

- p Not so good actually
- p It has to do at most n-1 reversals with permutation of length n
- ${\sf p}$  The algorithm can return a distance that is as large as (n 1)/2 times the correct result d(T)
  - n For example, if n = 1001, result can be as bad as 500 x d( $\Pi$ )

# Estimating reversal distance by cycle decomposition

- P We can estimate d(∏) by cycle decomposition
- p Lets represent permutation  $\Pi$  = 1 2 4 5 3 with the following graph



where edges correspond to adjacencies (identity, permutation F)





## Cycle decompositions

- p Cycle decomposition is NP-complete
   n We cannot solve the general problem exactly for large instances
- P However, with signed data the problem becomes easy
  - n Before going into signed data, lets discuss another algorithm for the general case

#### Computing reversals with breakpoints

- p Lets investigate a better way to compute reversal distance
- p First, some concepts related to permutation  $\prod_{1}\prod_{2,..}\prod_{n-1}\prod_{n}$ 
  - n Breakpoint: two elements  $\prod_i$  and  $\prod_{i+1}$  are a breakpoint, if they are not consecutive numbers
  - n Adjacency: if  $\Pi_i$  and  $\Pi_{i+1}$  are consecutive, they are called adjacency











#### Improved breakpoint reversal sort

- 1. While  $b(\Pi) > 0$
- 2. If ∏ has a decreasing strip
- 3. Do reversal p that removes most BPs
- 4. Else
- 5. Reverse an increasing strip
- 6. Output ∏
- 7. return

## Is Improved BP removal enough?

- p The algorithm works pretty well:
  - n It produces a result that is at most four times worse than the optimal result
  - n ... is this good?
- P We considered only reversals
- p What about translocations & duplications?





- minimum reversal distances is NPcomplete
  - n Why is this so if sorting is easy?
- P An algorithm has been developed that achieves 1.375-approximation
- p However, reversal distance in signed data can be computed quickly!
  - n It takes linear time w.r.t. the length of permutation (Bader, Moret, Yan, 2001)

#### Cycle decomposition with signed data

- p Consider the following two permutations that include *orientation* of markers n J: +1 +5 -2 +3 +4 n K: +1 -3 +2 +4 -5
- p We modify this representation a bit to include both endpoints of each marker:
  n J': 0 1a 1b 5a 5b 2b 2a 3a 3b 4a 4b 6
  n K': 0 1a 1b 3b 3a 2a 2b 4a 4b 5b 5a 6

### Graph representation of J' and K'

p Drawn online in lecture!

#### Multiple chromosomes

- P In unichromosomal genomes, inversion (reversal) is the most common operation
- p In multichromosomal genomes, inversions, translocations, *fissions* and *fusions* are most common

### Multiple chromosomes

p Lets represent multichromosomal genome as a set of permutations, with \$ denoting the boundary of a chromosome:

5	9	\$	Chr 1
1	3	283	\$ Chr 2
7	6	4\$	Chr 3

This notation is frequently used in software used to analyse genome rearrangements.

#### Multiple chromosomes

 P Note that when dealing with multiple chromosomes, you need to specify numbering for elements on both genomes



#### **Fusions & fissions**

- p Fusion: merging of two chromosomes
- p Fission: chromosome is split into two chromosomes
- p Both events can be represented with a translocation





## Algorithms for general genomic distance problem

P Hannenhalli, Pevzner: Transforming Men into Mice (polynomial algorithm for genomic distance problem), 36th Annual IEEE Symposium on Foundations of Computer Science, 1995

#### Human & mouse revisited

- P Human and mouse are separated by about 75-83 million years of evolutionary history
- P Only a few hundred rearrangements have happened after speciation from the common ancestory
- P Pevzner & Tesler identified in 2003 for 281 synteny blocks a rearrangement from mouse to human with
  - n 149 inversions
  - n 93 translocations
  - n 9 fissions

#### Discussion

- p Genome rearrangement events are very rare compared to, e.g., point mutations
   n We can study rearrangement events further back in the evolutionary history
- P Rearrangements are easier to detect in comparison to many other genomic events
- P We cannot detect homologs 100% correctly so the input permutation can contain errors

#### Discussion

- p Genome rearrangement is to some degree constrained by the number and size of repeats in a genome
  - n Notice how the importance of genomic repeats pops up once again
- p Sequencing gives us (usually) signed data so we can utilize faster algorithms
- p What if there are more than one optimal solution?





