

Lecture 11 Practical Examples with Specific Problems

Memory Queue
Priorities
Disk Sub-System
CPU Scheduling
Paging

15.4.2002

Copyright Teemu Kerola 2002

1

Flow Equivalent Server

- Fig. 8.2
- Approach OK, if sub-model is “busy” part of model
 - many state transitions within sub-model as compared to transitions between sub-model and rest of the original model
- Hierarchical models
 - orig model, sub-model, aggregate model

15.4.2002

Copyright Teemu Kerola 2002

4

Problems

- Memory queue Simultaneous resource possession
- Disk subsystem Complex sub-model
- CPU scheduling Priorities
- Paging Dependence on other jobs
- General: non-product form

15.4.2002

Copyright Teemu Kerola 2002

2

Non-Product Form Solutions

- Use your imagination and know-how
- Flow equivalence
- Load concealment
- Change model
- Multi-level modeling
- Simulation
- Hybrid simulation

15.4.2002

Copyright Teemu Kerola 2002

3

Modeling Memory

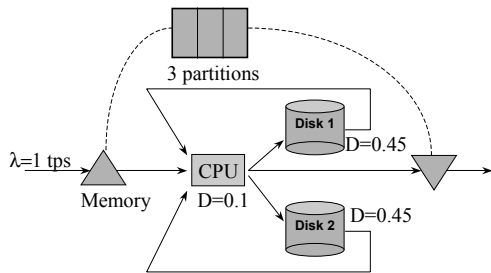
- Fig. 8.1
- Original model not product form
- Use FESC, max mpl 5
 - short cut sub-system to closed model
 - solve for all $mpl = \{1, 2, 3, 4, 5\}$
 - create service times for FESC: $S^{FESC}(k) = 1/X^{SUBSYS}(k)$
 - solve new model (or models), Fig. 8.3
 - solve open class first, slow down FESC
 - solve closed class

15.4.2002

Copyright Teemu Kerola 2002

6

Memory Constraint, One Class



Not product form! Why? Simultaneous resource possession

15.4.2002

Copyright Teemu Kerola 2002

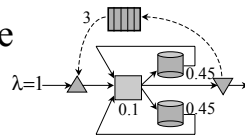
source:[Men 94, p. 239]
7

15.4.2002

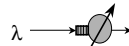
Copyright Teemu Kerola 2002

10

One Class Example



- Isolate system, use shortcuts
- Solve product form model for $mpl=\{1,2,3\}$
 - use MVA: $X=\{1, 1.413, 1.623\}$
- Create FESC: $S(n) = \{1, 1/1.413, 1/1.623, 1/1.623, \dots\}$
 $= \{1, 0.708, 0.616, 0.616, \dots\}$
- Create new model
 - birth-death process
 - state dependent serv. rate: $X=\{1, 1.413, 1.623\}$



15.4.2002

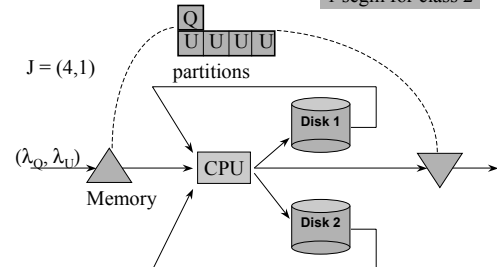
Copyright Teemu Kerola 2002

8

Memory Constraint, Many Classes

- Each class c has its own constraints J_c
 - each class in its own domain
 - classes are independent

4 segm for class 1
1 segm for class 2

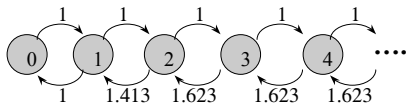


15.4.2002

Copyright Teemu Kerola 2002

11

Solve Birth-Death Model ⁽⁵⁾



$P_0 = 0.260, P_1 = 0.260, P_2 = 0.184, P_3 = 0.113,$
 $P_{N>3} = 1 - 0.260 - 0.260 - 0.184 - 0.113 = 0.183$

average jobs in mem = $0 * P_0 + 1 * P_1 + 2 * P_2 + 3 * (P_3 + P_{N>3})$
 $= 0.260 + 2 * 0.184 + 3 * 0.296 = 1.516$

average number of waiting for memory jobs: $N_w = \sum_{i=1}^{\infty} i P_{i+3} = \frac{P_0 \lambda^3}{\mu_1 \mu_2 \mu_3} \frac{\lambda / \mu_3}{[1 - (\lambda / \mu_3)]^2} = 0.474$

total popul = $1.516 + 0.474 = 1.99$

time spent in memory queue: $0.474/1.99 = 23.8\%$

15.4.2002

Copyright Teemu Kerola 2002

9

Multiple Domain Solution

- Assumptions
 - Class r population is independent of population in other classes
 - Throughput in class r depends only on *average* populations in other classes:

$$X_r(n_r) = f(\bar{n}_1, \bar{n}_2, \dots, n_r, \dots, \bar{n}_R)$$

- Iterative solution, one class at a time
 - solution for each class is not quite simple...

15.4.2002

Copyright Teemu Kerola 2002

12

Model with Memory, Multiple Classes Iterative Solution

- Guess initial average populations \bar{N}
- Solve one class r at a time for population $\bar{N} = (\bar{n}_1, \bar{n}_2, \dots, \bar{n}_r, \dots, \bar{n}_R)$
 - Get new average population for each class r : $\bar{n}_r, X_r, R_r, U_{kr}$
 - $\bar{N} = (\bar{n}_1, \bar{n}_2, \dots, \bar{n}_r, \dots, \bar{n}_R)$
- Iterate until “convergence”
 $\bar{N} = (2.1, 5.3, 2)$

15.4.2002

Copyright Teemu Kerola 2002

13

Iterative Memory Solution (contd)

- 4. Iterate step 3 until convergence
- 5. Get performance results for constrained classes c from the latest solutions for each such class
- 6. Solve model for unconstrained classes, using fixed \bar{n}_c 's constrained classes

15.4.2002

Copyright Teemu Kerola 2002

16

Iterative Memory Solution

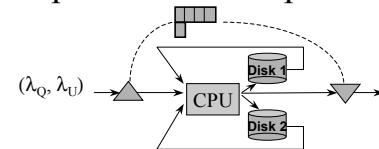
- 1. Initialize
 - solve network without memory queue
 - get average popul. for each class: \bar{n}_r^{nomem}
 - set initial $\bar{n}_r = \min(\bar{n}_r^{nomem}, J_r)$
- 2. Create transformed model
 - remove memory constraint
 - make all memory constrained classes c closed (batch) job classes

15.4.2002

Copyright Teemu Kerola 2002

14

Multiple Class Example



- Two class model, Tbl 8.1
- Step 1. Solve open model without memory constraint

$$\bar{n}^{nomem} = (6.0192, 0.8540) \quad \text{max pop = max mpl}$$

$$\text{init } \bar{n} = (\bar{n}_Q, \bar{n}_U) = (4.0, 0.8540)$$

15.4.2002

Copyright Teemu Kerola 2002

17

Iterative Memory Solution (contd)

- 3. Solve the model for all constrained classes c , one class at a time:
 - solve it for populations $\bar{N} = (\bar{n}_1, \bar{n}_2, \dots, \bar{n}_c, \dots, \bar{n}_R)$
 - $\bar{N} = (\bar{n}_1, \bar{n}_2, \dots, 2, \dots, \bar{n}_R)$
 - $\bar{N} = (\bar{n}_1, \bar{n}_2, \dots, J_c, \dots, \bar{n}_R)$
 - Approx MVA... why? population not integers!
 - get $X_c(n_c)$ for this class $\forall n_c \in \{1, \dots, J_c\}$
 - create single class memory queue birth-death model for class c , with system as FESC
 - solve it, get new \bar{n}_c = "average number of jobs in memory"
 - iterate until “done”

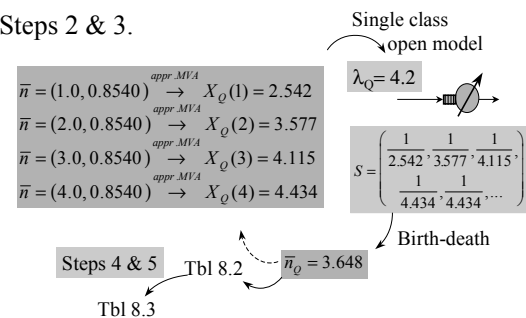
15.4.2002

Copyright Teemu Kerola 2002

15

Multiple Class Example (contd)

- Steps 2 & 3.



15.4.2002

Copyright Teemu Kerola 2002

18

15.4.2002

Copyright Teemu Kerola 2002

19

Many Priority Levels

- Generalized solution method for many priority levels
- Each level (but the one with highest priority) will get their own shadow server

Alg. 11.1 [LZGS 84]

- Shadow server utilizations of no use

15.4.2002

Copyright Teemu Kerola 2002

22

Priorities with Shadow Server

- Two job classes: Tbl 8.6
- No priorities: $R = (2.69, 8.19)$ appr. MVA $(2.37, 6.74)$ from PMVA

PMVA listing fig.8.6a.out

15.4.2002

Copyright Teemu Kerola 2002

20

Another Simple Example

(from Distr. OS homework)

- We consider a supermarket with one check-out ("kassa"). A client arrives once every 3 minutes, and the average service time is 2.5 minutes. During a day, how long is the check-out clerk idle? On the other hand, how long will a client spend in the queue?
- Every fifth client has only one purchase, and for him/her the service time is only half a minute. The manager wants to improve the service for these "express clients". Two alternatives are considered: 1) an "express client" may pass the queue (but he/she is or she is not allowed to interrupt an ongoing service), 2) a new check-out is established for the "express clients".
- How would these alternatives affect the performance of the check-out service? Which alternative is better?
- How would it be possible to guarantee "express service" for "express clients" that the total delay is less than one minute?

15.4.2002

Copyright Teemu Kerola 2002

23

Shadow Server

- Class P: CPU "just for it"
- Class D: sees a "shadow" CPU as slower device
 - how much slower? $1/(1-U_{CPU,P}) = 1/(1-0.291)$
 - inflate demands D_{kD} this much for class D
- Get: model with no priorities

PMVA listing fig.8.6b.out
 Fig 8.6 [Men 94]
 PMVA listing fig.8.6.out

15.4.2002

Copyright Teemu Kerola 2002

21

Another Simple Example (contd)

- Basic 1-class solution
- Priority pre-emptive solution
- Priority non pre-emptive solution
- 2-server solution
- Basic 2-class solution

slides ASE 1-3
 slide ASE 4
 slides ASE 5-7
 slide ASE 8
 slides ASE 9-13

15.4.2002

Copyright Teemu Kerola 2002

24

15.4.2002Copyright Teemu Kerola 200225

Paging (contd)

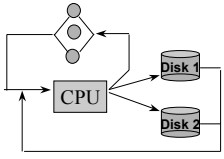
$$D_{disk}^{paging} = \frac{D_{cpu}^{paging}}{IFT(f)} S_{disk}^{paging} = \frac{D_{cpu}^{paging}}{D_{cpu} \left[1 + \left(\frac{a}{NP/n} \right)^2 - \left(\frac{a}{F} \right)^2 \right]} S_{disk}^{paging}$$
$$= \left[1 + \left(\frac{a}{NP/n} \right)^2 - \left(\frac{a}{F} \right)^2 \right] S_{disk}^{paging}$$

F = nr of frames in virtual addr space

$$D_{disk} = \begin{cases} D_{disk}^{file} + D_{disk}^{paging} & \text{if } nF > NP \\ D_{disk}^{file} & \text{o / w} \end{cases}$$

15.4.2002Copyright Teemu Kerola 200228

Paging



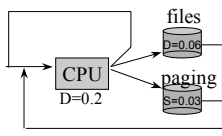
- Page fault rate depends on behaviour of other jobs, and total number of jobs in system
- Is paging disk the same unit as for files?

$$D = D_{paging} + D_{file}$$

nr of page faults * Spaging

15.4.2002Copyright Teemu Kerola 200226

Paging Example



- Memory NP=10M/1K=10K=10240
- Virt. addr. space = 2 MB
 - nr virt pages F = 2MB/1K = 1K = 2048
- match IFT(f) to data: magic a=4000

$$D_{d2}(n) = D_{d2}^{paging}(n) = \left[1 + \left(\frac{4000}{10240/n} \right)^2 - \left(\frac{4000}{2048} \right)^2 \right] * 0.03$$
$$= [1 + 0.153n^2 - 3.81] * 0.03 \text{ if } n > \frac{NP}{F} = \frac{10240}{2048} = 5$$
$$D_{d2}(n) = 0 \text{ o / w (i.e., } n \leq 5 \text{)}$$

15.4.2002Copyright Teemu Kerola 200229

Paging (contd)

- Nr of page faults?
 - Fig 8.8
 - Fig. 9.5 from [LZGS 84]
 - Nr page faults:

$$\frac{D_{cpu}}{IFT(f)} = \frac{D_{cpu}}{IFT(\frac{NP}{n})}$$

total Nr of Pages

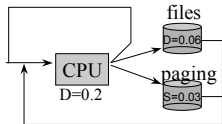
6 sec

1.5 sec / fault = 4 faults

nr of frames in average

15.4.2002Copyright Teemu Kerola 200227

Paging Example (contd)



- Modify MVA to account for varying demand
- Solve, get system throughput as fn of load
 - Fig. 8.9
- X, R, U as function of load:
 - Figs. 9.6-9.8 from [LZGS 84]

15.4.2002Copyright Teemu Kerola 200230