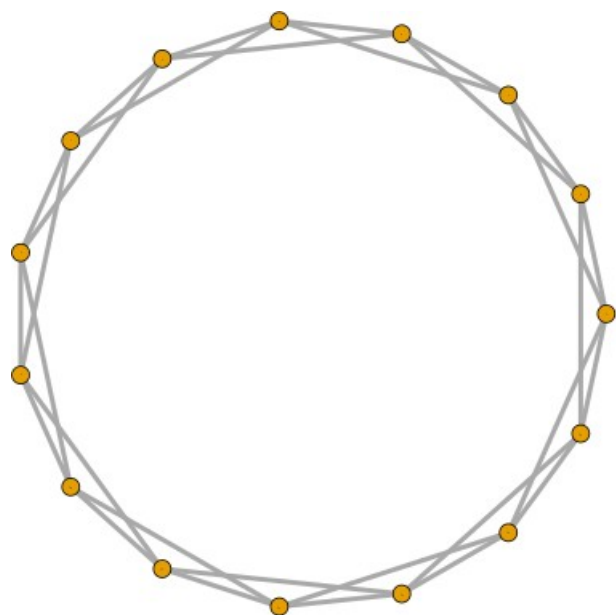
$p=1$

n : number of vertices
 k : degree of each node, i.e., neighbours of a vertex ($n \gg k \gg \ln(n) \gg 1$)
 p : probability of rewiring

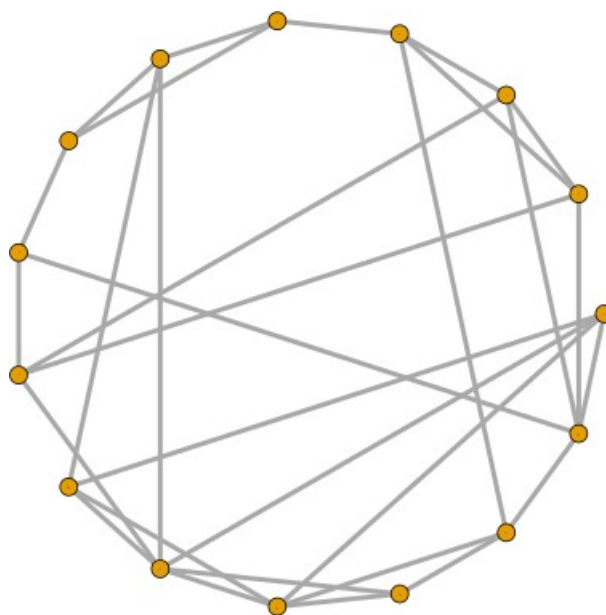


Random Rewiring Procedure

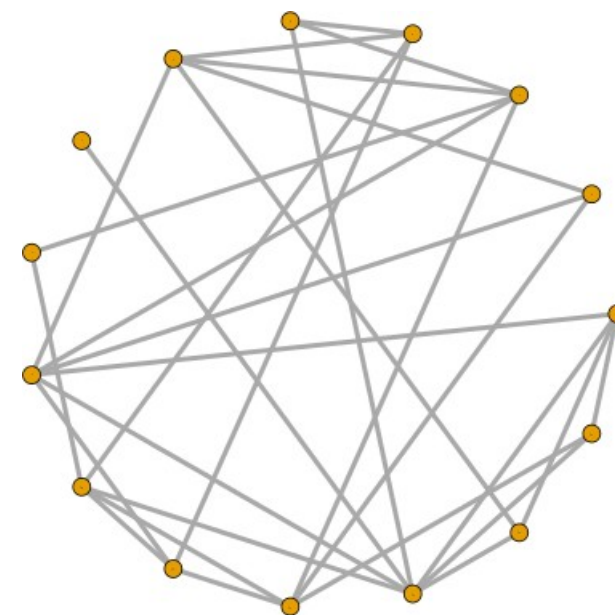
$n=10, k=4$



$p=0$



($p=0.15$)



$p=1$

n : number of vertices

k : degree of each node, i.e., neighbours of a vertex ($n \gg k \gg \ln(n) \gg 1$)

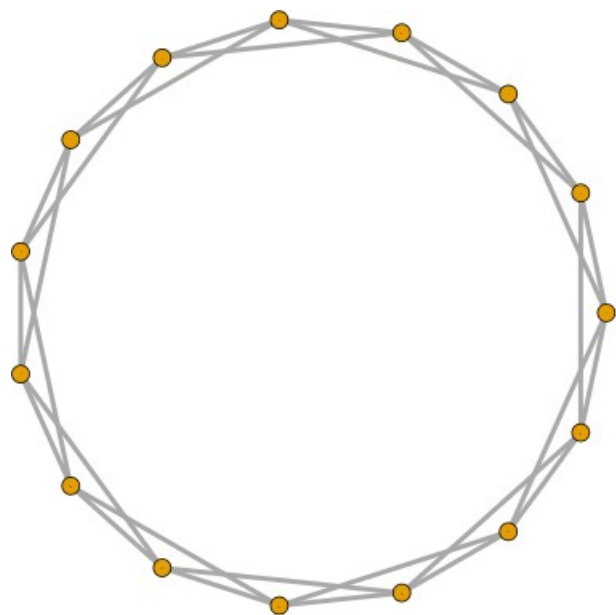
p : probability of rewiring



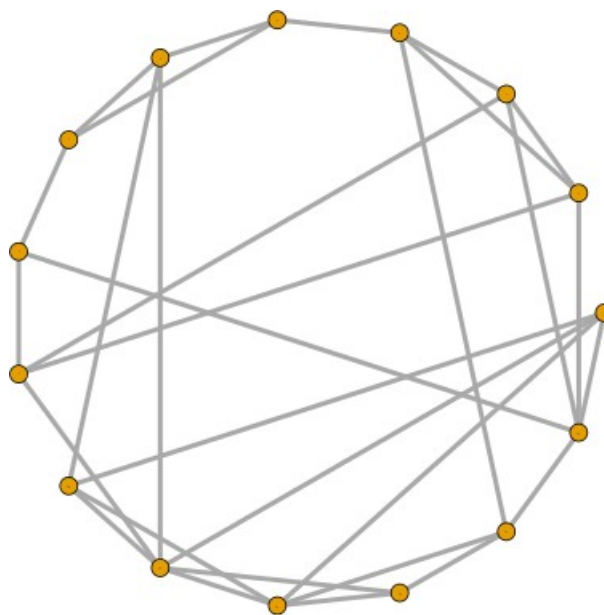
Random Rewiring Procedure

$n=10, k=4$

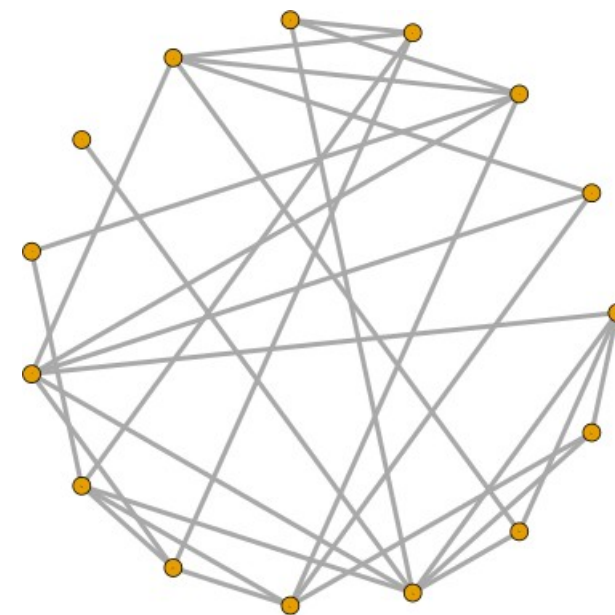
What is the diameter?
What happens if I remove a neighbour?



$p=0$



($p=0.15$)



$p=1$

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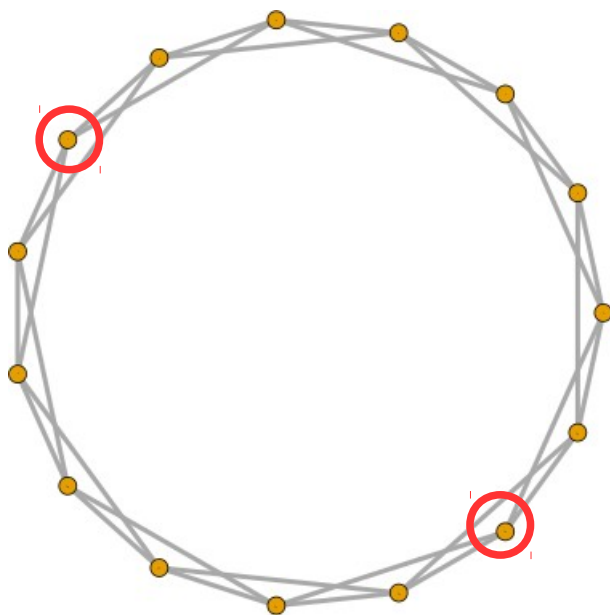
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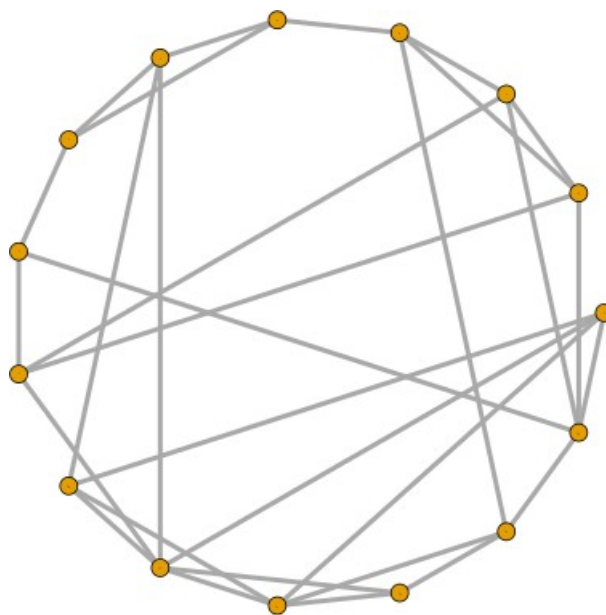
Random Rewiring Procedure

$n=10, k=4$

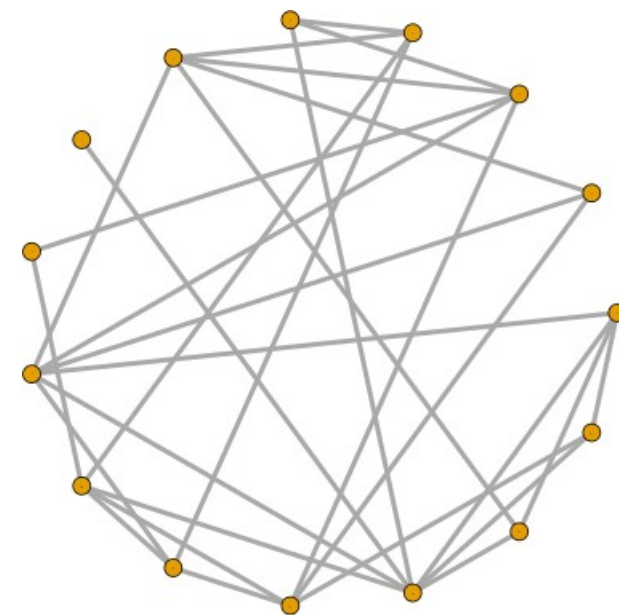
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($p=0.15$)



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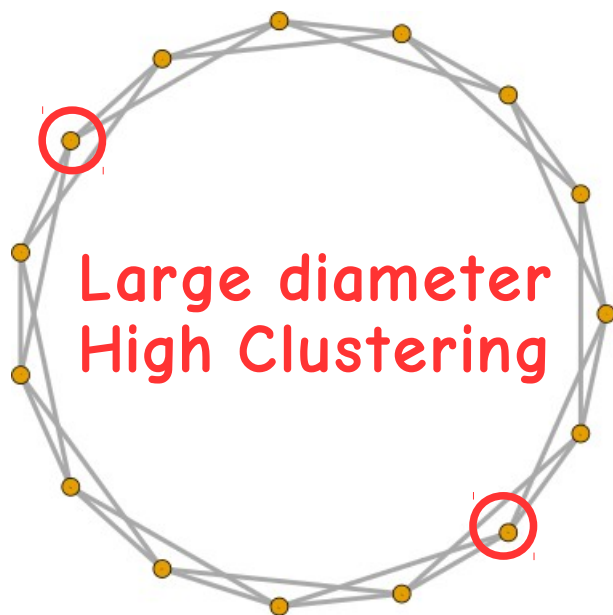
p : probability of rewiring



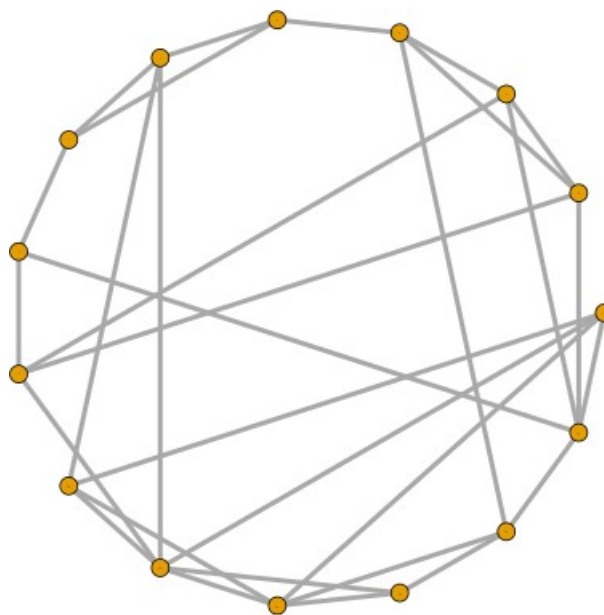
Random Rewiring Procedure

$n=10, k=4$

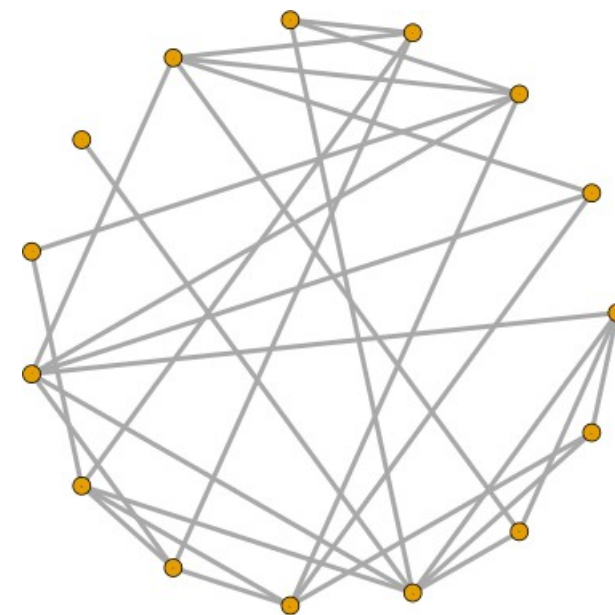
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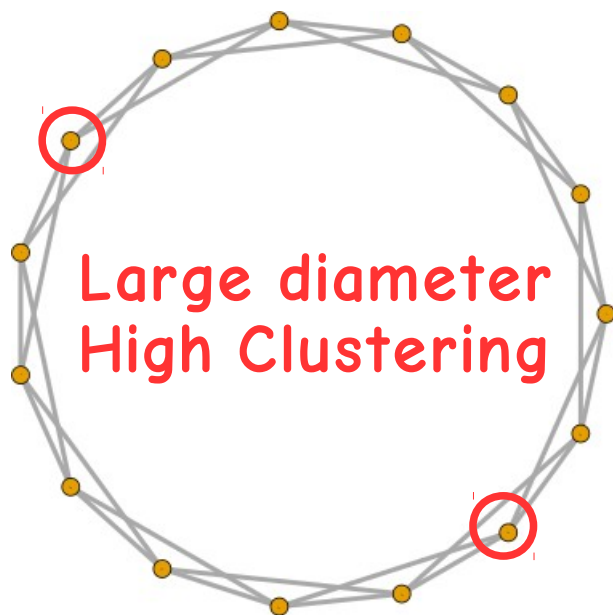
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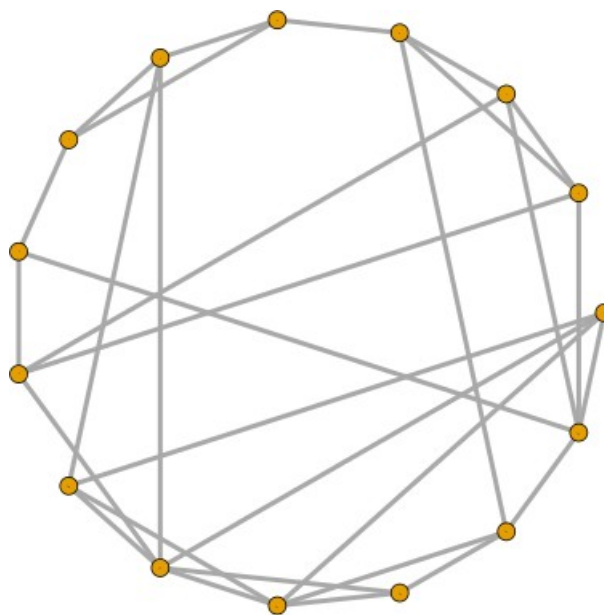
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$n=10, k=4$

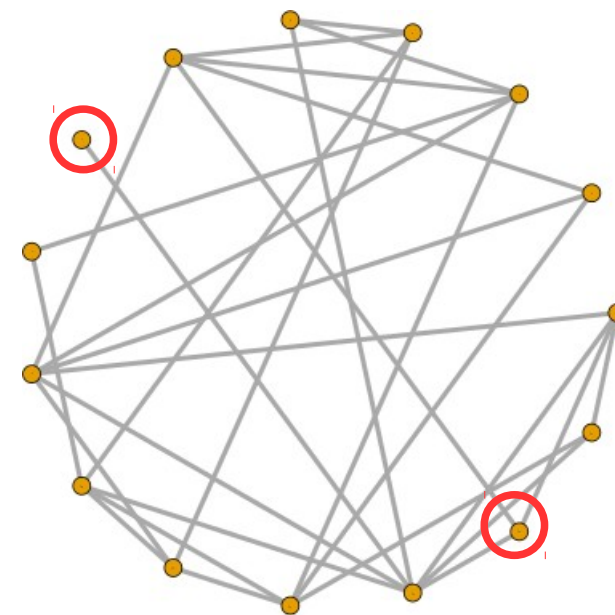
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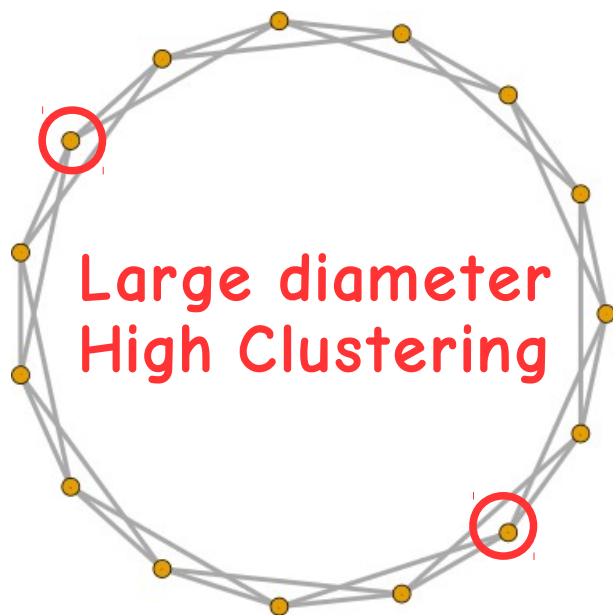
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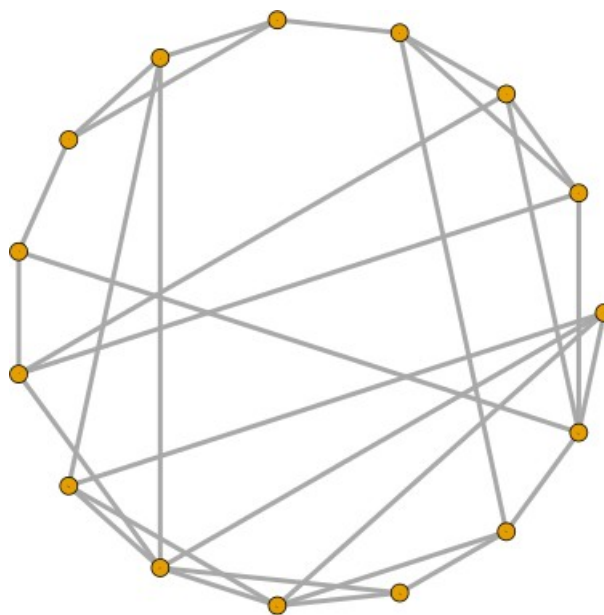
Random Rewiring Procedure

$n=10, k=4$

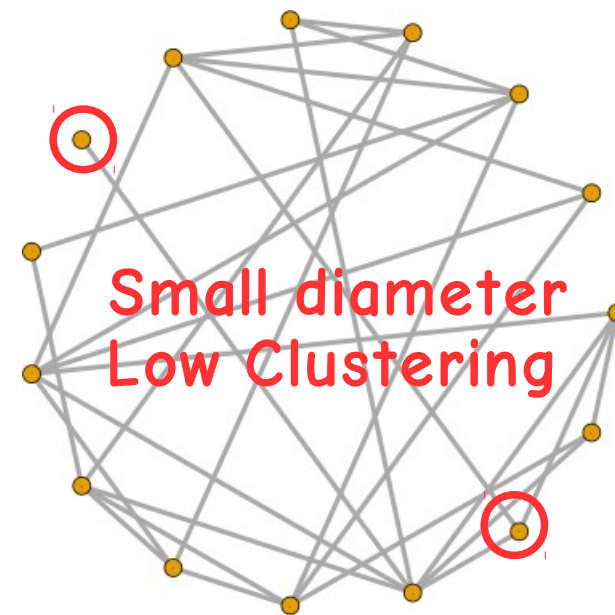
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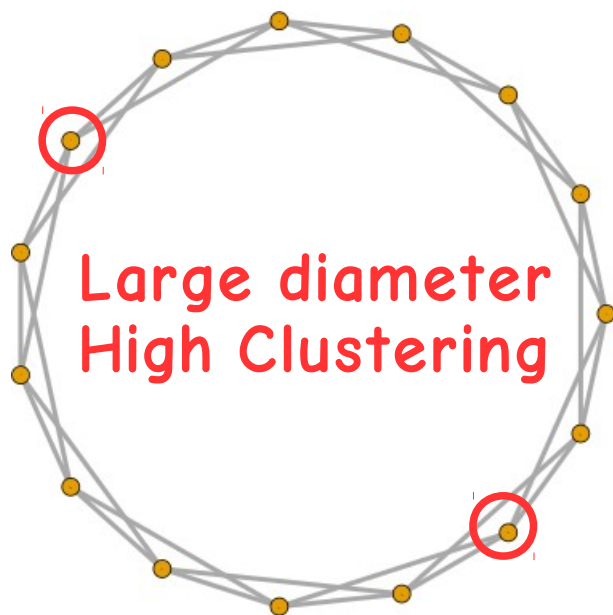
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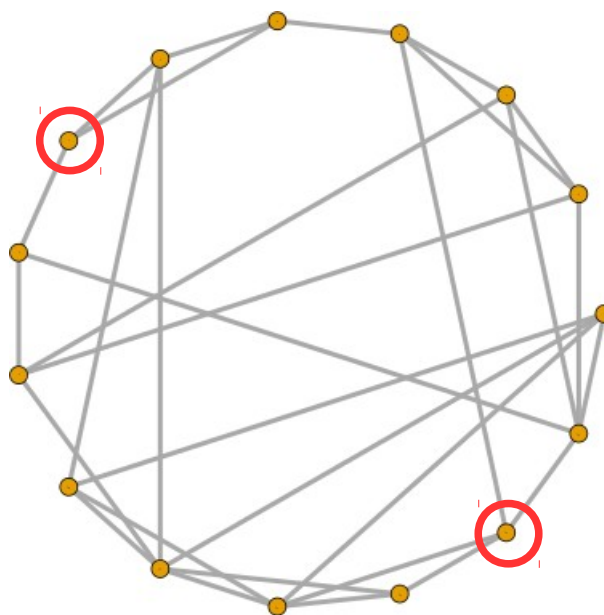
Random Rewiring Procedure

$n=10, k=4$

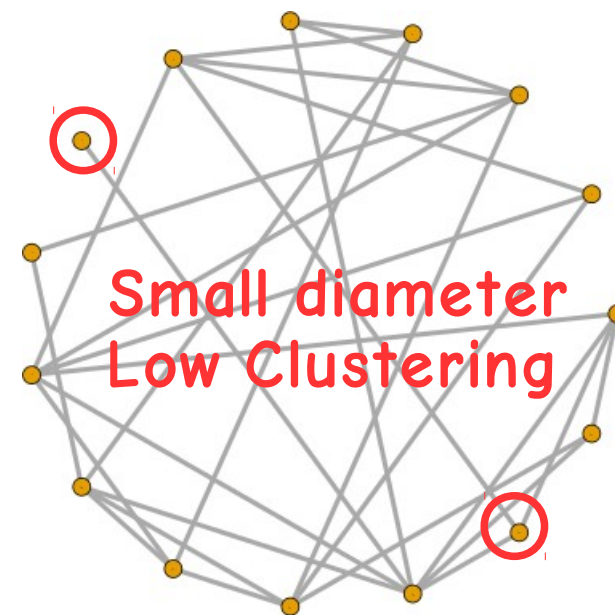
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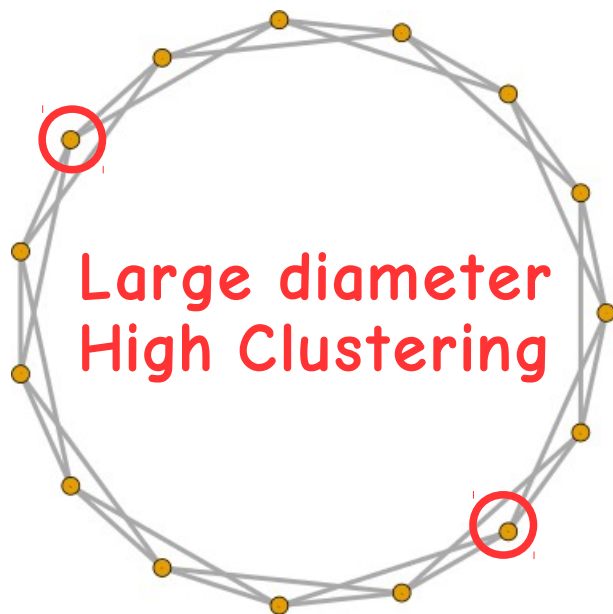
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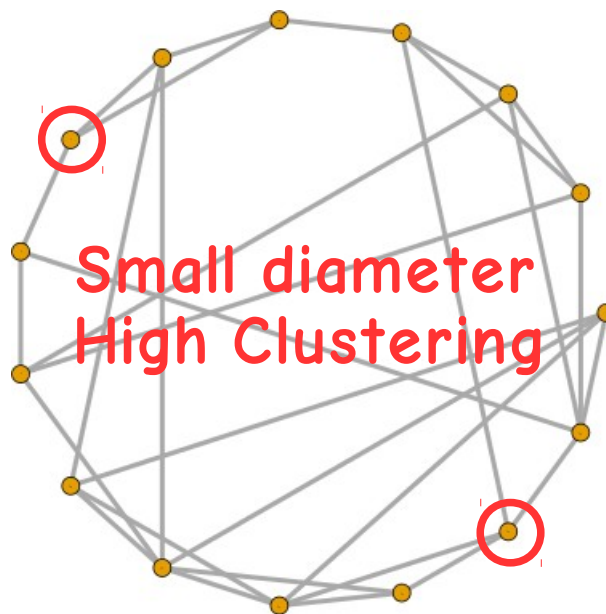
Random Rewiring Procedure

$n=10, k=4$

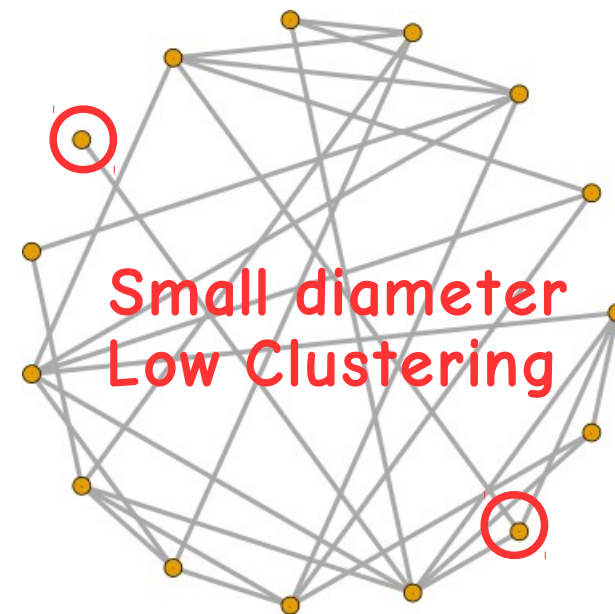
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$(p=0.15)$



$p=1$

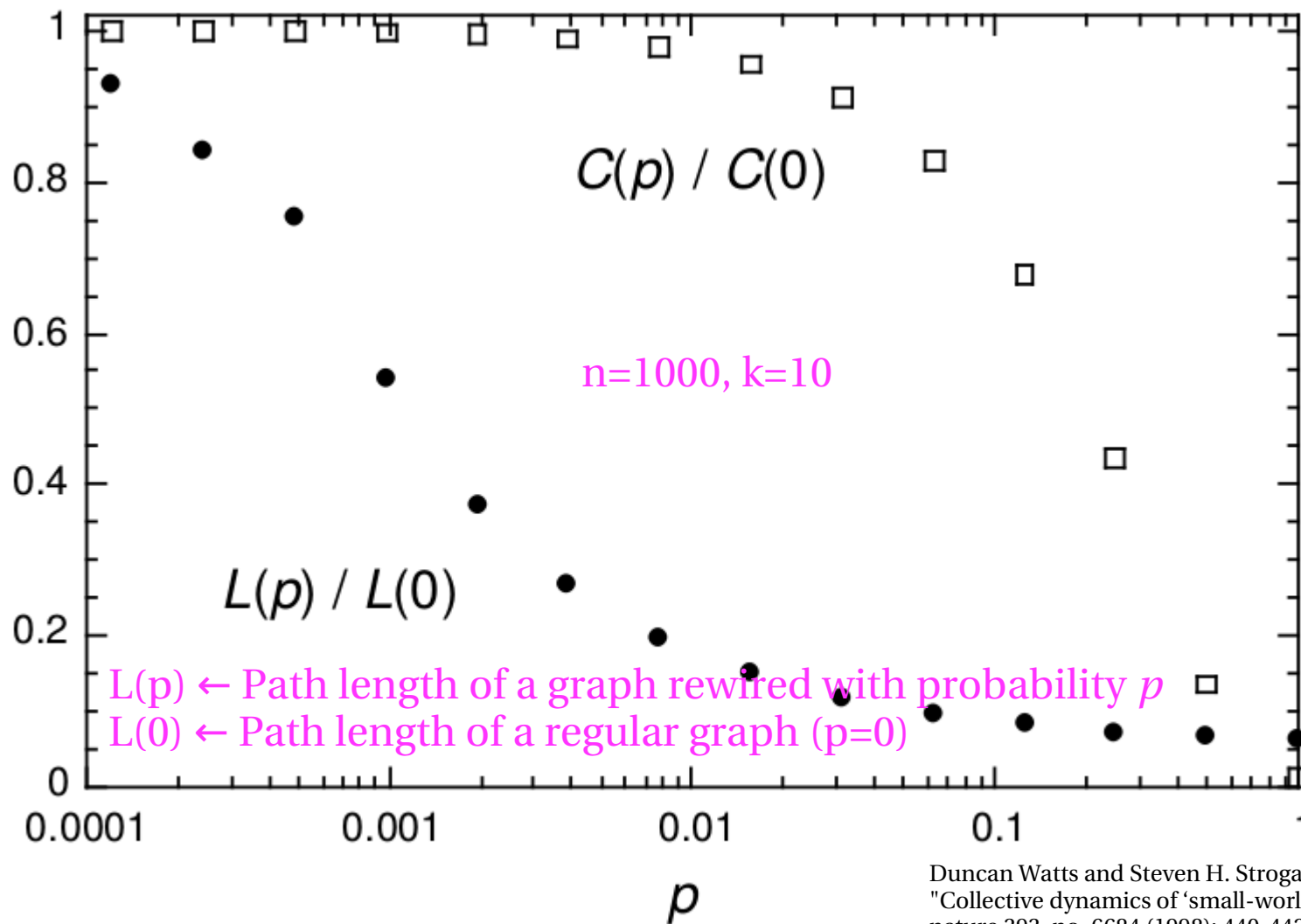
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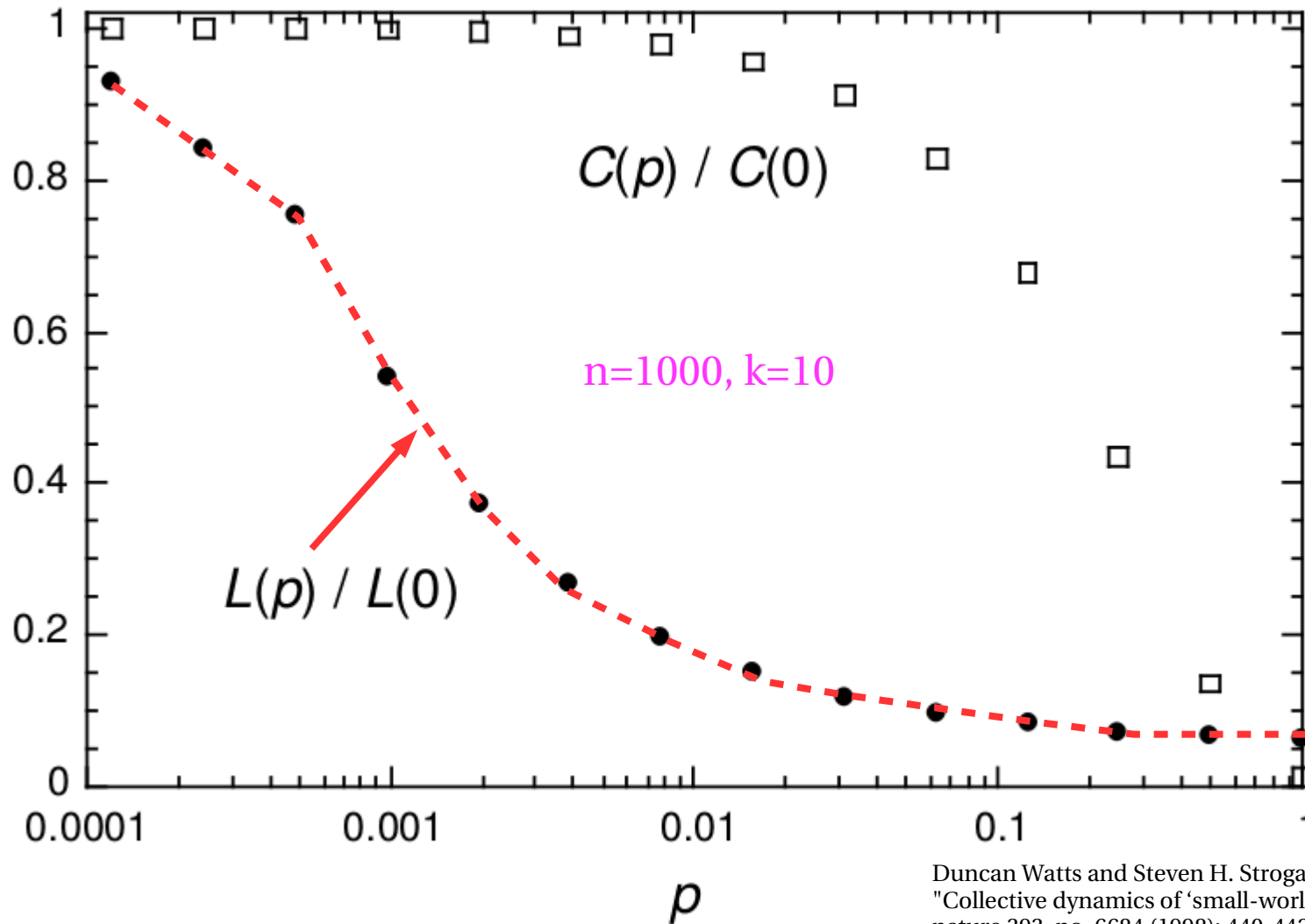


Path Length $L(\cdot)$ and Clustering Coefficient $C(\cdot)$ in Rewired Graphs





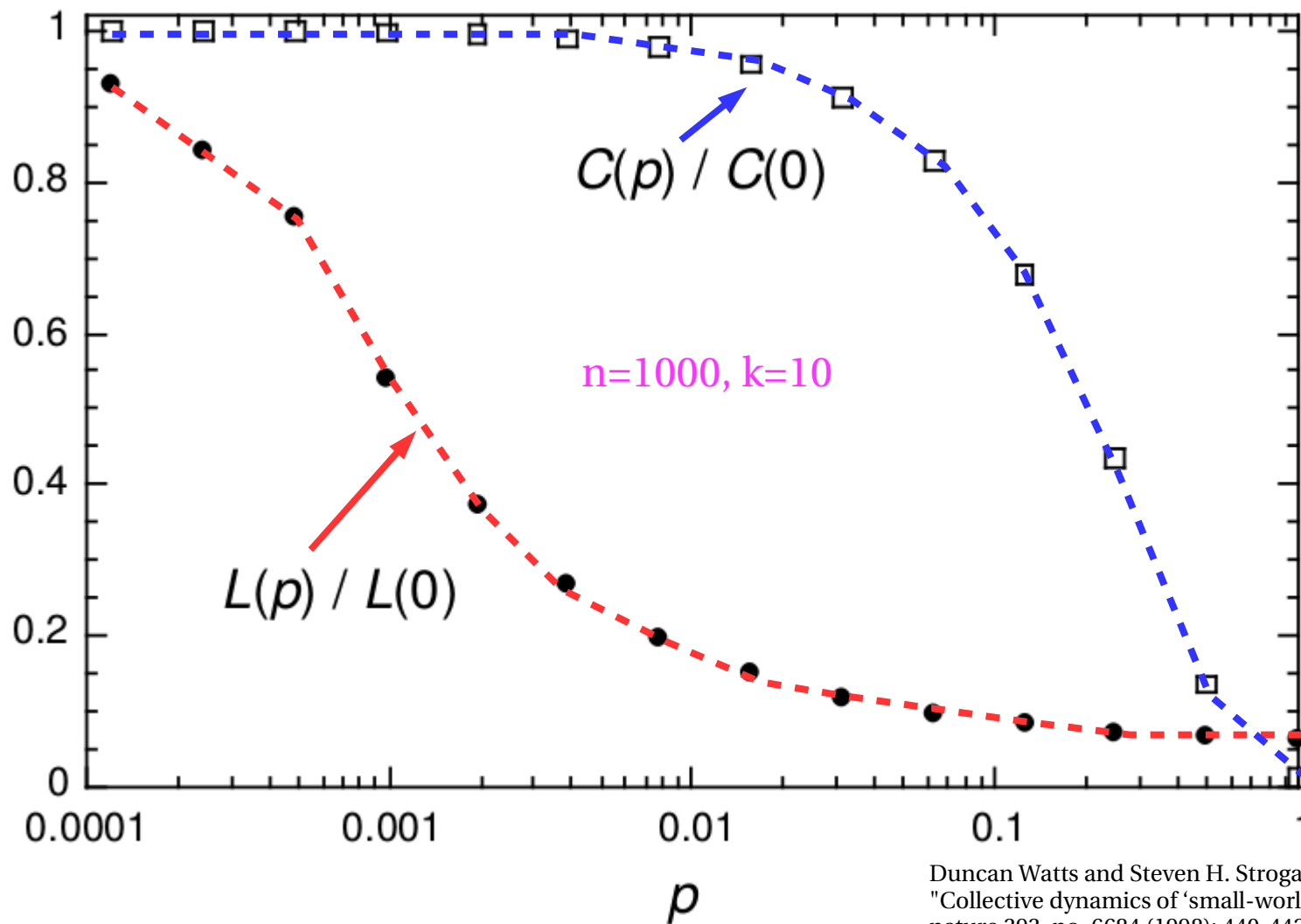
Path Length $L(\cdot)$ and Clustering Coefficient $C(\cdot)$ in Rewired Graphs



Duncan Watts and Steven H. Strogatz.
"Collective dynamics of 'small-world' networks."
nature 393, no. 6684 (1998): 440-442.



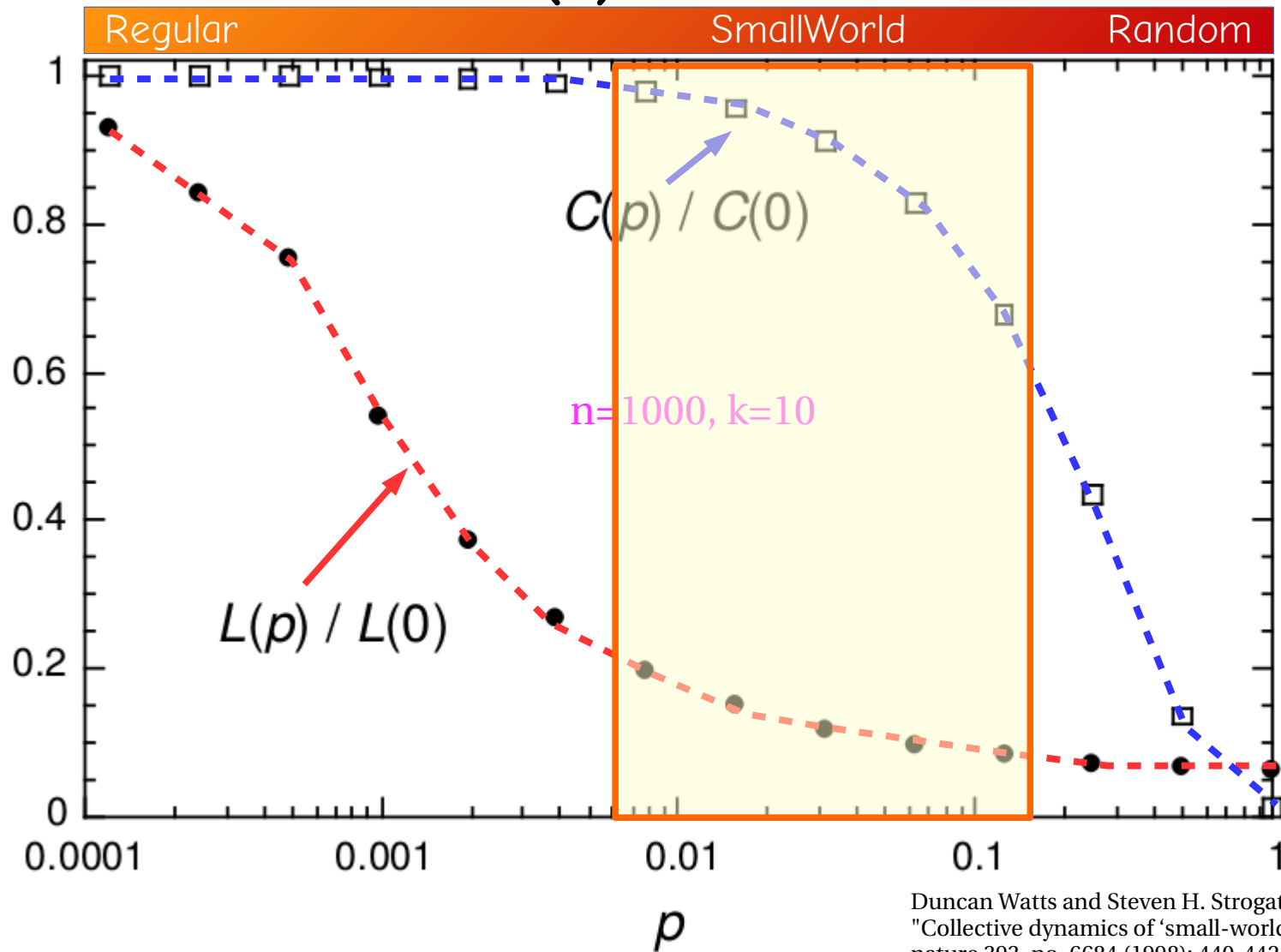
Path Length $L(\cdot)$ and Clustering Coefficient $C(\cdot)$ in Rewired Graphs



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Path Length $L(\cdot)$ and Clustering Coefficient $C(\cdot)$ in Rewired Graphs



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Is Small-World Networks the right model?



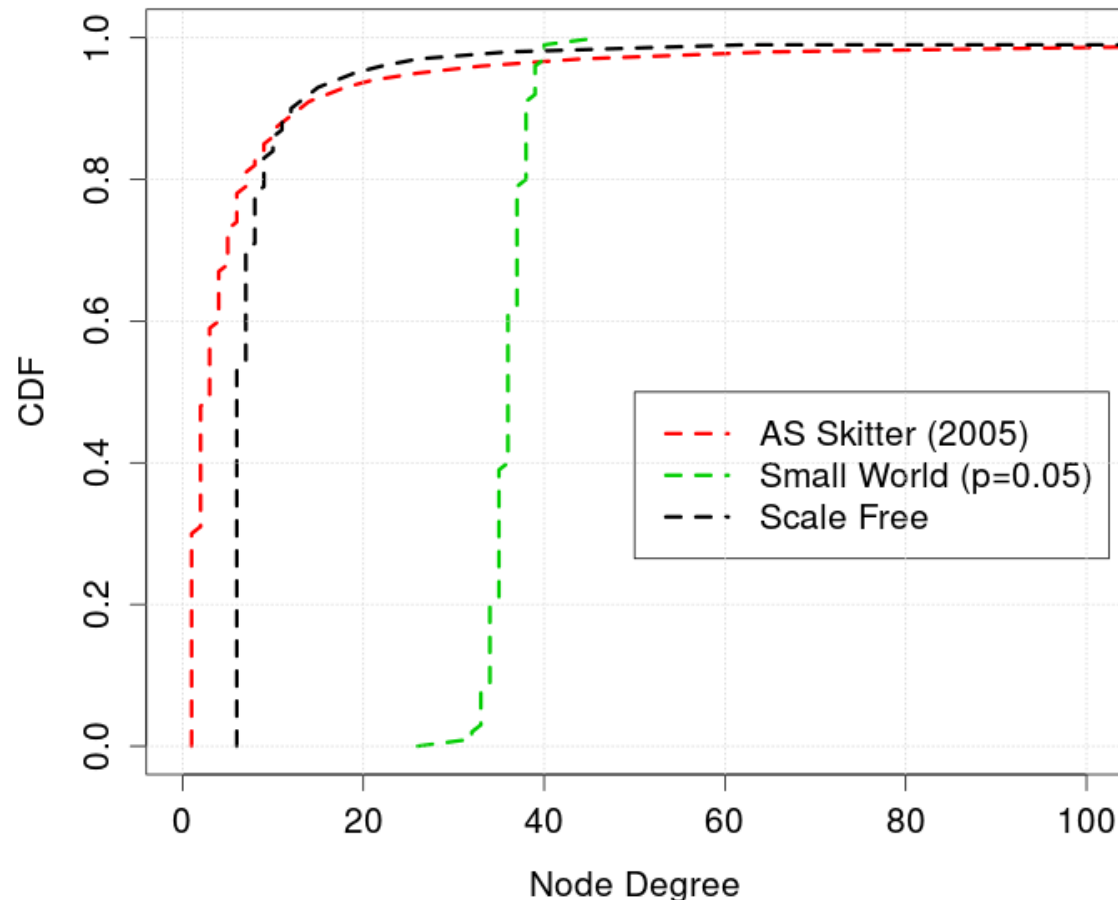
Is Small-World Networks the right model?

- What happens in dynamic networks whose members/vertices change with time?
- With which vertices of a graph do new arrivals prefer to attach?
- Is the the development of large networks governed by a robust self-organizing phenomena?
- What about heterogeniety in type of elements in and the degree distribution?
- ...



What about degree distribution?

- Do small-world/random-graph models capture the presence of hubs?





Assumptions of Random Graphs and Small-World

- Fixed number of nodes that are either randomly connected (Random Graphs) or randomly rewired (Small-World)
- Probability that two vertices are connected is random and uniform

Barabási, Albert-László, and Réka Albert.
"Emergence of scaling in random networks."
Science 286, no. 5439 (1999): 509-512.



Evaluation Methodology

- 1) Make observations (conduct measurement studies)
- 2) Build model to explain observations
 - Choose the right level of granularity (zoom level)
 - Strip the problem to a simple form
 - Attempt to formulate the problem and model the system
- 3) Validate model
 - Reproduce observations/measurements
 - Explain observations
- 4) Revisit step 2 (and 1) to improve understanding



Summary

- Large number of interacting elements
- System adapts and evolves
- Although elements follow simple rules, the system behaves in a **complex** manner
- System behavior is an outcome of the interaction between the elements, so studying elements in isolation will not provide detailed insights on system behavior
- Similar processes shape networks therefore many networks share similar characteristics



Complex Networks

Overlay
Networks





References



Important Papers

- Stanley Milgram. "**The small world problem.**" *Psychology today* 2.1 (1967): 60-67
- Duncan Watts and Steven H. Strogatz. "**Collective dynamics of 'small-world' networks.**" *Nature* 393.6684 (1998): 440-442.
- Barabási, Albert-László, and Réka Albert. "**Emergence of scaling in random networks.**" *Science* 286, no. 5439 (1999): 509-512.
- Albert, Réka, and Albert-László Barabási. "**Statistical mechanics of complex networks.**" *Reviews of modern physics* 74.1 (2002): 47.
- Mitzenmacher, M. (2004). "**A brief history of generative models for power law and lognormal distributions.**" *Internet mathematics*, 1(2), 226-251.



Sources for these slides

- Sasu Tarkoma "Overlay and P2P Networks", 2015
- Arnaud Legout. "Peer-to-Peer Applications : From BitTorrent to Privacy", January 2012.
- Jari Saramäki "Introduction to Complex Networks", 2010.
- Datasets from Stanford Network Analysis Project (SNAP)