582670 Algorithms for Bioinformatics

Lecture 1: Primer to algorithms and molecular biology

3.9.2013

These slides are based on previous years’ slides of Leena Salmela and Veli Mäkinen
Course format

Thursday 12-14

Tuesday 12-14

Tuesday 10-12
Grading

- Exam 48 points
- Exercises 12 points
  - 30% $\Rightarrow$ 1
  - 85% $\Rightarrow$ 12
- Grading $\sim$ 30 $\Rightarrow$ 1, $\sim$ 50 $\Rightarrow$ 5 (depending on difficulty of exam)
- Tuesday study group is mandatory!
  (Inform beforehand if you cannot attend)
Course overview

- Introduction to algorithms in the context of molecular biology
- Targeted for
  - biology and medicine students
  - first year bioinformatics students
  - CS / Math / Statistics students thinking of specializing in bioinformatics
- Some programming skills required
  - We will use Python in this course
- Not as systematic as other CS algorithm courses, emphasis on learning some design principles and techniques with the biological realm as motivation
Algorithms for Bioinformatics

- State-of-the-art algorithms in bioinformatics are rather involved.
- Instead, we study toy problems motivated by biology (but not too far from reality) that have clean and introductory level algorithmic solutions.
- The goal is to arouse interest to study the real advanced algorithms in bioinformatics!
- We avoid statistical notions to give algorithmic concepts the priority.
- Continue to further bioinformatics course to learn the practical realm.
Algorithm

Well-defined problem  Solution to problem

input  →→→  . . .  →  output

number of steps:  \( f(\text{size of input}) \)

Homework:
Find out what the following algorithm running time notions mean:

\[
\begin{align*}
 f(n) & \in O(g(n)) & g(n) & \in \Omega(f(n)) \\
 f(n) & \in o(g(n)) & g(n) & \in \omega(f(n)) \\
 f(n) & \in \Theta(g(n))
\end{align*}
\]
Algorithms in Bioinformatics

Weakly defined problem

\[
\begin{align*}
\text{input} & \rightarrow \text{output} = \text{input}' \rightarrow \text{output}' = \text{input}'' \rightarrow \text{output}''
\end{align*}
\]

Solution to problem

Reasons:
- Biological problems usually too complex to admit a simple algorithmic formulation
- Problem modeling sometimes leads to statistical notions

Problematic for CS theory:
- Optimal solutions to subproblems do not necessarily lead to best global solution
Algorithms in Bioinformatics

Plenty of important subproblems where algorithmic techniques have been vital:

- Fragment assembly $\implies$ human genome
- Design of microarrays $\implies$ gene expression measurements
- Sequence comparison $\implies$ comparative genomics
- Phylogenetic tree construction $\implies$ evolution modeling
- Genome rearrangements $\implies$ comparative genomics, evolution
- Motif finding $\implies$ gene regulatory mechanism
- Biomolecular secondary structure prediction $\implies$ function
- Analysis of high-throughput sequencing data $\implies$ genomic variations in populations
Course prerequisites

- Programming skills
- High-school level biology++
  - 57780: Molecular genetics reading group recommended to be taken in parallel
  - To avoid overlap with other bioinformatics courses, we do not cover any more biology than is necessary to motivate the problems
Programming in this Course

- We will use Python
- What we need (in this course):
  - Built-in data types
  - Syntax for control flow statements
  - Function definitions
- What we can omit (i.e. software engineering):
  - Standard library, OOP, exceptions, I/O, etc.
Assignment

<table>
<thead>
<tr>
<th>Pseudocode</th>
<th>Python</th>
</tr>
</thead>
<tbody>
<tr>
<td>$b \leftarrow 2$</td>
<td>$b = 2$</td>
</tr>
<tr>
<td>$a \leftarrow b$</td>
<td>$a = b$</td>
</tr>
<tr>
<td></td>
<td><code>print a</code></td>
</tr>
</tbody>
</table>
# Arithmetic

## Pseudocode

<table>
<thead>
<tr>
<th>Step</th>
<th>Equation</th>
</tr>
</thead>
<tbody>
<tr>
<td>1.</td>
<td>$dx \leftarrow (x_2 - x_1)^2$</td>
</tr>
<tr>
<td>2.</td>
<td>$dy \leftarrow (y_2 - y_1)^2$</td>
</tr>
<tr>
<td>3.</td>
<td>return $\sqrt{dx + dy}$</td>
</tr>
</tbody>
</table>

## Python

```python
from math import sqrt

def dist(x1, y1, x2, y2):
    dx = pow(x2-x1, 2)
    dy = pow(y2-y1, 2)
    return sqrt(dx+dy)

print dist(0, 0, 3, 4)
```
Conditional

Pseudocode

MAX (a, b)
1 if (a < b)
2 return b
3 else
4 return a

Python

def MAX(a, b):
    if a < b:
        return b
    else:
        return a

print MAX(1, 99)
for loops

Pseudocode

SumIntegers \( (n) \)

1. \( sum \leftarrow 0 \)
2. for \( i \leftarrow 1 \) to \( n \)
3. \( sum \leftarrow sum + i \)
4. return \( sum \)

Python

```python
def SUMINTEGERS(n):
    sum = 0
    for i in range(1, n+1):
        sum = sum + i
    return sum

print SUMINTEGERS(10)
```
while loops

**Pseudocode**

AddUntil (b)
1  \( i \leftarrow 1 \)
2  \( total \leftarrow i \)
3  while \( total \leq b \)
4     \( i \leftarrow i + 1 \)
5  \( total \leftarrow total + i \)
6 return \( i \)

**Python**

```python
def ADDUNTIL(b):
    i = 1
    total = i
    while total <= b:
        i = i + 1
        total = total + i
    return i

print ADDUNTIL(25)
```
Recursion

Pseudocode

\[ F(n) = \begin{cases} 
0, & \text{when } n = 0 \\
1, & \text{when } n = 1 \\
F(n - 1) + F(n - 2), & \text{otherwise} 
\end{cases} \]

Python

def RECURSIVEFIBONACCI(n):
    if n == 0:
        return 0
    elif n == 1:
        return 1
    else:
        a = RECURSIVEFIBONACCI(n-1)
        b = RECURSIVEFIBONACCI(n-2)
        return a+b

print RECURSIVEFIBONACCI(8)
### Lists

#### Python

<table>
<thead>
<tr>
<th>Code</th>
<th>Output</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>l = [0] * 3</code></td>
<td><code>[0,0,0]</code></td>
</tr>
<tr>
<td><code>l[0] = 1</code> # list is mutable</td>
<td><code>[1,0,0]</code></td>
</tr>
<tr>
<td><code>l = range(1,4)</code></td>
<td><code>[1,2,3]</code></td>
</tr>
<tr>
<td><code>l.append('four')</code></td>
<td><code>[1,2,3,'four']</code></td>
</tr>
<tr>
<td><code>l = [2**i for i in range(6)]</code></td>
<td><code>[1,2,4,8,16,32]</code></td>
</tr>
<tr>
<td><code>l2 = l[2:4]</code></td>
<td><code>[4,8]</code></td>
</tr>
</tbody>
</table>
## List access

### Pseudocode

FIBONACCI \((n)\)

1. \(F_0 \leftarrow 0\)
2. \(F_1 \leftarrow 1\)
3. for \(i \leftarrow 2\) to \(n\)
4. \(F_i \leftarrow F_{i-1} + F_{i-2}\)
5. return \(F_n\)

### Python

def FIBONACCI(n):
    F = [0]*(n+1)
    F[0] = 0
    F[1] = 1
    for i in range(2,n+1):
        F[i] = F[i-1] + F[i-2]
    return F[n]

print FIBONACCI(8)
## Strings

<table>
<thead>
<tr>
<th>Python</th>
<th>Output</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>s='Hello'</code></td>
<td></td>
</tr>
<tr>
<td><code>s[0] = 'C'</code> # error: str</td>
<td></td>
</tr>
<tr>
<td><code>s.append('!')</code> # is immutable</td>
<td></td>
</tr>
<tr>
<td><code>s = s + '!'</code></td>
<td></td>
</tr>
<tr>
<td><code>s = s[:5]</code></td>
<td></td>
</tr>
<tr>
<td><code>s = s.upper()</code></td>
<td></td>
</tr>
</tbody>
</table>

### Output

- `Hello`  
- `Hello!`  
- `Hello`  
- `HELLO`
Immutable vs Mutable

**Immutable (int, str, ...)**

a = 2
b = a
b = b + 1  # does not change a
s = 'Hello'
t = s
t = t + '!'  # does not change s

**Mutable (list, set, dict, ...)**
l = [0]
m = l
m = m + [1]  # changes also l

l = [0]
m = l
m = [1]  # does not change l

l = [0]
m = l[:]: # shallow copy of l
m = m + [1]  # does not change l

**Immutable (int, str, ...)**

```python
def ADDONE(x,y):
    x = x + 1  # x and y
    y = y + 1  # are local

def ADDONE(x,y):
    return x+1, y+1
```

```python
x,y = ADDONE(x,y)
```

**Mutable (list, set, dict, ...)**

```python
def CLEAR(l):
    l = []  # l is local

    # any mutable can still be
    # changed in place, e.g.:
    def CLEAR(l):
        l[:]= []

    def ADDONE(l,i):
        l[i] = l[i] + 1

def ADDONE(l,i):
    l[i] = l[i] + 1
```
## Multidimensional lists

### Python

```python
l = [[0] * 2] * 3  # Caution!
  # You probably
  # don’t want
  # to do this!

l[0][0] = 1

# This is safe:
l = [[0]*2 for i in range(3)]

l[0][0] = 1
```

### Output (print l)

```
[[0, 0], [0, 0], [0, 0]]
[[1, 0], [1, 0], [1, 0]]
[[0, 0], [0, 0], [0, 0]]
[[1, 0], [0, 0], [0, 0]]
```
Idea

Python (collections.deque)

```python
from collections import deque

def FIBONACCI(n):
    F = deque()
    F.append(0)
    F.append(1)
    for i in range(2, n+1):
        F.append(F[n-1]+F[n-2])
    return F[n]

print FIBONACCI(8)
```
Idea

Store max key and max value of each subtree to the nodes

Python

- No built in data type (several external libraries exist)
- For many purposes hash-based dictionary type `dict` is enough:
  - Stores (key, value) pairs so that value associated with a key can be retrieved efficiently (average constant time)
  - Does not support retrieval by value

```python
fib = {0:0, 1:1, 2:1, 3:2, 4:3, 5:5, 6:8, 7:13, 8:21}
print fib[8]
```
Large(r) data sets

- For mutable strings, use e.g.
  - array.array('c', 'Hello')
  - bytearray('Hello')
- list uses a lot of memory (∼16 bytes per int)
- For homogeneous data, use e.g.
  - array.array('l', [1,2,3,4])
  - numpy.array([1,2,3,4])
Helpful links

- http://openbookproject.net/thinkcs/python/english2e/ (Programming tutorial for those who have no programming experience)
- http://docs.python.org/tutorial/
- http://docs.python.org/library/
- http://docs.scipy.org/doc/ (NumPy documentation)
Outline

Crash Course in Python

Study Group Assignments
One of the fundamental and most deeply studied algorithmic problems is sorting. Before coming to the study group familiarize yourself with the problem (e.g. using Wikipedia) and be ready to explain the idea of couple of well-known sorting algorithms like insertion sort, quicksort, merge sort, and radix sort.

At study group, try to understand the running time $O()$-notion of different sorting algorithms:

- What happens if you are sorting a set of DNA sequences into lexicographic order instead of integers?
- What if the set of DNA sequences consists of all suffixes of one DNA sequence?
Group 2 (students with CS background)

- Study the slides “molecular biology primer” (found on course website) before coming to the study group.
- At study group, be ready to explain the material just using the “molecular biology cheat sheet”.