



Spatial Data Mining Co-location rules

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Background: frequent sets

- Frequently co-occurring items in transaction data
 - Finite set of disjoint transactions
 - E.g. customer data derived from supermarket cash registers
 - Well-known problem since the early 1990's
- Next step: association rules
 - $\{A_1, \dots, A_n\} \Rightarrow B$
 - Confidence: $\hat{P}(B|\{A_i\}) = \frac{|\{A_i, B\}|}{|\{A_i\}|}$
 - Support: $\hat{P}(\{A_i, B\}) = \frac{|\{A_i, B\}|}{|X|}$



Frequent sets: Apriori

- Classic algorithm for finding frequent sets
 - Two independent formulations in 1993–94
- Start with all pairs of items that are sufficiently frequent
- As long as there are sets of size $n - 1$,
 - Generate as candidates those sets of size n whose subsets of size $n - 1$ are frequent
 - Accept as frequent those candidates that are in fact frequent



Apriori: example

- Transaction data
 - baby_food beer milk
 - baby_food beer mustard sausage
 - baby_food bread butter
 - baby_food bread butter cigarettes milk
 - baby_food bread diapers milk sausage
 - baby_food bread milk
 - baby_food butter candy cigarettes diapers
 - baby_food candy diapers mustard
 - beer bread butter mustard sausage
 - beer bread candy
 - beer bread milk mustard sausage
 - beer butter sausage
 - candy cigarettes



Apriori: example

- Limit: frequency ≥ 0.2
- 1st iteration: frequent items
 - {baby_food:0.62, beer:0.46, mustard:0.31, bread:0.54, butter:0.38, candy:0.31, cigarettes:0.23, diapers:0.23, milk:0.38, sausage:0.38}
- 2nd iteration: pairs
 - Candidates: all pairs of the above
 - Frequent: {(baby_food,bread):0.31, (baby_food,diapers):0.23, (baby_food,milk):0.31, (beer,bread):0.23, (beer,mustard):0.23, (beer,sausage):0.31, (bread,butter):0.23, (bread,milk):0.31, (bread,sausage):0.23, (mustard,sausage):0.23}



Apriori: example

- 3rd iteration: triplets
 - Candidates: {(baby_food,bread,milk), (beer,bread,sausage), (beer,mustard,sausage)}
 - Frequent: {(baby_food,bread,milk):0.23, (beer,mustard,sausage):0.23}
- 4th iteration: quadruplets
 - No more candidates



Association rules

- The example discovered some frequent sets
- Association rules can be derived from those
 - Sets (beer,mustard,sausage):0.23 and (beer,sausage):0.31
 - Rule (beer,sausage) \Rightarrow mustard
 - Support: 0.23
 - Confidence: $\frac{0.23}{0.31} \approx 0.7$
 - Sets (baby_food,diapers):0.23 and (diapers):0.23
 - Rule diapers \Rightarrow baby_food
 - Support: 0.23
 - Confidence: 1



From transactions to spatial data

- Transactions are disjoint
- Spatial co-location is not
- Something must be done
- Three main options
 1. Divide the space into areas and treat them as transactions
 2. Choose a reference point pattern and treat the neighbourhood of each of its points as a transaction
 3. Treat all point patterns as equal



Window-centric co-location mining

- Divide the space into areas
 - Create a uniform grid that covers the space
 - See which phenomena occur in each grid cell
 - Treat grid cells as transactions
- Easy: just use transaction-based algorithms
- Useful for large-scale co-location rules
 - Correlations between the distributions of the different phenomena on e.g. national scale
- Not very useful for small-scale co-locations
 - Noise level increases as the size of grid cells decreases



Reference feature centric co-location mining

- Choose one point pattern as the reference
- Find the neighbourhood of each point in the reference pattern
- Treat these as transactions
- Again, relatively easy to use transaction-based algorithms
- Useful for applications where there is an obvious choice for the reference phenomenon
- Not very useful when there is no such candidate



Event-centric co-location mining

- Large number of different point patterns
 - Each describe the existence of a phenomenon
 - These phenomena are considered equal
- Transaction-based algorithms not immediately applicable
- More general than the other two approaches
- Still, only binary phenomena
 - Each point describes the existence of something
 - More detailed properties – e.g. temperature scale – must be discretised as a preprocessing step



Mining without transactions

- Possible to adapt Apriori for event-centric co-location mining
 - Needed: a measure for co-occurrence
 - Apriori uses frequency of (A,B)
- Find co-occurring pairs
- Use an Apriori-derivative to find larger sets



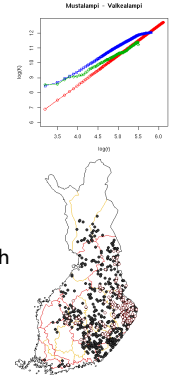
Measuring spatial attraction

- Spatial statistics: the K function
- In its basic form, for a single point pattern, $\lambda K(h) = E(\text{number of points within radius } h \text{ of a random point})$
 - If no spatial correlation, $K(h) = \pi h^2$
 - Attraction: $K(h) > \pi h^2$
 - Repulsion: $K(h) < \pi h^2$
- Correlation between two point patterns:
 $\lambda_2 K_{12}(h) = E(\text{number of points of type 2 within radius } h \text{ of a random point of type 1})$



Combining K and Apriori

- Calculate the K_{12} function for each pair of point patterns
- Use these as the measure for co-occurrence
 - Accept those sets where K_{12} for each pair exceeds a set limit
- Example: two place names with significant attraction
Mustalampi 'Black Pond'
Valkealampi 'White Pond'



Apriori and the K function: example

- Raw data: Finnish lake names
 - Preprocessing: select those with ≥ 20 occurrences
 - This gives 331 names and 19 230 lakes
- Criterion: $K_{12}(1\ 000) > 20\ 000\ 000\ \pi$ (units: metres)

Set size	Number of sets	Distinct pairs
4	2	12
3	104	255
2	638	638
2-4	744	903



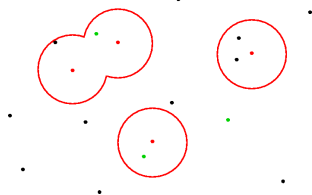
Apriori and the K function: results

- Some interesting co-location patterns:
 - (*Myllyjärvi* 'Mill Lake', *Kirkkojärvi* 'Church Lake')
 - (*Kaitajärvi* 'Narrow Lake', *Hoikkajärvi* 'Thin Lake')
 - (*Mäntyjärvi* 'Pine Lake', *Mäntylampi* 'Pine Pond')
 - (*Iso Haukilampi* 'Greater Pike Pond', *Pieni Haukilampi* 'Lesser Pike Pond')
 - (*Ahvenlampi* 'Perch Pond', *Haukilampi* 'Pike Pond')
 - (*Alalampi* 'Low Pond', *Keskilampi* 'Middle Pond', *Ylilampi* 'High Pond')
 - Also a lot of noise
- Several co-location patterns can be interpreted in terms of linguistics
- Insight into properties of the name system and the name-giving process



Co-locations without K

- K function is
 - statistically justifiable
 - computationally expensive
- Simpler method: frequency of points
 - in the neighbourhood of points in another pattern
 - across the entire space



Points in a neighbourhood

- If point patterns A and B are independent,
 - The neighbourhood of the A points is a random sample of B points
 - The number of B points $\sim \text{Poisson}(\lambda)$, where $\lambda =$ the number of all points in the neighbourhood \times the overall frequency of B points
- For larger sets, select those points of type B whose neighbourhood contains points $A_i, \forall i$
 - If the point patterns are independent, this is still a random sample of B
 - This gives an association rule of $A_i \Rightarrow B$
- Assumptions
 - All point patterns (A, B, \dots) fundamentally similar
 - The point patterns do not have internal spatial correlation



Apriori and neighbourhoods

- Again, possible to adapt an Apriori-like algorithm
- Compute co-location pairs
- As long as there are co-location rules of size $n - 1$,
 - Generate candidates of size n
 - Accept those candidates that fulfill the criteria
- Problem: checking the neighbourhoods
 - Spatial operations are expensive



Minimising spatial operations

- In a database environment, spatial queries can be expensive
- Fortunately, they are not required all the time
- Sufficient to compute neighbourhoods once
 - Create a new database table that contains
 - Point-id
 - Which point pattern this one belongs to
 - Which point patterns have instances in the neighbourhood of this point
 - This table is sufficient for checking the candidates
 - Not necessary to do spatial queries in all iterations



Further development

- This is just a starting point for co-location mining
- Further optimisations are possible
 - Fine-tuning of Apriori-based algorithms
 - Different approaches
- The next three sessions will touch on these issues



Revised schedule Week 12

- 19.3. Huang & al. 2004: Discovering Colocation Patterns from Spatial Data Sets: A General Approach
Joona Lehtomäki
- Salmenkivi 2006: Efficient Mining of Correlation Patterns in Spatial Point Data
Daniela Hellgren
- 22.3. Yoo & al. 2006: A Joinless Approach for Mining Spatial Colocation Patterns (TBD)
- Huang & al. 2005: Can We Apply Projection Based Frequent Pattern Mining Paradigm to Spatial Colocation Mining?
Zoltán Bójas



Revised schedule Week 13

- 26.3. Xiong & al. 2004: A Framework for Discovering Co-location Patterns in Data Sets with Extended Spatial Objects
Paula Silvonon
- Yoo & al. 2006: Discovery of Co-evolving Spatial Event Sets
Timo Nurmi
- 29.3. Introduction: spatial clustering



Revised schedule Week 14

- 2.4. Tung & al. 2001: Spatial Clustering in the Presence of Obstacles
Milan Magdics
- Wang & Hamilton 2003: DBRS: A Density-Based Spatial Clustering Method with Random Sampling
Bence Novák
- Easter break



Revised schedule

Week 16

- 16.4. Introduction: spatial modelling
- 19.4. Kavouras 2001: Understanding and Modelling Spatial Change
Sandeep Puthan Purayil
 - Kazar & al. 2004: Comparing Exact and Approximate Spatial Auto-Regression Model Solutions for Spatial Data Analysis
Magnus Udd



Revised schedule

Week 17

- 23.4. Shekhar & al. 2003: A Unified Approach to Detecting Spatial Outliers
Pekka Maksimainen
 - Hyvönen & al. (forthcoming): Multivariate Analysis of Finnish Dialect Data – an overview of lexical variation
Hanna Tikkanen
- 26.4. Summary