

1. Show that in **G0ip** without weakening $A \supset (B \supset A)$ is not derivable. Show that in **G0ip** without contraction $(A \supset (A \supset B)) \supset (A \supset B)$ is not derivable.
2. Show that generalized axioms $A, \Gamma \Rightarrow \Delta, A$ are derivable in **G3cp**.
3. Using the calculus **G3cp** find conjunctive normal form for the following formulae
 - (a) $(A \& B) \supset (A \supset (B \& \sim A))$
 - (b) $(A \vee (\sim B \& B)) \& \sim(B \& \sim C)$
 - (c) $(A \vee \sim \sim B) \supset (\sim B \supset A)$
4. Complete the proof of height-preserving contraction for **G3cp** (Theorem 3.2.2 on page 53 of the book) presented in the last lecture.